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# Efficient propulsion and hovering of bubble-driven hollow micromotors underneath an air-liquid interface

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## ABSTRACT

Bubble-driven micromotors have attracted substantial interest due to their remarkable self-motile and cargo-delivering abilities in biomedical or environmental applications. Here, we developed a hollow micromotor that experiences fast self-propulsion underneath an air-liquid interface by periodic bubble growth and collapse. The collapsing of a single microbubble induces an  $\sim 1 \text{ m}\cdot\text{s}^{-1}$  impulsive jetting flow that instantaneously pushes the micromotor forward. Unlike previously reported micromotors propelled by the recoiling of bubbles, cavitation-induced jetting further utilizes the energy stored in the bubble to propel the micromotor, and thus enhances the energy conversion efficiency by three orders of magnitude. Four different modes of propulsion are, for the first time, identified by quantifying the dependence of propulsion strength on microbubble size. Meanwhile, the vertical component of the jetting flow counteracts the buoyancy of the micromotor-bubble dimer and facilitates counterintuitive hovering underneath the air-liquid interface. This work not only enriches the understanding of the propulsion mechanism of bubble-driven micromotors but also gives insight into the physical aspects of cavitation bubble dynamics near the air-liquid interface on the microscale.

## INTRODUCTION

The autonomous motion of artificial micromotors has attracted great attention over the past decades owing to their potential applications in biomedical<sup>1-6</sup> and environmental areas.<sup>7, 8</sup> Among existing micromotors, one main category is catalytic micromotors that convert chemical energy into mechanical motion based on the local chemical reaction at the surface, such as the bimetallic nanorods<sup>9, 10</sup> and insulator-catalyst Janus microspheres.<sup>11, 12</sup> One main challenge of designing high-efficiency micromotors is to overcome the restrictions inherent to propulsion in a viscous flow with a low Reynolds number ( $Re = uL/\nu$ , where  $u$ ,  $L$  and  $\nu$  are the typical velocity, typical flow dimension and kinetic viscosity of the fluid, respectively).

For a small platinum-silica (Pt-SiO<sub>2</sub>) Janus micromotor (JM) with a size of  $\sim 1$   $\mu\text{m}$ , phoretic propulsion emerges when the JM is immersed in a H<sub>2</sub>O<sub>2</sub> solution to create a nonuniform concentration field as a result of the decomposition of H<sub>2</sub>O<sub>2</sub> on the Pt side.<sup>11, 13, 14</sup> However, the speed and propulsion efficiency are sometimes too low for engineering applications.<sup>15</sup> As first reported for tubular micromotors,<sup>16, 17</sup> bubble propulsion achieves the highest speed among all kinds of micromotors.<sup>15, 18</sup> In a system similar to the aforementioned Pt-SiO<sub>2</sub> JM but with a larger size ( $\sim 10$   $\mu\text{m}$ ), microbubbles can nucleate and grow near the Pt surface. The periodic emergence of the bubbles and the interaction between the bubbles and the JM enable symmetry-breaking in microscale viscous flows with a low Re number and induce fast motion of the JM.<sup>19, 20</sup>

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4 In contrast to previous studies that only focused on the direct momentum  
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6 exchange between a JM and microbubbles during bubble growth and recoiling  
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8 stages,<sup>21-25</sup> the hydrodynamic effect during the bubble collapse stage should be given  
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10 more attention when considering the dramatic variation of the flow field in a short  
11  
12 time. So far, a detailed propulsion mechanism for the different stages of the entire  
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14 lifetime of a bubble is still lacking. For example, a good understanding of the  
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16 hydrodynamic effect during the bubble collapse stage is desired. Without this effect,  
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18 the negative pullback of a JM after bubble collapse cannot be well explained.<sup>21</sup>  
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20 Furthermore, the rich and interesting physics of microscopic bubble dynamics needs  
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22 to be clarified, such as bubble growth behavior<sup>26</sup> and bubble collapse dynamics.<sup>27-29</sup> In  
23  
24 particular, the presence of boundaries, such as an air-liquid interface, significantly  
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26 influences the bubble collapse process;<sup>30-33</sup> however, their impact on JM propulsion  
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28 has not been experimentally investigated.  
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35 In this work, we study the self-propulsion of hollow Pt-SiO<sub>2</sub> Janus micromotors  
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37 moving just underneath an air-liquid interface. These hollow Janus micromotors  
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39 (hJMs) are made of cenospheres, which are byproducts of coal powder combustion  
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41 and have a hollow structure with a density of approximately 400 kg·m<sup>-3</sup> and a  
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43 diameter of about tens of microns. In the horizontal direction, owing to the subtle  
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45 interactions between the microbubble and the hJM, an instantaneous speed of ~1 m·s<sup>-1</sup>  
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47 for the impulsive jetting flow is generated after bubble collapse. The energy stored by  
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49 the bubble is focused by cavitation-induced jetting to propel the hJM, thus increasing  
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51 the energy conversion efficiency by three orders of magnitude. In the perpendicular  
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3 direction, the buoyancy of the bubble-hJM aggregate is counteracted by the vertical  
4 component of the jetting from the collapse of the microbubble. As a result, the hJM  
5 hovers up and down underneath the air-liquid interface. The complete mechanism is  
6 illustrated by flow visualization via particle tracking velocimetry (PTV) and  
7 computational fluid dynamic (CFD) simulations. The significant influence of the  
8 interface near the micromotor is verified by control experiments using solid Janus  
9 micromotors (sJMs) near a solid-liquid interface. The present bubble self-propulsion  
10 system is vividly described as an artificial ‘microcatapult’, analogous to the  
11 ‘cavitation catapult’ in nature;<sup>34</sup> the elastic launching of the payload is replaced by the  
12 dynamics of a single confined cavitation microbubble.  
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## 29 **EXPERIMENTAL SECTION**

