



Catalytic oxidation of methane over PdO in wire microcalorimetry

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ABSTRACT

A two-dimensional model of a weakly buoyant flow over a horizontal wire with surface reaction was developed, using a literature mechanism, to simulate the heat release rate of the catalytic oxidation of methane (2 vol.% in air) over a Pd wire with a porous 1–2 μm PdO surface layer, acquired by wire microcalorimetry over the temperature range of 600–770 K. The experimental and simulation results demonstrate that the catalytic oxidation is characterized by a low-temperature, reaction-controlled regime in which the internal pore surface is totally accessible to the reactions, and a high-temperature regime in which finite-rate pore diffusion also affects the overall heat release rate. Furthermore, the controlling reactions are identified to be the oxidative adsorption of methane, desorption of oxygen, and adsorption of oxygen, with the former two being facilitating and the last retarding. The reaction mechanism was modified using the response surface methodology and the experimental data in the low-temperature reaction-controlled regime, yielding satisfactory prediction of the global activation energy and identification of the role of oxygen coverage in the transition of the global activation energy.

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1. Introduction

The potential use of methane as a fuel for aero-propulsion is based on the consideration of its greater heat sink capacity, reduced coking propensity than conventional jet fuels, and its higher volumetric energy density than hydrogen in the cryogenic state. Methane, however, is difficult to ignite, and as such presents a significant handicap for such severely residence-time-limited application as supersonic propulsion. Recently it has been suggested that ignition can be catalytically facilitated by seeding the flow with palladium (Pd) or palladium oxide (PdO) nanoparticles generated in situ from a soluble Pd precursor [1].

Since Pd-based catalysts have higher reactivity for methane than other catalysts, the oxidation of methane over them has been extensively studied [2–12]. These studies were mostly focused on certain global aspects of the catalytic process, such as the adsorption of methane [3–5] and oxygen [9], water poisoning [6–8], and the oxidation of Pd [12]. However, only few surface mechanisms were reported. In particular, Sidwell and co-workers proposed a 15-reaction surface mechanism to describe their stagnation flow

experimental data in the catalyst temperature range of 673–1033 K [10], and deduced a global surface mechanism in the temperature range of 953–1383 K [11]. Furthermore, Shimizu et al. [1] experimentally studied the catalytic ignition of methane over in situ generated Pd-based nano-catalyst in a flow tube. A surface mechanism was developed to simulate the experimental data, with good agreement. Experiments were also conducted [13] on the catalytic ignition of methane over PdO using wire microcalorimetry, which offers a well-defined geometry, flow field and catalyst surface. The catalytic ignition temperature and heat release rate were measured for various methane/air concentrations and system pressures, from which the global activation energy and reaction order were extracted.

In view of the simplicity in concept and design of wire microcalorimetry, yielding a well-defined two-dimensional weakly-buoyant flow field which is amenable to accurate computational simulation, the purpose of the present investigation is to simulate the experiment of [13], and through it acquire further understanding of the catalytic ignition process. Our interest includes the assessment and improvement of the catalytic reaction mechanism compiled in [1], the influence of the surface morphology of the catalytic wire on the extent of the catalytic heat release rate, as well as the cause for the existence of a transition temperature in the global activation energy.

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2. Experimental specifications

We briefly describe the experimentation in order to define the experimental situation adopted in the simulation. Wire microcalorimetry [13–15] involves placing a straight catalytic wire in a steady, low-speed gas flow in the cross-stream orientation. By passing an electric current through it, the wire is heated and its temperature is determined through a balance between Joule heat generation and heat loss due to radiation, conduction, and convection to the gas stream. Thus by passing a certain current (I) through the wire, and also by measuring its resistance (R), the power required to maintain the wire at temperature T as $P = I^2R$ can be evaluated, with T simultaneously determined by the property relation $R(T)$. Since there is catalytic heat release at the wire surface, less current is needed to maintain the wire at a certain temperature in the reactive flow, consisting of a mixture of air and fuel, as compared to the nonreactive flow of air. The difference in the power inputs determined in the nonreactive and reactive environments is the catalytic heat release rate (ΔP) of the surface reaction. Experiments for different temperatures were conducted up to 780 K as the wire temperature becomes non-uniform for higher temperatures, caused by the end effect of thermal conduction.

