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# Modelling windwave driven by typhoon Chan-Hom (201509) in the East China Sea



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### h i g h l i g h t s

- Discussed anisotropic energy dissipation in the wave propagation direction.
- The new modified model to simulate and forecast wave evolution caused by Chan-Hom (201509).
- Discussed typical wave parameters near Donghai Bridge.

#### ARTICLE INFO

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## a b s t r a c t

Typhoon-generated waves pose a serious threat to the development of offshore wind power; therefore typical wave parameters caused by typhoon near Donghai Bridge, a demonstration area of offshore wind farm, were analysed. We pay particular attention to the dissipation term which is one of the source terms of governing equation for windwave evolution in WAVEWATCH III. Anisotropic energy dissipation in the wave propagation direction is considered and further applied in our model. A good agreement is observed by comparison with in situ data. Furthermore, the new improved model is used to simulate and forecast wave evolution caused by Chan-Hom (201509). The evolution of typical wave parameters i.e. significant wave height and mean wave period were discussed in the East China Sea, especially near Donghai Bridge.

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Air–sea interaction is one of the important fluid dynamical processes which mediate exchanges of momentum, heat, and gases between atmosphere and ocean [\[1\]](#page-4-0). On the other hand, rouge waves generated by wind have profound implications for the design, placement, and safety of offshore wind power system. Based on these considerations, in this paper, we primarily explore the classical problem of windwave especially for typhoongenerated waves that occur in the East China Sea, where a few marine wind farms are under construction now. The study on the wave spectrum forecast made great progress and developed from the first generation to the third generation. Numerical method and source terms are continuously improved and modified. In these source terms, one of the least known is the dissipation term. Phillips [\[2\]](#page-4-1) thought that in the balance equation, the wind

term, the wave–wave interaction, and the dissipation term are all important. Balanced by wave–wave interactions, the dissipation term is the cube of ''saturation''. Later results showed that the wave breaking has an obvious critical value. Banner et al. [\[3\]](#page-4-2) found that there is a relationship between wave breaking probability and saturation spectrum, and wave breaking happened when saturation level exceeds a certain threshold. Ardhuin et al.  $[4]$ further supposed that energy dissipation caused by wave breaking are in proportion to probability and dimension of the wave breaking, and so energy dissipation by wave breaking is expressed as

<span id="page-0-4"></span>
$$
S_{ds}^{SAT}(k, \theta) = \sigma C_{ds}^{SAT} \left\{ C_{ds, 6} \left[ \max \left\{ \frac{B(k)}{B_{r}P(kD)} - B_{0}, 0 \right\} \right]^{p^{sat}} + (1 - C_{ds, 6}) \right\}
$$

$$
\times \left[ \max \left\{ \frac{B'(k, \theta)}{B_{r}P(kD)} - B_{0}, 0 \right\} \right]^{p^{sat}} \right\} N(k, \theta), \tag{1}
$$

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Letter





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where  $C_{\rm ds}^{\rm SAT}$ ,  $C_{\rm ds,6}$ , and  $p^{\rm sat}$  are empirical parameters;  $B_r$  and  $B_0$  are wave breaking thresholds. In this paper,  $C_{ds}^{SAT} = -2.4 \times 10^{-5}$ ,  $C_{ds,6} = 0.25$ ,  $p^{sat} = 2$ ,  $B_0 = 1.2 \times 10^{-3}$ , and  $B_r = 1.2 \times 10^{-3}$ are taken. Here  $B'(k, \theta)$  is defined as partial integration saturation spectrum in direction, and *B*(*k*) is fully integration saturation spectrum in direction. *P*(*kD*) is maximum wave steepness from deep water to shallow water. However, the spectrum of wave field by Eq.  $(1)$  has narrow ranges [\[5\]](#page-4-4), and this means wave propagation direction is important and needs to be considered [\[6–8\]](#page-4-5). Young and Babanin [\[7\]](#page-4-6) studied energy dissipation caused by wave breaking experimentally and the results showed that in different wave propagation directions, dissipation energy distribution is not usually homogeneous. Considering the factor of inhomogeneous dissipation energy distribution in different directions, Wang [\[9\]](#page-4-7) further compute the wave evolution process under the 0814 hurricane ''Hagupit'' and find that the results of improved model agree well with existing filed observational data.