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32 **Preparation of the hJMs.** The cenospheres, which were made of silica, were  
33 purchased from Sino-steel Co. Ltd. The diameter of the cenospheres is approximately  
34 20–50  $\mu\text{m}$ . The Pt-SiO<sub>2</sub>-type hJM was made by coating a layer of Pt onto one of the  
35 two hemispheres of a cenosphere. A droplet of the cenosphere solution was placed on  
36 a silicon wafer mounted on a spin coater. A rotating speed of 200 rpm was applied to  
37 spread the cenospheres uniformly on the wafer. After heat-drying, a monolayer of  
38 cenospheres was formed on the wafer. Then, an approximately 20-nm-thick Pt layer  
39 was evaporated using an Innotec E-beam evaporator. Due to the compact arrangement  
40 of the cenospheres, the Pt layer only covered the top half of the cenospheres, forming  
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3 a double-faced Janus particle. Ultrasonic treatment was applied to keep the  
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5 monodispersity of the hJMs prior to each experiment.  
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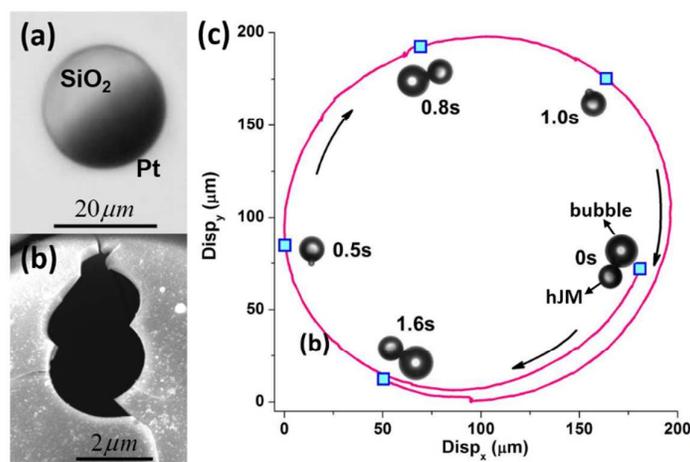
8 **Self-propulsion of the hJMs.** In the experiment, a droplet (70  $\mu\text{L}$ ) containing  
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10 hJMs diluted in an  $\text{H}_2\text{O}_2$  solution (2–5 vol %) was placed on a hydrophilic glass slide.  
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12 The thickness of the sample solution was approximately 0.5–1 mm. The motions of  
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14 the hJMs were observed with an inverted microscope (Nikon Eclipse Ti-U, with 20 $\times$   
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16 or 40 $\times$  objectives). A high-speed video camera (Phantom v7.3) was used to record the  
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18 hJM motion and microbubble growth with frame rates of up to 85,000 fps. We  
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20 obtained the positions of the hJMs and bubbles in each image by using the particle  
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22 tracking method and further calculated their trajectories, bubble diameters, and bubble  
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24 growth rate.<sup>12</sup> Polystyrene (PS) microspheres (diameter, 2  $\mu\text{m}$ ) were used as tracers to  
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26 visualize the flow field of the strong, instantaneous jetting.  
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## 33 34 **RESULTS AND DISCUSSION**