The Pd wire used in the experiment was 105 mm in length and 0.1 mm in diameter (99.99%, Aldrich). Methane (99.98%, Airgas) and high purity air (21% O₂ + 79% N₂, Airgas) were premixed to obtain 2 vol.% methane in air. The wire was subjected to a well-defined pre-treatment process [13] leading to the formation of a porous surface layer of PdO. Surface analysis [13] demonstrated conclusively that, after pre-treatment and throughout experimentation, a 1–2 μm thick PdO layer is formed at the Pd wire surface with a significant porous structure, which results in an increase of the total surface area of the wire.

3. Computational simulation

3.1. Specifics of the computation

Since the weakly buoyant flow field is sufficiently simple and well defined, its simulation was performed by using the commercial software package FLUENT to determine the surface heat release rate of a horizontal cylinder maintained at a given temperature. In particular, since the ratio of the wire length to its diameter is large, the flow around the heated wire can be approximated as a 2D natural convection problem. Furthermore, because of axisymmetry, only half of the cylinder was simulated. Figure 1 shows the mesh, which was created by the software GAMBIT, with a maximum cell squish of 0.13. Quad instead of tri meshes were used for increased accuracy with fewer cells. The area external to the cylinder covering the bulk flow was also resolved with fine meshes because of the importance and complication of the flow around the cylinder. The laminar, viscous flow was solved using pressure-based solver at steady-state conditions. Radiation was not considered because the highest wire temperature was less than 800 K and the wire was very thin. For pressure-velocity coupling, the SIMPLE (Semi-Implicit Method for Pressure Linked Equations) algorithm was used. The discretization scheme was least squares cell based for the gradient, standard for the pressure, and second order upwind for the momentum, energy and species concentrations (O₂, H₂O, CH₄, CO, and CO₂). Since the velocity in the present natural convection flow is very low, the residue values for continuity and momentum were taken as 10⁻⁶ while that for energy as 10⁻¹⁰. The boundary conditions are as follows: the cylinder was defined as a wall with the surface reaction mechanism at constant temperature; bottom, top and side surfaces were defined as the pressure-inlet type and taken as equal to the ambient temperature; the mole

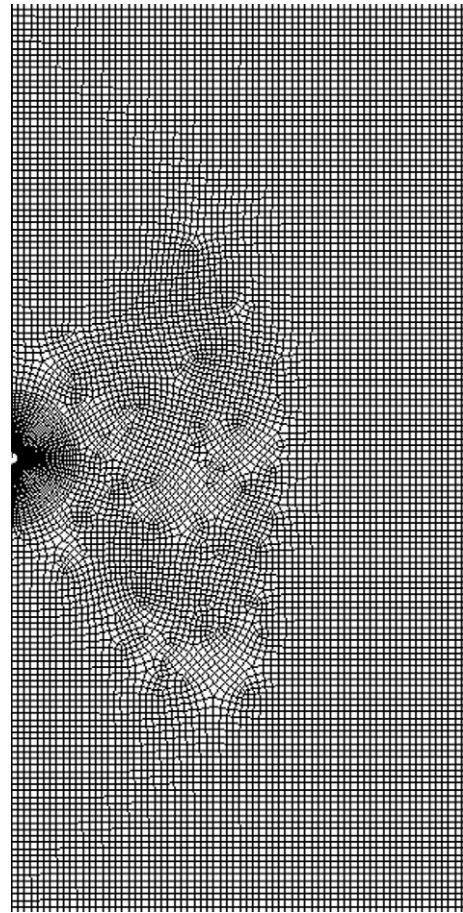


Fig. 1. The grid of the 2D model of the horizontal cylinder.

fraction of each component in the fuel/air mixture was defined as constant at bottom, top and side surfaces. The height of the mesh domain was twice its width. With increasing width of the mesh, the influence of the mesh domain on the heat flux rate of the cylinder was studied. The result shows that the heat flux rate becomes independent of the domain size when the ratio of the domain's width and cylinder's diameter is larger than 60. Thus the ratio was set at 70. The surface reaction mechanism was taken from Ref. [1].