Total wave energy or wave action is conservation which gives the balance equation for the wave action density spectrum *N* as Eq. [\(2\)](#page-1-0) in the spherical coordinate system.

$$
\frac{\partial N}{\partial t} + \frac{1}{\cos \varphi} \frac{\partial}{\partial \varphi} \dot{\phi} N \cos \theta + \frac{\partial}{\partial \lambda} \dot{\lambda} N + \frac{\partial}{\partial k} \dot{k} N + \frac{\partial}{\partial \theta} \dot{\theta}_{g} N = \frac{S}{\sigma},
$$
  
\n
$$
\dot{\phi} = \frac{c_{g} \cos \theta + U_{\varphi}}{R},
$$
  
\n
$$
\dot{\lambda} = \frac{c_{g} \sin \theta + U_{\lambda}}{R \cos \varphi},
$$
  
\n
$$
\dot{\theta}_{g} = \dot{\theta} - \frac{c_{g} \tan \varphi \cos \theta}{R},
$$
\n(2)

where *R* is the radius of the earth;  $\lambda$  and  $\phi$  are the longitude and latitude, respectively;  $U_{\lambda}$  and  $U_{\varphi}$  are current components;  $\theta$  is the wave travelling direction in the Cartesian definition, and  $\theta = 0$ corresponds to waves travelling from west to east; *k* and *c<sup>g</sup>* are wave number and group velocity, respectively; and  $\sigma$  is the relative frequency observed in a frame of reference moving with the mean current.

The source term *S* at the right hand of the equation consists of four parts, an energy input term *S*in, a nonlinear wave–wave interactions term  $S_{nl}$ , a dissipation term  $S_{ds}$ , and a bottom friction term S<sub>bot</sub>.

$$
S = Sin + Sds + Snl + Sbot.
$$
\n(3)

By analysing the source terms, we primarily focus on the term of *S*ds as it plays a major role in the balance and is not well understood thus far. The dissipation term  $S_{ds}$  in the source terms due to wave breaking are generally considered as a combination of the saturation-based term ( $S_{\rm ds}^{\rm SAT}$ ), the wave–turbulence interaction term (S $_{\rm ds}^{\rm TURB}$ ), and other dissipation terms (S $_{\rm ds}^{\rm OTH}$ ), as follows:

$$
S_{ds} = S_{ds}^{SAT} + S_{ds}^{TURB} + C_{if} \frac{1-S}{2} S_{ds}^{OTH} + C_{hf} \frac{1+S}{2} S_{ds}^{OTH},
$$
(4)

where *S* is the saturation level; *C*<sub>if</sub> and *C*<sub>hf</sub> are switch coefficients of unsaturation and saturation terms, respectively.

The saturation-based term related to the spectral density, breaking probability and breaking severity is parameterized by the saturation spectrum, as shown in Eq.  $(1)$ . In the past, the saturation spectrum is usually assumed independent of wave propagation direction.

$$
B'(k,\theta) = \int_{\theta-\Delta\theta}^{\theta+\Delta\theta} \sigma k^3 N(k,\theta') d\theta'.
$$
 (5)

However, recent research shows that energy dissipation due to wave breaking is anisotropic in the wave propagation direction. Thus we integrate the direction-weighted saturation spectrum

<span id="page-1-3"></span>

**Fig. 1.** History of the significant wave height at station (12.10°E, 34.45°N). The open square is in situ data from Ref. [\[10\]](#page-4-8).

 $B'(f, \theta)$  expressed as Eq. [\(5\)](#page-1-1) into the windwave predicting model expecting to improve its accuracy.

<span id="page-1-2"></span>
$$
B'(f,\theta) = \int_{\theta-\Delta\theta}^{\theta+\Delta\theta} k^3 \cos^p(\theta-\theta') F(f,\theta') \frac{C_g}{2\pi} d\theta',
$$
 (6)

<span id="page-1-0"></span>where  $F(f, \theta')$  is the wave's spectral density over frequencies  $f$ and directions  $\theta$ ';  $p$  was suggested to take 2 which is related to the maximum orbital velocity in direction  $\theta$  for waves with frequencies close to *f* .

Considering the effect of wave direction on energy dissipation caused by wave breaking, in this paper, new definition of saturation spectrum expressed by Eq.  $(6)$  is applied in WAVEWATCH III.

Muifa (201109) is chosen to validate our new model. The target typhoon formed as a tropical depression over the Western Pacific Ocean on July 25, 2011, and then strengthened to a super typhoon by the end of the month. It came to the East China Sea on August 5, and landed North Korea on August 9. Thus, we studied the windwave of the East China Sea in 5 days since August 5. Our results are validated with significant wave heights from three observation stations: (120.10°E, 34.45°N), (126.02°E, 37.23°N), and (125.77°E, 36.25°N), hereinafter referred to as SI, SII and SIII. As an example, the comparisons of significant wave height between in-situ SI data and our model are illustrated in [Fig. 1,](#page-1-3) which shows that the maximum significant wave heights are 2.18 m (in situ) and 2.54 m (our model). Comparing with the in situ data, our result has a sight phase delay. That is caused by the wind data updating delay in our computing, since the wind data we used is the remotely sensed wind field data from NASA's cross-calibrated, multi-platform ocean surface wind velocity project with time resolution six hours. The maximum significant wave heights at SII and SIII are 4.58 m (in situ) and 6.95 m (our results) and 3.86 m (in situ) and 5.97 m (our results), respectively. The deviation between simulation and observations, i.e. the significant wave heights of simulation seem larger than the in situ observation, are in fact in the allowable tolerance. Because mechanisms of wave dissipation in inshore water, where those three observation stations located, are quite complicated due to the nonlinear effect in wave breaking and bottom friction. Moreover, the effects such as reflection, refraction, and wave–current interaction will also become significant in those regions. In addition, wind field and bathymetry data in inshore waters seems somewhat coarser due to land terrain effect and large bathymetry slope.