### 35 36 37 **Horizontal locomotion**

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40 Images of an hJM with a hemispherical coating of platinum and its inner hollow  
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42 structure are shown in Figure 1a. In pure water, hJMs automatically float up toward  
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44 the air-liquid interface owing to their lower apparent density. However, when hJMs  
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46 are dispersed into a fuel solution, e.g.,  $\text{H}_2\text{O}_2$ , their self-propelled movement occurs.  
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48 The typical trajectory of an hJM (diameter  $2R_{\text{hJM}} = 19.9 \mu\text{m}$ ;  $\text{H}_2\text{O}_2$  concentration, 3%)  
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50 according to the experimental video (video S1 in Supporting Information) is  
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52 illustrated in Figure 1c. During a series of growth-collapse cycles of microbubbles,  
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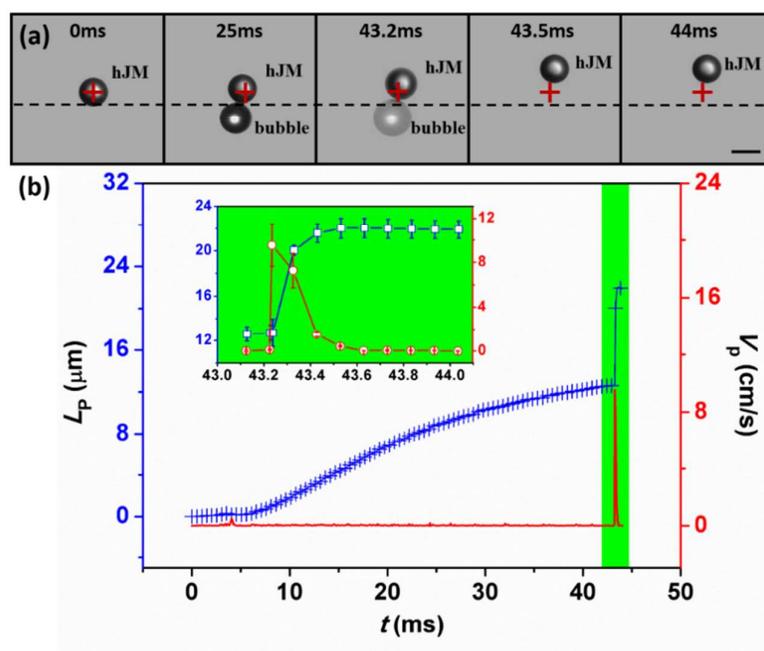
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3 the hJM exhibits an approximately circular motion. The average speed of the hJM was  
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5 calculated to be approximately  $500 \mu\text{m}\cdot\text{s}^{-1}$ , which corresponds to a speed-body length  
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7 (S-BL) ratio of 25.  
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27 **Figure 1.** (a) A microscopy image of an hJM. (b) An SEM image of the broken shell  
28 of an hJM (in the experiments, only perfect hJMs were used). (c) The typical circular  
29 trajectory of a self-propelled hJM lasting 1.6 s.  
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35 The details of the hJM movement during a single cycle are shown in Figure 2a and  
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37 2b. The period from bubble formation to collapse lasts approximately 44 ms.  
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39 According to the hJM displacement ( $L_p$ ) vs. time ( $t$ ) data (blue curve in Figure 2b),  
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41 hJM motion is composed of three stages. In the first stage (0–8 ms), no bubble can be  
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43 observed, and hJM displacement is approximately zero. This indicates that the period  
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45 of restoration of the flow field is disrupted by a previous bubble. In the second stage  
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47 (8–43.2 ms), a bubble appears and grows on the Pt hemisphere. This propels the hJM  
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49 at an average speed of  $V_p = 310 \pm 10 \mu\text{m}\cdot\text{s}^{-1}$ , which corresponds to an S-BL ratio of  
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51 15.5. The hJM locomotion in this stage is driven by diffusiophoretic forces and  
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4 bubble growth, as mentioned in previous works<sup>11,21</sup>. In the last stage (43.2–44 ms),  
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6 the hJM exhibits a large instantaneous speed, following the microbubble collapse at  
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8 approximately 43.2 ms. The maximum propulsion speed,  $V_p$  (red curves in Figure 2b),  
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10 at this stage can reach up to  $\sim 10 \text{ cm}\cdot\text{s}^{-1}$ , which corresponds to a large S-BL ratio of  
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12 5000. Afterwards, the hJM decelerates in approximately 1 ms by the viscous drag  
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14 force. These growth-collapse cycles can be repeated continuously to propel the hJM  
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16 motion. The resultant Re numbers of the three stages in one cycle are  $\sim 0$ ,  $\sim 10^{-2}$  and  
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18  $\sim 10$ , respectively, indicating a span of more than three orders of magnitude.  
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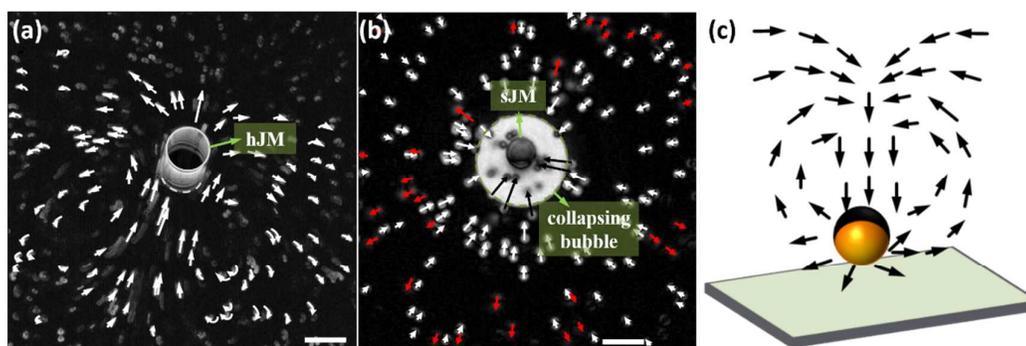
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46 **Figure 2.** Experimental snapshots (a) and typical time-varied behavior in one single  
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48 cycle (b). (a) The red cross denotes the initial position of a hJM. Scale bar, 20  $\mu\text{m}$ . (b)  
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50 The instantaneous displacement,  $L_p$  (blue curve with crosses), and speed,  $V_p$  (red  