3.2. Validation of the flow model

The model without considering surface reaction was validated by the relation of Rayleigh number (Ra) and Nusselt number (Nu).

$$Ra = GrPr = \frac{g\beta}{\nu\alpha} (T_s - T_\infty) D^3$$

$$Nu = \frac{hD}{\kappa} = \frac{q}{A\Delta T} \frac{D}{\kappa}$$

where Gr is the Grashof number, Pr the Prandtl number, g the gravitational acceleration, β the thermal expansion coefficient, ν the kinetic viscosity, α the thermal diffusivity, T_s the surface temperature, T_∞ the environment temperature, D the diameter of the cylinder, Nu the Nusselt number, h the convective heat transfer coefficient, κ the thermal conductivity, q the heat flow, and A the heat transfer surface area, ΔT difference in temperature of the wire surface and ambient gas. The fluid properties Pr, β , ν , α and κ were evaluated at the film temperature (T_f), which is defined as $T_f = (T_s + T_\infty)/2$. In our case T_∞ is the room temperature and T_s varies in the range of

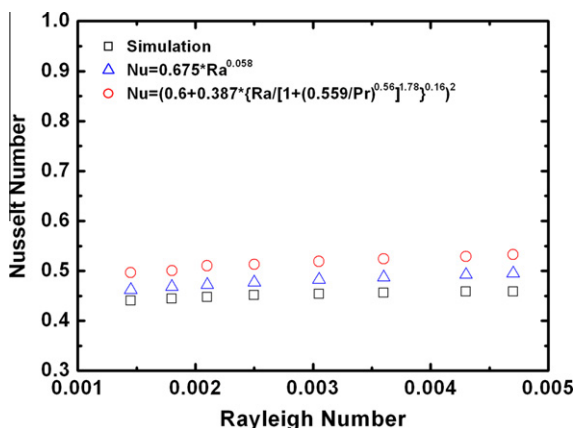


Fig. 2. Dependence of Nusselt Number on Rayleigh Number given by expressions in the literature and determined through the present simulation.

500–1200 K. Correspondingly, Ra is in the range of $1.5\text{--}5 \times 10^{-3}$, implying low Rayleigh number flows. The ratio q/A was calculated, from which Nu was determined.

As shown in Fig. 2, the black blocks represent the calculated relation between Ra and Nu, while the red circles and blue triangles denote the relation of Ra and Nu calculated by using the following two expressions for free-convection heat transfer [16],

$$Nu = \left(0.60 + 0.387 \left(\frac{Ra}{(1 + (0.559/Pr)^{0.56})^{1.78}} \right)^{0.16} \right)^2 10^{-5}$$

$$\leq Ra \leq 10^{12}$$

$$Nu = 0.675 Ra^{0.058} 10^{-10} \leq Ra \leq 10^{-2}$$

It is seen that the values determined by the calculation are very close to those given by the correlations, hence substantiating the adequacy of the computational simulation. It is noted that since the two correlations were obtained by fitting the experimental data in different ranges, they do not overlap in their respective ranges of correlation.

4. Results and discussion

4.1. Heat release rate and effective surface area

In Fig. 3 we compare the experimental data for the catalytic oxidation of 2% CH₄ with the simulated heat release rate per unit area of the cylinder surface, assuming that it is nonporous. It is seen that the simulated results are substantially lower than the corresponding experimental values, with the former approaching the latter only when the wire temperature approaches 780 K. The comparison therefore implies two aspects of the catalytic ignition not adequately captured by the simulation, namely an under-count of the accessible surface area due to the surface porosity, and some intrinsic weakness of the reaction mechanism. Indeed, our previous work [13] on surface characterization demonstrated that a 1–2 μm porous layer was formed at the Pd wire surface, thereby indicating that the surface increase must be considered in the simulation. Furthermore, it is reasonable to expect that the surface area effect dominates at the lower temperature regime, within which the surface reactions are sufficiently slow such that all surfaces are accessible to the reactants through diffusion and reaction is rate controlling.