<span id="page-1-1"></span>Chan-Hom (201509) formed on June 29, 2015 from a westerly wind burst on the Northern Pacific Ocean. It headed northwest and intensified into a typhoon on July 7 before passing between the Japanese islands of Okinawa and Miyako-jima, and it reached the peak winds of 165 km/h two days later. The wind speed of typhoons hit China coast often decayed greatly during their way to China Seas. However, the wind speed of Chan-Hom was still as high as 130 km/h when it struck the coast of Zhejiang on July 11.

<span id="page-2-2"></span>

**Fig. 2.** Wind field caused by Chan-Hom at 08:00:00, July 11.

Then it turned to north crossing the East China Sea and Yellow Sea, and made landfall on the Korean Peninsula on July 13 finally. Since the East China Sea is the region of interest, the geographical area considered in this analysis is formed by a rectangle covering those areas. Its four corners being assigned at the most northerly, the most southerly, the westernmost, and the most easterly points are: 38.00°N, 22.00°N, 115.00°E, and 130.00°E. Based on the track, our analysis period lasts from 02:00:00 of July 8 to 22:00:00 of July 12.

The Bathymetry data is retrieved from the National Centers for Environment Information, which belongs to National Oceanic and Atmospheric Administration. In this analysis, ETOP01, a 1 arcminute global relief model of Earth's surface, was utilized.

The wind field caused by Chan-Hom was reconstructed based on the tropical cyclone model  $[11,12]$  $[11,12]$ . In the tropical cyclone model we used, wind field *v* is decomposed into three components: tangential wind speed  $v<sub>T</sub>$ , radial wind speed  $v<sub>R</sub>$ , and environmental scale wind velocity  $v<sub>E</sub>$  as expressed by Eq. [\(7\).](#page-2-0)

$$
\mathbf{v} = \mathbf{v}_{\mathrm{T}} + \mathbf{v}_{\mathrm{R}} + \mathbf{v}_{\mathrm{E}}.\tag{7}
$$

We here only present the final expressions of those three components, for the details one may refer to Ref. [\[12\]](#page-4-10).  $v_T$ ,  $v_R$ , and  $v<sub>E</sub>$  are given as Eqs. [\(8\)–\(10\)](#page-2-1) with vector marks omitted for convenience.

$$
v_{\rm T}/V_{\rm m} = \sqrt{R^{-B}\exp\left(1 - R^{-B}\right) + a^2R^2} - aR,\tag{8}
$$

$$
v_{R} = \frac{B[BR^{-2B} + (1 - 3B)R^{-B} + B - 1]k - 2k - RC}{B(R^{-B} - 1) + 2 + 4aR(v_{T}/V_{m})^{-1}} \cdot v_{T},
$$
(9)

$$
v_{\rm E} = U_0 \exp\left(-\frac{r}{R_{\rm G}}\right),\tag{10}
$$

where  $V_m$  is the maximal wind velocity,  $U_0$  is the translation velocity of the cyclone.  $R_G$  is the length scale of the environmental scale processes of order of 500 km, *r* is the distance form tropical cyclone centre. *R* is  $r/R<sub>M</sub>$ , where  $R<sub>M</sub>$  is the radius to maximum wind speed. As for the coefficients *B*, *C* and *k*, we took the typical values  $B = 1.5$ ,  $C = 0.013$ , and  $k = 0.16$  as suggested by Jakobsen and Madsen [\[12\]](#page-4-10). *a* equals to  $fR_M/(2V_m)$ , where *f* is the Coriolis parameter related to latitude.

Using the aforementioned tropical cyclone model, wind field can be obtained once the maximal wind velocity and location of tropical cyclone centre are given. In this analysis, the maximal wind velocity and location were retrieved from the joint typhoon warning center (JTWC), a joint United States Navy. Its time resolution is 6 h during the life cycle time of Chan-Hom. As a demonstration, the wind field at 08:00:00 July 11 is presented

<span id="page-2-3"></span>

**Fig. 3.** Maximal significant wave heights at observation stations in Chan-Hom life cycle. S1–S15 are the observation stations located along China coast from the Taiwan Strait to the Shandong Peninsula.