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52 curve), of hJM as a function of time,  $t$ , for a period of 44 ms. Inset: the data on hJM  
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54 movement during bubble collapse (in the green region). The error bars for  
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3 displacement and speed are calculated based on standard deviations from n=8 cycles.  
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6 To clarify this confinement effect, a control experiment using sJMs located near a  
7 solid-liquid interface was performed and compared with the experimental results of  
8 the hJMs. Flow visualization experiments using polystyrene (PS) tracers for both  
9 hJMs and sJMs were carried out to capture the distinctive behavior of instantaneous  
10 flow during bubble collapse. Figure 3a illustrates the flow field around an hJM  
11 (created from a series of 30 consecutive images based on a video recorded at 9900 fps;  
12 see video S2 in Supporting Information). This clearly shows that a strong jetting flow  
13 was propelling the hJM forward immediately after the collapse of the bubble. A pair  
14 of vortices was observed in the wake region of the hJM, and the diameter of the jet  
15 core (the distance between the two vortices) was approximately 40  $\mu\text{m}$ . This jet flow  
16 transfers the energy from the collapsing bubble into the propulsion of the hJM. The  
17 maximum speed of the core jet flow shown by the tracers was approximately 1  $\text{m}\cdot\text{s}^{-1}$ ,  
18 i.e., 10 times larger than that of the hJM. Based on Kelvin's impulse theorem, which  
19 states that  $Ft = \Delta(m_p V_p)$ ,<sup>29</sup> the maximum speed of the hJM can be estimated using the  
20 equation,  $V_p = 3Ft/4\pi\rho_p R_p^3$ . Since surface tension dominates bubble collapse, the  
21 equations of force and time should be  $F \sim \pi R_b \sigma$  and  $t \sim (\rho_{\text{water}} R_b^3 / \sigma)^{0.5}$ , respectively.  
22  
23 Considering that the sizes of the bubbles and the hJM are on the same order of  
24 magnitude, the resultant value of  $V_p \sim (\sigma \rho_{\text{water}} / \rho_p^2 R_p)^{0.5}$  is approximately 0.1–1  $\text{m}\cdot\text{s}^{-1}$ ,  
25 which is consistent with our experimental result. Such speed will exert an effective  
26 impulse of  $I \sim 10^{-13}$  N·s. To the best of our knowledge, this is the first study to  
27 directly identify microcavitation-induced jetting and its significant hydrodynamic  
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3 effect on bubble propulsion, which unveils a new mechanism different from that of  
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5 microbubble recoiling or microbubble-JM interactions proposed in recent works.<sup>21, 23,</sup>  
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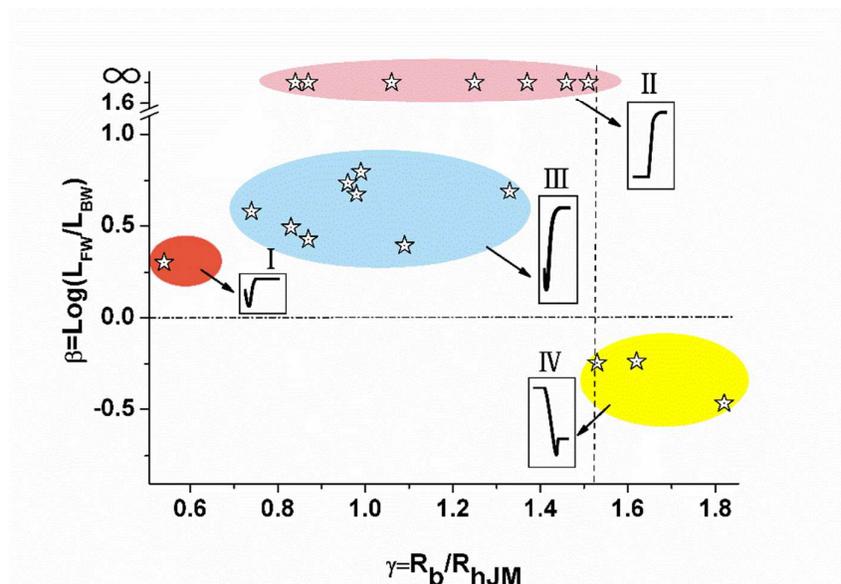
10  
11 Similar to the measured flow field of an hJM underneath the air-liquid interface  
12 shown in Figure 3a, Figure 3b shows the flow field around a sJM near the solid-liquid  
13 interface. Generally, the size of the bubbles generated in this case was much larger  
14 than that in the experiment using hJMs, and the bubbles were located on top of the  
15 sJM because of the buoyant force. The experimental videos showed that the sJM  
16 moved much slower ( $20\text{--}50\ \mu\text{m}\cdot\text{s}^{-1}$ ) during bubble formation and exhibited a clear  
17 backward displacement during bubble collapse (videos S3 and S4 in Supporting  
18 Information). At the horizontal focus plane across the bubble center, no liquid jetting  
19 was observed from the top view, and the flow direction pointed to the bubble center  
20 (white arrows in Figure 3b). At the plane between the sJM and the solid wall, the flow  
21 was found to be directed from the center to the outer region (red arrows in Figure 3b).  
22 The focus plane of the camera for Figure 3b was located near the bubble center, and  
23 so the tracers, indicated by the white arrows, were clearer and brighter than those  
24 shown by the red arrows. Based on the above information, we proposed a model, as  
25 shown in Figure 3c, to illustrate the vertical flow field around a sJM after bubble  
26 collapse. As a result, this flow field cannot propel the sJM significantly in the  
27 horizontal plane, and the efficiency of the propulsion is much lower due to the  
28 hindering effect of the wall.  
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**Figure 3.** Images of the flow field during bubble collapse around (a) an hJM underneath the air-liquid interface and (b) a sJM near a solid wall. The white arrows represent the velocity vectors based on the motions of the tracers in the objective focus plane, and in (b) the red arrows represent the motions of the out-of-focus plane tracers. (c) A schematic diagram showing the vertical flow field around a sJM near a solid wall. Scale bar, 20  $\mu\text{m}$ .