The increase in the surface area by factors of two and three was considered in Fig. 3. It is seen that these results with augmented surface areas indeed compare closer to the experimental data. Furthermore, since the 2× results are consistently below the

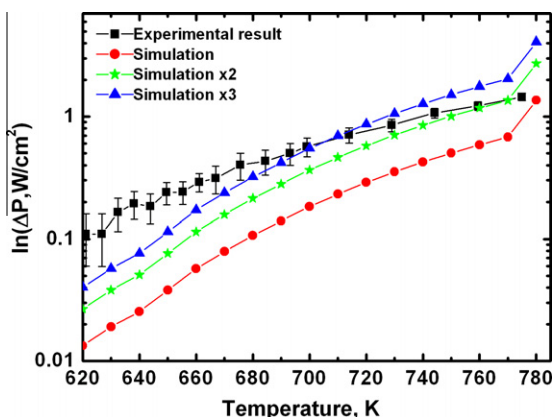


Fig. 3. Comparison of the measured and simulated heat release rate per unit area for the catalytic oxidation of 2% CH₄, allowing for 2× and 3× increase in the accessible surface area due to porosity.

experimental data while the 3× results exceed them at about 700 K, the increase in the surface area should be between 2× and 3×, which is accordant with the finding of Ref. [17] that an increase in the surface area by a factor of two to three through surface roughing during the chemical transformation Pd metal to Pd oxide.

Figure 4 plots the calculated methane concentration next to the surface at different surface temperatures. It is seen that the concentration maintains a nearly constant value below 700 K, but decreases with increasing temperature afterwards. It is noted that although the system is not solely controlled by diffusion above 700 K, a decreasing trend in the mass fraction of methane at the wire surface highlights the influence of mass diffusion over this range. It is therefore reasonable to consider that reactions occur over all available surfaces including the inner surfaces of the pores below the temperature range of 700 K. With increasing temperature, finite-rate mass diffusion becomes more important, leading to less and less surface area within the pore structure is accessed.

4.2. Global activation energy and surface mechanism modification

The global activation energies extracted from the experimental and simulation results were determined and compared. The extraction is based on an overall reaction for complete methane oxidation. A relationship between the surface heat release rate ΔP , and the reaction rate constant k can be expressed as:

$$\Delta P/A = k[\text{CH}_4(\text{g})]^a \Delta H$$

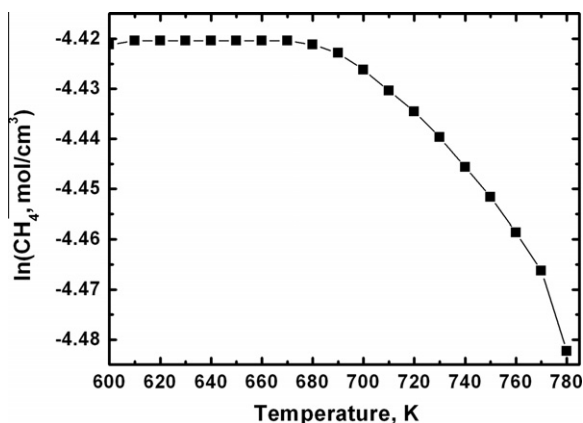


Fig. 4. Simulated mass fraction of methane adjacent to the catalyst with increasing temperature, demonstrating the role of mass diffusion in the transition from low- to high-temperature regimes.