<span id="page-2-4"></span>

**Fig. 4.** History of significant wave heights at S5 to S9. The observation stations S5 to S9 are Zhoushan, Daishan, Chengshan, Dajishan, and Sheshan, respectively. The horizontal and vertical axes are time from 24:00:00 July 9 to 00:00:00 July 13 and significant wave height, respectively.

<span id="page-2-0"></span>as [Fig. 2.](#page-2-2) From which, the eye of Chan-Hom and the asymmetric wind vectors due to translation heading northwest are quite straightforward.

<span id="page-2-1"></span>The maximal significant wave heights of fifteen stations along China coast from the Taiwan Strait to the Shandong Peninsula were observed. The observation stations are Pingtan (120.190°E, 25.49°N), Beishuang (120.830°E, 26.71°N), Nanlu (121.580°E, 27.46°N), Dachen (122.500°E, 28.46°N), Zhoushan (123.040°E, 29.87°N), Daishan (123.000°E, 30.27°N), Chengshan (123.460°E, 30.73°N), Dajishan (122.950°E, 30.83°N), Sheshan (122.810°E, 31.52°N), Waikejiao (122.180°E, 33.02°N), Binhai (120.780°E, 34.28°N), Lianyungang (119.860°E, 34.79°N), Qianliyan (121.960°E, 36.25°N), Chengshantou (123.36°E, 37.38°N), Penglai (121.20°E, 37.86°N), which are referred to as S1–S15, respectively, hereinafter.

As shown in [Fig. 3,](#page-2-3) the maximal significant wave heights of S1–S3 (at nearshore of provinces Fujian and southern Zhejiang) and S11–S15 (at nearshore of provinces Shandong and Jiangsu) are all below 6 m, since those stations are a little bit far away from the typhoon track. While the maximal significant wave heights of S6–S9, i.e. Daishan station, Chengshan station, Dajishan station and Sheshan station, are all above 9 m, in which S9 reaches 16.06 m. Those stations sit at the nearshore of Shanghai and northern Zhejiang, just on the track (see  $Fig. 5$ ). Besides, the wind speed is still as high as 130 km/h when Chan-Hom passing this region.

To be more specific, the histories of significant wave height of S5–S9 are presented as shown in [Fig. 4.](#page-2-4) Significant wave heights

<span id="page-3-0"></span>

Fig. 5. Distribution and evolution of significant wave heights. Subfigure (a)–(f) are for different moments: (a) 18:00 July 8, (b) 06:00 July 9, (c) 18:00 July 9, (d) 06:00 July 9, (d) 06:00 July 9, (d) 06:00 July 9, (d) 0 10, (e) 06:00 July 11, (f) 06:00 July 12. The solid line is track of Chan-Hom.

rise sharply at morning of July 10 and decay at July 12, it is coincident with the arriving and leaving time of Chan-Hom for those stations. Histories of significant wave height in [Fig. 4](#page-2-4) are not single peak curves, i.e. two peaks exist for each curve roughly. The ''two peaks'' phenomenon can be explained as: the maximum wind speed radius, the eye and the maximum wind speed radius will pass those stations in sequence because they are just on the track of the eye.

In addition, the distribution/evolution of significant wave heights (see [Fig. 5\)](#page-3-0) and mean wave periods (see [Fig. 6\)](#page-4-11) are presented. [Figure 5](#page-3-0) shows that the maximum significant wave height moves forward along the typhoon track. The shape of area with large significant wave height, say significant wave height above 8 m, seems more slender comparing with the elliptic wind field. This tailing effect is due to wave dissipation is much gentler comparing with the sharp growth by the strong driven wind

because of lack of intense dissipation force. From Fig.  $5(d)$  and (e), we can say significant wave height is strongly affected by bathymetry through wave breaking and bottom friction. As for the mean wave period (see Fig.  $6(d)$  and (e)), short mean wave period  $(<10 s)$  is in the high wind speed area where wave in the growth stage. While the mean wave period of mature wave in Yellow Sea is about 20 s (see Fig.  $6(e)$ ). When the maximum wind speed decreased to 90 km/h on 06:00 July 12 as shown in Fig.  $6(f)$ , mean wave periods are all below 15 s.

In this paper, we preliminarily examine the wind generated waves in the East China Sea using a theoretical model which considers the directional behaviours of the spectral dissipation. In comparison of numerical simulation with in situ data, basically, the model is shown to be reasonable. In the future, more in situ data is desired to further validate the model. In addition, the influences of other source terms are planned to be explored in more detail.

<span id="page-4-11"></span>

**Fig. 6.** Distribution and evolution of mean wave period. Subfigure (a)-(f) are for different moments: (a) 18:00 July 8, (b) 06:00 July 9, (c) 18:00 July 9, (d) 06:00 July 10, (e) 06:00 July 11, (f) 06:00 July 12. The solid line is track of Chan-Hom.

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