To better understand the locomotion of the microbubble, we further evaluated the propulsion performance based on the normalized microbubble size,  $\gamma = R_b/R_p$  (Figure 4). There is a dependence of the propulsion styles quantified by the forward-to-backward index,  $\beta$ , on  $\gamma$ .  $\beta = \log(L_{FW}/L_{BW})$  is defined as the logarithm of the ratio between the forward displacement ( $L_{FW}$ ) by jetting and the backward displacement ( $L_{BW}$ ) by the collapse of the bubble. Four different modes characterized by the hJM displacement styles were observed (see the four insets in Figure 4 and video S5 in Supporting Information). For small  $\gamma$  ( $\gamma < 0.7$ ), the mode of ‘moderate propulsion’ was seen after a clear back-pull (symbol I), quantified by  $0 < \beta \ll 1$ . In this mode, energy from the collapsing bubble was too weak to propel the hJM forward significantly. For intermediate values of  $\gamma$  ( $0.7 < \gamma < 1.5$ ), two possible modes could

occur: one is ‘perfect propulsion’ with no backward displacement (symbol II,  $\beta \rightarrow \infty$ ; also the case shown in Figure 2); the other is ‘strong propulsion’ with a small withdrawal (symbol III,  $\beta = 0.5-1$ ). When  $\gamma > 1.5$ , it is surprising to observe that there is a sudden transition from the perfect propulsion mode ( $\beta \rightarrow \infty$ ) to the opposite mode with a strong backward displacement (symbol IV,  $\beta < 0$ ). In this case, the size of the bubble was so large that the confinement effect of the hJM was negligible, and the homogeneous shrinkage of the bubble predominated. As a result, the quasi-oscillatory motion proposed by Manjare et al.<sup>2020</sup> will cause the clear backward motion of the hJM. We emphasize that the competition between the hydrodynamic jet flow and the quasi-oscillatory motion after bubble collapse will determine the propulsion mode. Without the contribution of the hydrodynamic jet flow, the previous theories cannot well explain the instantaneous strong forward propulsion. Therefore, an intermediate microbubble size ( $0.7 < \gamma < 1.5$ ) is crucial for generating a stronger forward propulsion by liquid jetting during collapse.



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4 **Figure 4.** Different propulsion modes shown by the forward-to-backward index  $\beta$   
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6 versus the dimensionless microbubble size  $\gamma = R_b/R_{hJM}$ . The four insets show the  
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8 typical displacement patterns occurring in the propulsion stage (corresponding to the  
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10 pattern of displacement after microbubble collapse shown in the green region of  
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12 Figure 2).  
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### 18 **Vertical hovering**

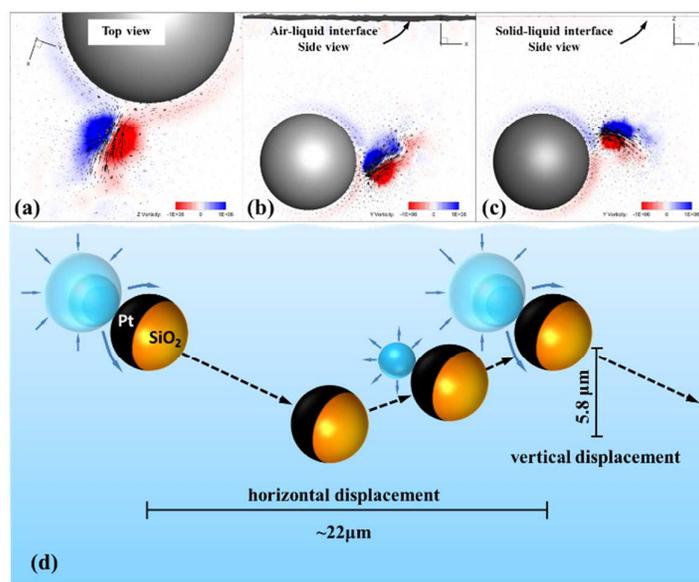
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21 It would be interesting to examine whether the hJM continues swimming in the  
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23 water or floating at the air-liquid interface. Some of the information on the vertical  
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25 movement of the hJM can be obtained based on microscopic observations. We were  
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27 able to locate the objective focus plane at the air-liquid interface by the highest  
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29 position where the suspended PS tracers could still be clearly observed. Then, by  
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31 adjusting the focus plane downwards, the hJM was estimated to be approximately 20–  
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33 40  $\mu\text{m}$  underneath the air-liquid interface. We could also exclude the possibility that  
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35 the hJM was accidentally trapped at the air-water interface and the significant  
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37 contribution of the interfacial tension. If this situation occurred, the collapsing bubble  
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39 would merge with air, inducing a vertical jet flow instead of a horizontal one, which  
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41 was not observed in the experiment.  
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48 Another interesting question is how an hJM with a density smaller than water could  
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50 overcome buoyancy and maintain its position underneath the air-liquid interface. The  
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52 reason is attributed to the three-dimensional flow occurring in both the horizontal and  
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54 vertical directions. In the vertical direction, because the constraint from the free  
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3 surface (air-liquid interface) was weaker than that from the bulk liquid phase, the  
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5 direction of the jet flow was towards the bulk liquid phase, which provides a  
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7 mechanism to overcome the buoyancy. The strength of the vertical flow depends on  
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9 the stand-off distance between the bubble and the air-liquid interface. The more  
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11 closely the bubble approaches the interface, the stronger the jet flow is. Therefore, the  
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13 hJM should periodically dive and float with the same small fluctuation in distance  
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15 around a balance position due to the dynamic competition between the jet flow and  
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17 the buoyancy. We refer to this adaptive vertical motion as ‘dynamic hovering’.<sup>36</sup>  
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19 Although it is difficult to experimentally obtain the real-time vertical position of the  
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21 hJM due to the ultrafast collapse process, the fluctuation distance can be evaluated to  
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23 be approximately 5.8  $\mu\text{m}$  (see SI1 in Supporting Information) in terms of the balance  
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25 between the buoyancy of the bubble-hJM aggregate and the Stokes drag force in the  
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27 floating stage.  
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36 CFD simulations were performed to characterize the flow field during bubble  
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38 collapse around a hJM (see SI2 and video S6 in Supporting Information). In the CFD  
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40 bubble collapse simulation, the hJM was placed at the center of a cubic flow domain  
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42  $[(40R_p)^3]$ , and the gap between the interface (air-liquid or solid-liquid) and the hJM  
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44 was  $2R_p$ . The finite volume method was used for numerical discretization, and the  
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46 volume of fluid method was utilized for multiphase modeling (see SI2 in the  
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48 Supporting Information). The time interval was set as  $10^{-9}$  s in order to capture  
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50 instantaneous information on the bubble collapse in the experiment. The simulation  
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52 results from the top view (Figure 5a) are in good agreement with the experimental  
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4 flow field shown in Figure 3a. For the side view, a jet flow pointing to the lower part  
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6 of the hJM is clearly shown in Figure 5b. This flow, pushing the hJM downwards,  
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8 resulted in the vertical dynamic hovering mentioned above, as illustrated in Figure 5d.  
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11 In contrast, the simulation results in Figure 5c show that when the air-liquid interface  
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13 is replaced by a solid-liquid interface, the jet flow pointed to the upper part of the hJM,  
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15 which exhibits a totally different behavior due to the confinement effect. This result  
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17 indicates that the flexible air-liquid interface makes a key contribution to the dynamic  
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19 hovering of the hJM.  
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41 **Figure 5.** The CFD results of the flow field around a hollow hJM near an air-liquid  
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43 interface from the (a) top view and (b) side view. (c) The distinct flow field near the  
44  
45 liquid-solid interface. The arrow represents velocity, and the color represents vorticity.  
46  
47 (d) A schematic drawing to show the dynamic hovering of an hJM near an air-liquid  
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49 interface.  
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54 Previous theoretical studies have usually focused on how the curved profile of the  
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56 air-liquid interface influences the balanced position of a spherical micromotor  
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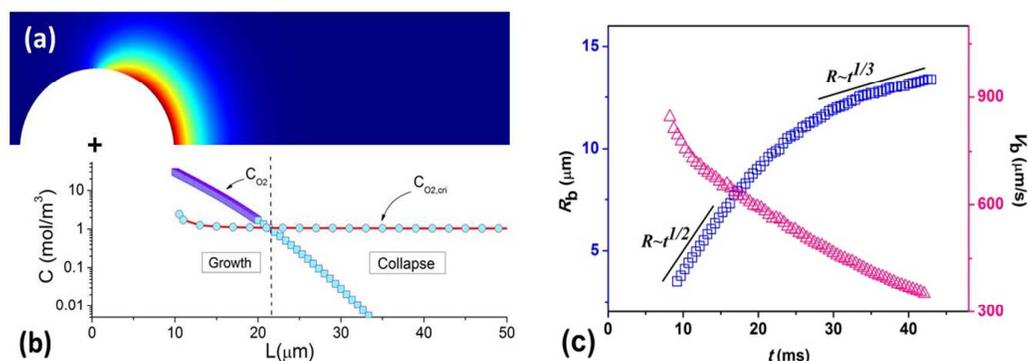
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3 underneath the air-water interface.<sup>37</sup> The dynamic hovering described in the present  
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5 work based on nonreciprocal vertical flow with a Re number ranging from ~0 to ~10  
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7 offers a novel mechanism. From our dynamic simulation, if the processes of both  
8  
9 bubble growth and collapse are in the low Re regime, the net displacement of the hJM  
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11 contributed by the cyclic bubbles must be zero. Then, buoyancy will always drive the  
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13 hJM upwards. Breaking down the vertical flow reciprocity is the key to generating the  
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15 dynamic hovering behavior that prevents lightweight underwater micromotors from  
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17 floating.  
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### 23 **Bubble Instability**