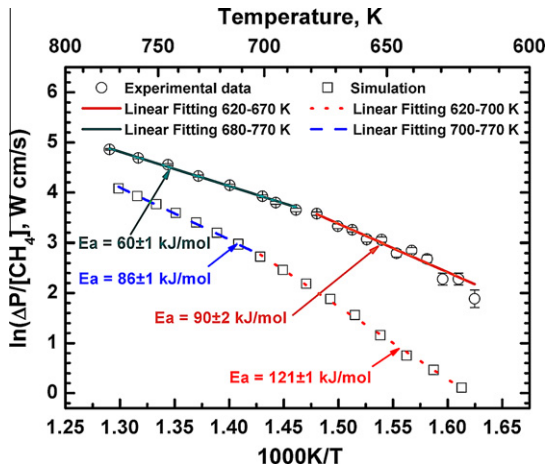


Fig. 5. Global activation energies extracted from the experimental and simulation data.

where A is the surface area, $[CH_4(g)]$ the ambient methane concentration adjacent to the wire surface, a the reaction order with respect to methane, and ΔH the enthalpy change of the overall reaction. In writing the above expression it is recognized that oxygen is in excess, and the products water and CO_2 are continuously removed by the weakly buoyant flow. The reaction order a has been found to be about 1.0 in [13,18,19]. Assuming that ΔH is not temperature dependent in the present narrow temperature range (600–780 K), and that the reaction is Arrhenius, we have

$$\frac{d \ln \left(\frac{\Delta P}{A[CH_4(g)]} \right)}{d(1/T)} = -\frac{E_a}{R} + B.$$

Figure 5 plots the experimental and simulation results of $\ln\{\Delta P/[A[CH_4(g)]]\}$ versus $1000/T$ for 2% methane in the temperature range of 620–770 K, where A is selected as the surface area of the nonporous cylinder. This surface area is proper for simulation study but different from the effective surface area of the experimental study, as discussed in Section 4.1. The reason for not using the effective surface area is that effective surface area is a deduced and inaccurate value, compared with the surface area of the nonporous cylinder. Moreover, it is constant below 700 K, which makes E_a not different from that obtained by using the surface area of the nonporous cylinder. Figure 5 indeed shows a discernible break in the slopes of the experimental results: 90 ± 2 kJ/mol over 620–670 K and 60 ± 1 kJ/mol over 680–770 K. It is noted that the break in slope occurs around the same temperature of about 700 K for the simulated results, although the global activation energies are substantially larger than the corresponding experimental values: 121 ± 1 kJ/mol over 620–700 K, and 86 ± 1 kJ/mol over 700–770 K. It is noted that comparison of E_a from experimental and simulated data is worthy only below 700 K, because the effective surface is completely accessible to reactions and as such remains fixed in the low temperature regime below 700 K, not influencing the slope of the plot. Consequently the extracted global activation energy is indeed a kinetic parameter. However, since the effective surface area is expected to change with increasing temperature above 700 K due to mass diffusion limitation, the activation energy above 700 K is necessarily affected.

Figure 5 shows the obvious difference between the experimental and simulation results below 700 K, which indicates certain inadequacies of the reaction mechanism. Consequently we shall examine the kinetics in this regime, attempting to improve the reaction mechanism. With the improved mechanism we can then study the behavior in the high-temperature regime.

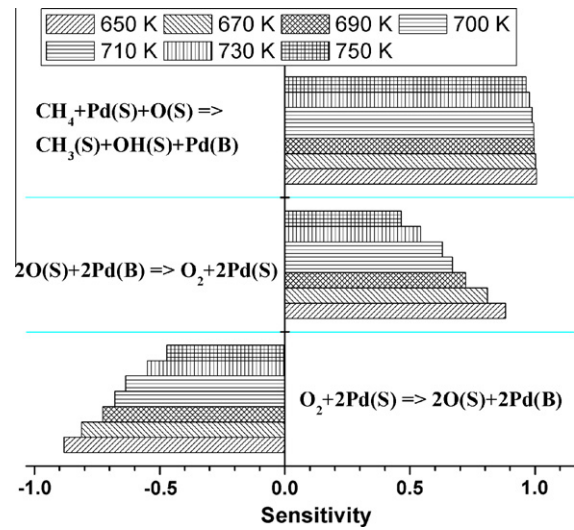


Fig. 6. Sensitivity analysis of the heat release rate for 2% CH_4 at seven different temperatures in the temperature range of 650–750 K. Sensitivity lower than 0.05 not included.

