

Computer simulation of Thermal Focal Length of Laser Crystal and Thermally-Near-Unstable Resonator

Geng Aicong^{1,3}, Li Baohe¹, Chen Xiaobai¹
 Department of Physics
 Beijing Technology and Business University
 Beijing 100048, China

Yang Xiaodong²
 Department of Physics
 Jiaying College
 Meizhou, 515015 China

Yang Mingjiang³
 Institute of mechanics
 Chinese Academy of Science
 Beijing 100190, China

Abstract—A simple method determining the thermal focal length of gain medium was investigated. Then by using computer simulation results, a novel configuration was proposed. In the new configuration, the gain medium acts as a mode limiter at maximal pump power, which restrains resonance of high-order modes and guarantees not only high output power but also high beam quality. An LD side-pumped Nd:YAG laser with output power of 400W at 1064nm was obtained experimentally with the new configuration. The experimental results are in agreement with theoretical predictions.

Keywords- laser; computer simulation; thermal focal length

I. INTRODUCTION

Scaling of the output power and brightness of diode-pumped solid-state laser sources to meet the needs of ever demanding applications continues to preoccupy many within the laser community. The use of a multirod solid-state laser system is one of the most promising approaches to generating a high-power laser beam, at high beam quality, with a wide range of output power [1]. However, when the laser runs at high pump power, thermal lens of every rod induces variations of output beam parameters that could limit the design and operation of solid-state laser devices such as the stability of, width of lasing mode and the beam quality. So it is the effective means by measuring the thermal focal length of gain medium to investigate the thermal effect. General experimental methods of measuring thermal focal length include: probe beam method [2-4], interference detecting method [5], unstable-resonator method [6-7], and transverse mode beat frequency [8]. But experimental steps are usually complex and time-consuming.

In this paper, we propose a simple method determine the thermal focal length of gain medium. Firstly, we could measure the maximum laser resonator length by an asymmetric plat-plat cavity under a certain pump power and deduce the corresponding waist size of the laser with the same parameters. Basing on the theory of standard matrix transform, we can achieve the thermal focal length of gain medium by using of computer simulation. This method has advantages such as

simple setup and easy operation. On basis of the analysis, a novel configuration was proposed. In the new configuration, the gain medium acts as a mode limiter at maximal pump power, which restrains resonance of high-order modes and guarantees not only high output power but also high beam quality. We experimentally gained 400W output power at 1064nm by an LD side-pumped Nd:YAG laser with the new configuration. The experimental results are in agreement with theoretical predictions.

II. THEORETICAL ANALYSIS

We begin by considering in more detail the adverse effects of heat generation within LD-pumped solid-state lasers. In general, a detailed knowledge of thermal lens can be quite difficult as it requires either accurate measurement of the thermally induced phase difference as a function of transverse position, or, if the values of all the required parameters are known, a numerical calculation of thermal lens taking into account the various contributing factors. Alternatively, if axial heat flow is neglected and consideration is limited to the contribution to thermal lens due to the temperature dependence of the refractive index, then an approximate expression for the thermal lens focal length can be gotten as the following[9]

$$f = \frac{KA}{P_d} \left(\frac{1}{2} \frac{dn}{dT} + n_0^3 \alpha C_{r,\phi} + \frac{\alpha r_0 (n_0 - 1)}{L} \right)^{-1} \quad (1)$$

where A is the rod cross-sectional area, K is the thermal conductivity of the laser material, P_d is the total heat dissipated in the rod, dn/dT is the change of refractive index with temperature, α is the thermal expansion coefficient, C_r and C_ϕ are functions of the elasto-optical coefficients for radial and tangential component of the polarized light, L is the sample length, r_0 is the radius of the laser rod, n_0 is the refractive index in the center of the rod.

It can be seen from the above formula that, laser rod thermal focal length is determined by many factors, which are difficult to obtain accurately. A simple theoretical calculation can not truly reflect the characteristics of thermal focal length.

Therefore, by combining experimental method with computer simulation calculation, we accurately measured the thermal focal length simply and practically.

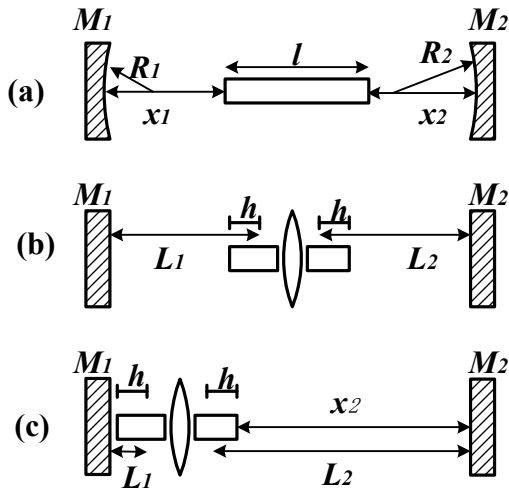


Figure 1. (a) Schematic representation of a simple laser cavity of length $x_1 + x_2 + l$. The laser rod is of length l ; (b) The laser rod is replaced by isotropic material and a thin lens, the cavity arms are measured from the principal plane, h ; (c) Ideal asymmetrical resonator where the laser rod is approximated by a thin lens.