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26 Considering the importance of bubble size on propulsion efficiency (shown in  
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28 Figure 4), we put forward a simplified model to explain the critical bubble size based  
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30 on bubble instability. Assuming a quasi-steady state and a far-field reference pressure,  
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32  $p_{ref}$ , the internal pressure,  $p_b$ , of a bubble with radius  $R_b$  can be given by  $p_{ref} + \sigma/R_b$ ,  
33  
34 where  $\sigma$  is surface tension. With the presence of  $H_2O_2$  in the solution, an  $O_2$  bubble  
35  
36 can be generated by the surface catalytic reaction,  $2H_2O_2 \rightarrow 2H_2O + O_2$ , and  $p_b$  is also  
37  
38 the partial pressure of  $O_2$ . According to Henry's law, the required average mole  
39  
40 concentration of dissolved  $O_2$  around the bubble is  $C_{O_2, cri} = C_{H_2O}(p_{ref} + \sigma/R_b)/H$  (blue  
41  
42 circles in Figure 6b), where  $H = 4.4 \times 10^9$  Pa is the Henry coefficient for  $O_2$  and  $C_{H_2O} =$   
43  
44  $5.6 \times 10^4$  mol·m<sup>-3</sup> is the mole concentration of water.<sup>26</sup> Figure 6a shows the practical  
45  
46 distribution of the concentration of dissolved oxygen,  $C_{O_2}$ , for the typical  
47  
48 experimental  $H_2O_2$  concentration of 3% (vol/vol), based on the numerical model (see  
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50 SI3 in Supporting Information). A sharp concentration gradient appears at the  
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4 downstream side, as indicated by the purple squares along the downstream axis in  
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6 Figure 6b. The converging of  $C_{O_2}$  to  $C_{O_2,cri}$  explains how mass transfer influences  
7  
8 bubble growth. In the region of  $C_{O_2} > C_{O_2,cri}$ , the continuous growth of the bubble is  
9  
10 supported by the sufficient background oxygen concentration. The larger  
11  
12 concentration difference near the hJM leads to rapid growth. When the bubble size  
13  
14 approaches the intersection point, the microbubble reaches its maximum radius. In the  
15  
16 region of  $C_{O_2} < C_{O_2,cri}$ , the bubble ceases growing because of a limited supply of  $O_2$ .  
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18 Once a small disturbance makes the bubble drift from this critical position, cavitation  
19  
20 instability will be triggered, and the bubble begins to collapse. The experimental  
21  
22 tendency of bubble growth is shown in Figure 6c. The maximum  $R_b$  observed in the  
23  
24 experiment is approximately 13.5  $\mu\text{m}$ . This is consistent with the prediction based on  
25  
26 the intersection point, which indicates that the maximum bubble size is  $2R_b \approx 25 \mu\text{m}$ .  
27  
28 In particular, two accurate exponential scaling laws of  $R_b$  during microbubble growth,  
29  
30  $R_b \sim t^{1/2}$  and  $R_b \sim t^{1/3}$ , are observed. The dependency can be depicted by the  
31  
32 Rayleigh-Plesset equation (see SI4 in Supporting Information) when either the surface  
33  
34 tension or the ambient fluid pressure predominates. It is interesting to see that the  
35  
36 Rayleigh-Plesset equation is still valid even considering the oxygen generation and  
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38 dissolving. Also, ideally the derivation of the Rayleigh-Plesset equation requires the  
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40 liquid around the microbubble should be infinite. However, even though the air-liquid  
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42 interface is only about 20 – 50  $\mu\text{m}$  above the bubble, we did not observe any  
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44 noticeable influence from the air-liquid interface on the bubble dynamics. The  
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46 gradually decreased growth rate indicated by the exponents of the above scaling laws  
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is due to the decrease in the background oxygen concentration as the bubble grows. The complete bubble dynamics can be easily understood based on this theoretical framework.