Figure 6 shows the sensitivity analysis of the heat release rate of 2% CH_4 at seven different temperatures over 650–750 K. The sensitivity of the i th surface reaction, S_i , is defined as

$$S_i = \frac{\Delta \ln(hr)}{\Delta \ln(k_i)},$$

where hr and k_i refer to the simulated heat release rate and the rate coefficient of the i th reaction. This sensitivity is calculated through perturbing the rate coefficient k_i by 0.1%.

Three dominant reactions are identified, as also identified in [1]: the oxidative adsorption of methane and desorption of oxygen play a positive role, while the adsorption of oxygen has a negative influence. With increasing temperature the importance of the adsorption and desorption of oxygen reduces, while the oxidative adsorption of methane exerts a large impact. We note in passing that simulations with the mechanism of Sidwell et al. [10] showed a much lower heat release rate for temperatures below 800 K. Compared to the mechanism of Shimizu et al. [1], the mechanism of Sidwell appears to underestimate the importance of the oxidative adsorption of methane and the desorption of oxygen, and overestimate the adsorption of oxygen.

Recognizing that the low-temperature regime, below 700 K, is purely kinetically controlled, we shall optimize the rate coefficients of the three dominant reactions based on our experimental data of a constant effective area. The optimization is based on the response surface methodology [20], which is briefly described here.

Generally, the simulation results are functions of model parameters. For instance, in this work, the simulated heat release rates, Hr_{sim} , depend on the rate coefficients of the three dominant reactions, say k_1 , k_2 , k_3 . Mathematically, Hr can be represented by a Taylor expansion:

$$Hr_{sim} = Hr_0 + \sum_{i=1}^3 a_i \Delta k_i + \sum_{i=1}^3 \sum_{j \geq i}^3 b_{ij} \Delta k_i \Delta k_j + \dots$$

where a_i and b_{ij} characterize the sensitivity of Hr_{sim} to perturbations of rate coefficients and their cross terms. When the rate coefficients vary in a constrained local range of the parameter space, a_i and b_{ij} are almost constant. Therefore, a_i and b_{ij} can be derived from a few tentative computations with slightly varied rate coefficients. Subsequently, corresponding to the experimentally measured heat release rate Hr_{exp} , the optimized rate coefficients can be inversely

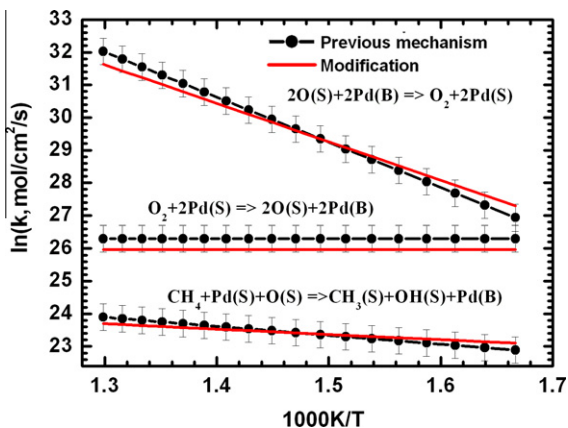


Fig. 7. Optimized rate coefficients of the three dominant reactions in the modified model.

Table 1
Optimized reaction rate coefficients of the three dominant reactions (values from the original model indicated in parenthesis).

Reactions	A	β	Ea (kJ/mol)
$O_2 + 2Pd(s) \rightarrow 2O(s) + 2Pd(B)$	0.6 (0.8) ^a	-0.5 (-0.5)	0.0 (0.0)
$2O(s) + 2Pd(B) \rightarrow O_2 + 2Pd(s)$	2.60E+20 (5.13E+21) ^b	0.0 (0.0)	230.0-132 (115) ₀
$CH_4 + Pd(s) + O(s) \rightarrow CH_3(s) + OH(s) + Pd(B)$	7.7E-3 (4.2E-2) ^a	0.0 (0.0)	10.6 (20.0)

^a Sticking coefficient.

^b Unit for A factor is $cm^2 mol^{-1} s^{-1}$.