The modeling analysis of this laser system is complicated because the transverse mode structure is dependent on the strength of thermal lens; to simplify analysis we make the assumption that the essential characteristics of the laser cavity (when approaching instability) can be modeled as the lowest order transverse mode. The stability of a laser resonator can be characterized by its equivalent g-parameters [10], where the rod can be approximated to first order by a thin spherical lens of focal length f , hence

$$g_1 = 1 - \frac{L_2}{f} - \frac{L'}{R_1} \quad (2)$$

and

$$g_2 = 1 - \frac{L_1}{f} - \frac{L'}{R_2} \quad (3)$$

where

$$L' = L_1 + L_2 - \frac{L_1 L_2}{f} \quad (4)$$

For the above equations, f is the thermal focal length of gain medium, $R_{1,2}$ are the radius of curvature of the end mirrors and the lengths of the cavity arms are $L_{1,2}$ as shown in Fig. 1(a). x_1, x_2 are the distances between the mirror and the corresponding end of the rod. The laser rod (of length l) can be approximated by a thin lens plus a length of isotropic medium of refractive index n_0 with the principal planes (h) of the lens defined from the ends of the laser rod. This is shown schematically in Fig. 1(b). At long focal lengths, it can be assumed the principle

plane position (hence arm length) is independent of induced focal length, i.e.

$$h = \frac{l}{2n_0} \quad (5)$$

Considering the length of the rod then

$$L_1 = x_1 + h \quad L_2 = x_2 + h \quad (6)$$

To simplify the analysis and experiment the cavity mirrors are chosen to be plane parallel. The cavity stability equation is

$$0 < g_1 g_2 = \left(1 - \frac{L_1}{f}\right) \left(1 - \frac{L_2}{f}\right) < 1 \quad (7)$$

Hence the cavity stability of this simple resonator is dependent only on the focal length (f) of the intra-cavity lens and the length of the cavity ($x_1 + x_2 + l$).

In conventional design, the cavity is configured so that the two arms of the cavity are equal. At the critical rod focal length corresponding to $f = L_1 = L_2$, the transverse laser modes are unstable. However, exact symmetrical cavity demands high precision and difficult to handle. Then we introduced asymmetrical cavity, $L_1 \neq L_2$, as shown in Fig. 1(c). For increasing focal strength the asymmetrical cavity changes from $g_1 \cdot g_2 = 1$ to $g_1 \cdot g_2 = 0$ in a resonator stability diagram. At the critical rod focal length corresponding to $g_1 \cdot g_2 = 0$, the transverse laser modes are unstable. The cavity stability equation, simplifies to

$$f = L_2 = x_2 + \frac{l}{2n_0} \quad (8)$$

When measuring thermal focal lengths at different pump power, the position of the laser module and the cavity mirror M_1 can be fixed, and only the position of cavity mirror M_2 need to be change. Therefore, this method has advantages such as simple setup and easy operation.

III. EXPERIMENTAL RESULTS

On the basis of the above theory, the thermal focal length was measured accurately, and then a thermally-near-unstable resonator was proposed. By using ABCD ray propagation matrix as an auxiliary tool [11], the beam radius of fundamental mode on the Nd:YAG rod and the cavity mirror was computer simulated.

As shown in Fig.2, in this new resonator, when the laser works at maximal pump power, which is the power stable point, the laser is thermally-near-unstable. The laser beam size on the Nd:YAG rod is larger than that on the cavity mirror. Therefore, gain medium acts as a mode limiter at maximal pump power, which restrains resonance of high-order modes and guarantees not only high output power but also high beam quality. Finally, we experimentally gained 400W output power

at 1064nm by an LD side-pumped Nd:YAG laser with the new configuration. The output power as a function of the LD pump current is showed in fig.3. The experimental results are in agreement with theoretical predictions.

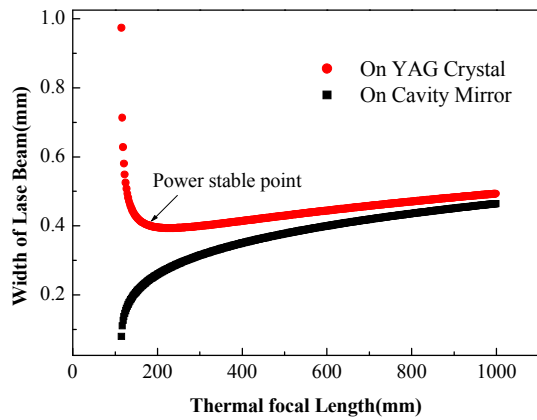


Figure 2. The beam radius of fundamental mode on the Nd:YAG rod and the cavity mirror at different thermal focal length

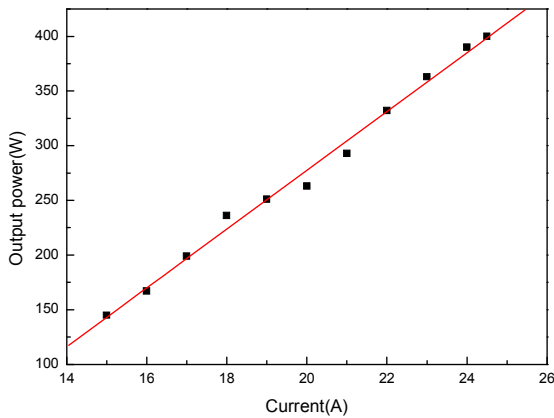


Figure 3. Experimental output power as a function of the LD pump current

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