**Figure 6.** (a) The concentration field of dissolved O<sub>2</sub> around an hJM and (b) the distribution along the downstream axis. (c) The experimental data of bubble growth.

### Analogy of a catapult

We demonstrate the observed instantaneous propulsion of the hJM as a microcavitation catapult by means of an analogy. In contrast to all other artificial catapults that use a crossbar to guide their movement direction, the present hJM, as the simplest microcatapult, has no such crossbar structure. However, a function similar to the crossbar is fully realized via dynamic interactions between the fluid and hJM through the bubble cavitation-collapse processes. Unlike the bubble collapse in an infinite flow field, when the bubble is confined in the vicinity of a boundary,<sup>30-32</sup> the rigid wall restricts the flow of the fluid to produce a jet flow towards the wall, while the flexible air-liquid interface promotes the flow to produce the jet flow away from the interface. We show that much of the sophistication here relies on the compact boundary combination between the air-liquid interface and the suspended

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3 hJM, where both boundaries guide the flow to a unique direction and the energy of the  
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6 collapsing bubble is focused to propel the hJM rather than being dissipated and  
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8 dispersed to the surrounding liquid.  
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11 The entire process of the cavitation catapult includes the power source of the  
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13 catapult (surface catalytic reaction), energy storage (bubble growth), triggering  
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15 mechanism (instability) and launching of the hJM (confinement-induced jetting flow).  
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17 Qualitative nonreciprocal flow is responsible for the initiation of this process.  
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19 However, a thorough understanding requires the full details of the lifetime of bubble  
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21 dynamics and the bubble-hJM interaction. Further work will be devoted to the  
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23 construction of an integral multi-timescale model.  
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28 It is interesting to compare the hJM catapult with natural and artificial counterparts.  
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30 Sakes et al. have shown that the launching acceleration ranges from 6.6 g to  
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32 approximately one million g based on the shooting mechanism in nature.<sup>38</sup> Our  
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34 artificial hJM launches the catapult shooting within 10  $\mu$ s, and thus, it could achieve  
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36 an acceleration of approximately 1000 g. Thus, the impulsive force of cavitation  
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38 jetting flow proved to be a powerful tool to realize complex motion control on the  
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40 microscale.  
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#### 44 45 **Efficiency**

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47 We also estimated the energy transfer efficiency based on the energy variation of  
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49 the system before and after bubble collapse. At the onset of bubble collapse, the  
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51 bubble surface energy, defined by  $E_b = 4\pi R_b^2 \sigma \sim 10^{-9}$  J, reaches its maximum value,  
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53 which is much larger than that of the translational kinetic energy ( $\sim 10^{-18}$  J) of a  
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4 recoiling bubble. Based on the observed speed,  $V_p$ , of the hJM after bubble collapse,  
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6 the kinetic energy of the hJM is estimated to be  $E_k = 2\pi\rho R_p^3 V_p^2/3 \sim 10^{-11}$  J. Therefore,  
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8 the energy transfer efficiency,  $\eta \sim E_k/E_b$ , in the launching phase is approximately 1%.  
9  
10 For the total energy transfer efficiency from the catalytic reaction phase to the  
11  
12 micromotor motion phase, the present value is approximately  $10^{-7}$ , and the previous  
13  
14 value from similar experiments is  $10^{-10}$ , which was estimated by Wang et al.<sup>15</sup> The  
15  
16 present value shows an improvement of about three orders of magnitude for spherical  
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18 Janus micromotors and is on the same order as that for the natural furious catapult  
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20 mechanism.<sup>38, 39</sup>  
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25 Compared to the phoretic micro/nano-motor<sup>11, 40</sup>, the present hJM has a  
26  
27 dramatically higher propulsion speed and distinct dependency on the ‘fuel’  
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29 concentration. As analyzed by Ebbens et al.,<sup>41</sup> for a JM with a diameter of less than 10  
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31  $\mu\text{m}$ , the propulsion speed is expected to be proportional to  $1/R$ . The corresponding  
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33 speed for a 10- $\mu\text{m}$  JM is usually  $\sim 1 \mu\text{m}\cdot\text{s}^{-1}$ , which is negligible. The present hJM  
34  
35 configuration that generates the cavitation catapult has overcome this limitation by  
36  
37 increasing the propulsion speed by over three orders of magnitude. Different from  
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39 most of the micro/nano-motors that have a monotonic dependency of velocity on fuel  
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41 concentration, herein, a suitable rather than plentiful fuel supply is the optimum  
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43 swimming strategy. A higher concentration of  $\text{H}_2\text{O}_2$  solution will produce more than  
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45 one bubble around the hJM, and the excessive dissolved oxygen will prevent the  
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47 bubbles from collapsing.  
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## 56 CONCLUSION