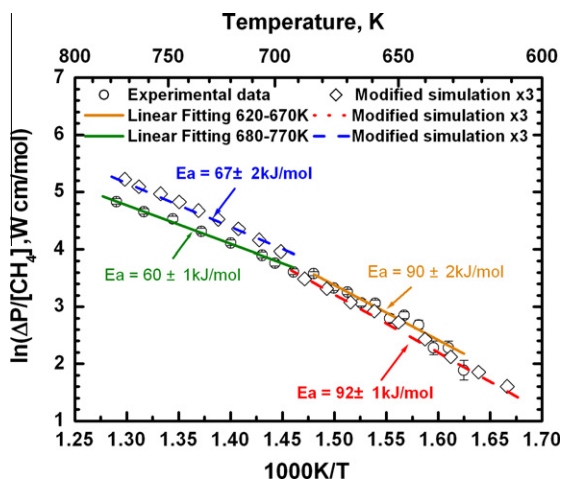


Fig. 8. Comparison of global activation energies deduced from the experimental data and the simulation with the optimized mechanism.

solved. In our case, for a temperature range over 600–700 K, Hr_{sim} is expressed by an expansion of Δk_i up to second-order, which is sufficient for most combustion problems. The rate coefficients are adjusted within $\pm 50\%$ of the original model, which is less than the common factor-of-two uncertainty in model development. The optimized rate coefficients are given in Fig. 7 and Table 1: the difference between the modified and the original rate coefficients is less typically than 25% at various temperatures.

Figure 8 shows the global activation energies deduced by the simulation results with the modified model. It is seen that, below 700 K, the predicted global activation energy of 92 ± 1 kJ/mol is fairly close to that from experimental measurement of 90 ± 2 kJ/mol. In the high-temperature range, the predicted value is

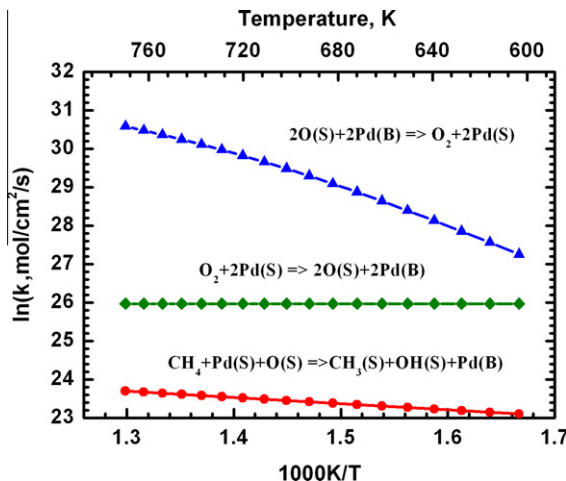


Fig. 9. Arrhenius plots for the three key catalytic reactions.

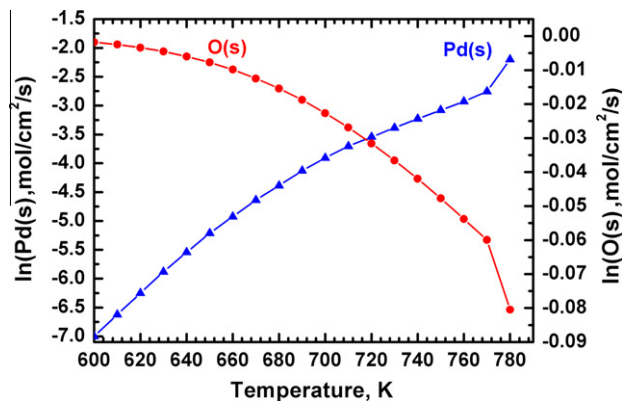


Fig. 10. Prediction fractional surface coverage of Pd(s) and O(s) on the catalyst surface with increasing temperature.

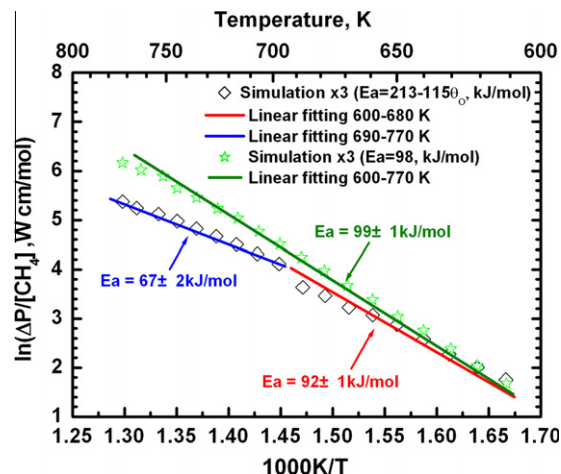


Fig. 11. Comparison of experimental activation energies and simulation with a constant oxygen desorption energy of 98 kJ/mol.

67 ± 2 kJ/mol. It is noted that the variation of effective surface area was not considered in the prediction in the high temperature range. However, it is still interesting that there is a huge difference between two predicted activation energies in the two temperature range.

4.3. Kinetic cause in transition in global activation energy

With the improved kinetic mechanism, we now further study its kinetic implications. Figure 9 plots the rate constants of the three dominant reactions in the Arrhenius form over the temperature range 600–780 K, showing linear variation for the rate constants of oxygen (green diamonds)¹ and methane (red circles) adsorption, while that of oxygen desorption (blue triangles) varies nonlinearly with increasing temperatures above 700 K. This therefore implies constant activation energy for oxidation and methane adsorption, and a varying one for oxygen desorption above 700 K. The transition comes from the oxygen coverage effect on the activation energy of oxygen desorption, $E_a(\text{kJ/mol}) = 230 - 132\theta_{\text{O}}$ (also shown in Table 1). Specifically, Fig. 10 shows that the coverage of O(s) is close to unity below 700 K, but decreases substantially above 700 K and as such affects the activation energy of oxygen desorption, which in turn affects the global activation energy, as observed herein both experimentally and computationally. To further substantiate this hypothesis, simulations with constant oxygen desorption energy of 98 kJ were conducted, yielding a constant global activation energy of 99 ± 1 kJ/mol, with no apparent break in the slope, as shown in Fig. 11.

5. Concluding remarks

In the present investigation we have further demonstrated the usefulness of the microcalorimetry technique in the study of heterogeneous catalytic reactions. Because of the simple and well-defined nature of the design, it can be experimentally set up and computationally simulated expediently and with good accuracy. While the observables are limited to the global properties of the heat release rate as a function of temperature, with the simultaneous determination of the ignition temperature, the controlling reactions can be assessed through simulation with detailed chemistry. Indeed, the present approach is similar to that of measuring the laminar flame speed of a reactive mixture and extracting useful chemical information through simulation with some given reaction mechanism.

For the present problem of the catalytic oxidation of methane/air over a Pd wire with a porous 1–2 μm PdO surface layer, the experimental and simulation results demonstrate that the catalytic oxidation is characterized by a low-temperature, reaction-controlled regime in which the internal pore surface is totally accessible to the reactions, and a high-temperature regime in which finite-rate pore diffusion also affects the overall heat release rate. Furthermore, the heat release rate is found to be primarily affected by the oxidative adsorption of methane together with the adsorption and desorption of oxygen, and the temperature-dependent O(s) surface coverage strongly affects the transition from the low- to the high-temperature regimes.

Quantitatively useful information acquired from the present study include an optimized catalytic reaction mechanism with the attendant revision of the key reaction rate constants from literature values; the determination of the transition temperature of 700 K from the kinetically controlled low-temperature regime to the diffusion-affected high-temperature regime, with the associated global activation energies of 92 ± 1 kJ/mol for the catalytic ignition; and the demonstration that the effective surface area allowing for the porous structure is about 2–3 times larger than the nonporous surface, in agreement with the independently measured value in the literature. Our study on the improved kinetic mechanism further demonstrates the significant effect of surface coverage on the activation energy.

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¹ For interpretation of color in Fig. 9, the reader is referred to the web version of this article.