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4 This study introduced the strong self-propulsion and dynamic hovering of hJMs by  
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6 cyclical microbubble cavitation. The asymmetric collapse of a cavitation microbubble  
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8 led to an instantaneous jet flow with a speed of up to  $1 \text{ m}\cdot\text{s}^{-1}$  and a relatively high  $Re$   
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10  $\sim 10$ . This hydrodynamic jetting is found to be a key propulsion effect after  
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12 microbubble collapse, in contrast to microbubble recoiling or the JM-bubble  
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14 interaction. Four different propulsion modes were identified based on the  
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16 dimensionless size,  $\gamma$ . Boundary confinement and stand-off distance are two of the  
17  
18 most important factors to generate effective propulsion. We further proposed that  
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20 dynamic hovering is the locomotion mechanism to keep a lightweight micro-object  
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22 swimming underneath an air-liquid interface, the buoyancy of which is counteracted  
23  
24 by the vertical nonreciprocal flow. The combination of the relatively high  $Re$  and the  
25  
26 focused energy of the jet flow improved the efficiency of the hJM up to 1%. The  
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28 findings of this study shed light on the design of more efficient and adaptive  
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30 micro-/nano-motors in autonomous micro-/nano-systems.  
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## 40 ASSOCIATED CONTENT

### 41 Supporting Information

42 The Supporting Information is available free of charge via the internet at  
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44 <http://pubs.acs.org>.  
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47 **SI:** additional results from CFD simulation and analysis of the scaling law of bubble  
48  
49 growth.  
50

- 51 1. SI1: Evaluation of the vertical fluctuation distance of the hJM
- 52 2. SI2: CFD simulation of bubble collapse near different types of boundaries
- 53 3. SI3: CFD simulation of the  $\text{O}_2$  concentration around the hJM
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4. SI4: Scaling law of bubble growth by using the Rayleigh-Plesset equation

**Video:**

1. Video S1: Circular motion and perfect propulsion
2. Video S2: Flow visualization of the jetting flow near the hJM
3. Video S3: Flow visualization at the upper plane of the sJM near the solid-liquid interface
4. Video S4: Flow visualization at the bottom plane of the sJM near the solid-liquid interface
5. Video S5: Four propulsion styles with different  $\gamma$
6. Video S6: Computational fluid dynamics (CFD) simulation of bubble collapse near two types of boundaries

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**Author Contributions**

Leilei Wang and Li Chen contributed equally to this work. Leilei Wang prepared the micromotor and conducted the motion testing. Li Chen simulated the processes of bubble collapse. Hai-hang Cui, Xu Zheng and Zhan-hua Silber-Li designed the experiment. Jing Zhang finished the flow visualization by PIV experiment. Jin-ming Duan and Lei Wang conducted the theoretical analysis for the dynamic hovering of the micromotor. All authors made contributions to the writing of the paper.

**Notes**

The authors declare no competing financial interest.

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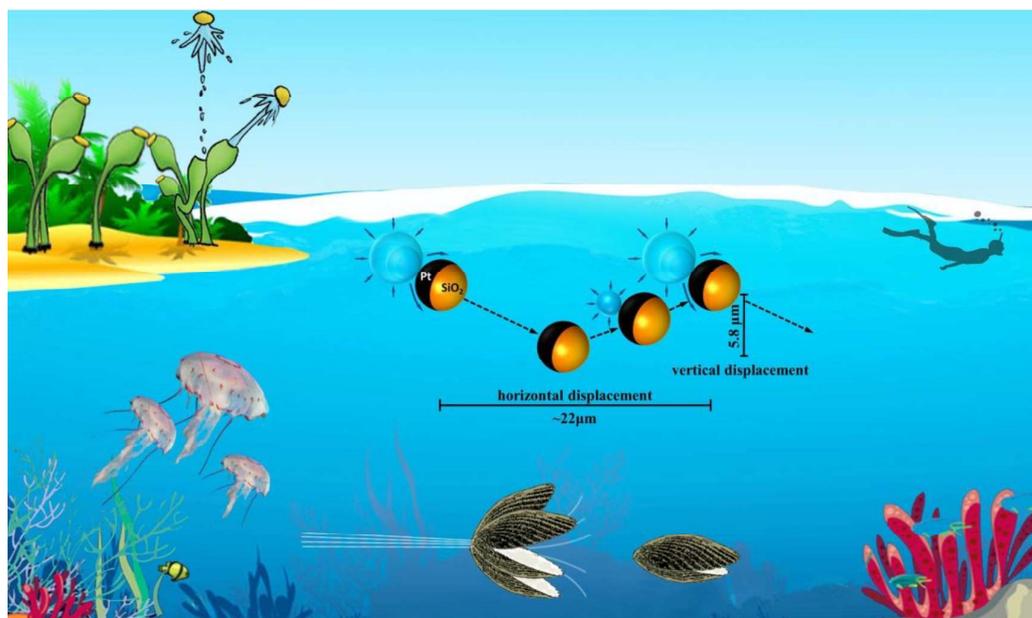
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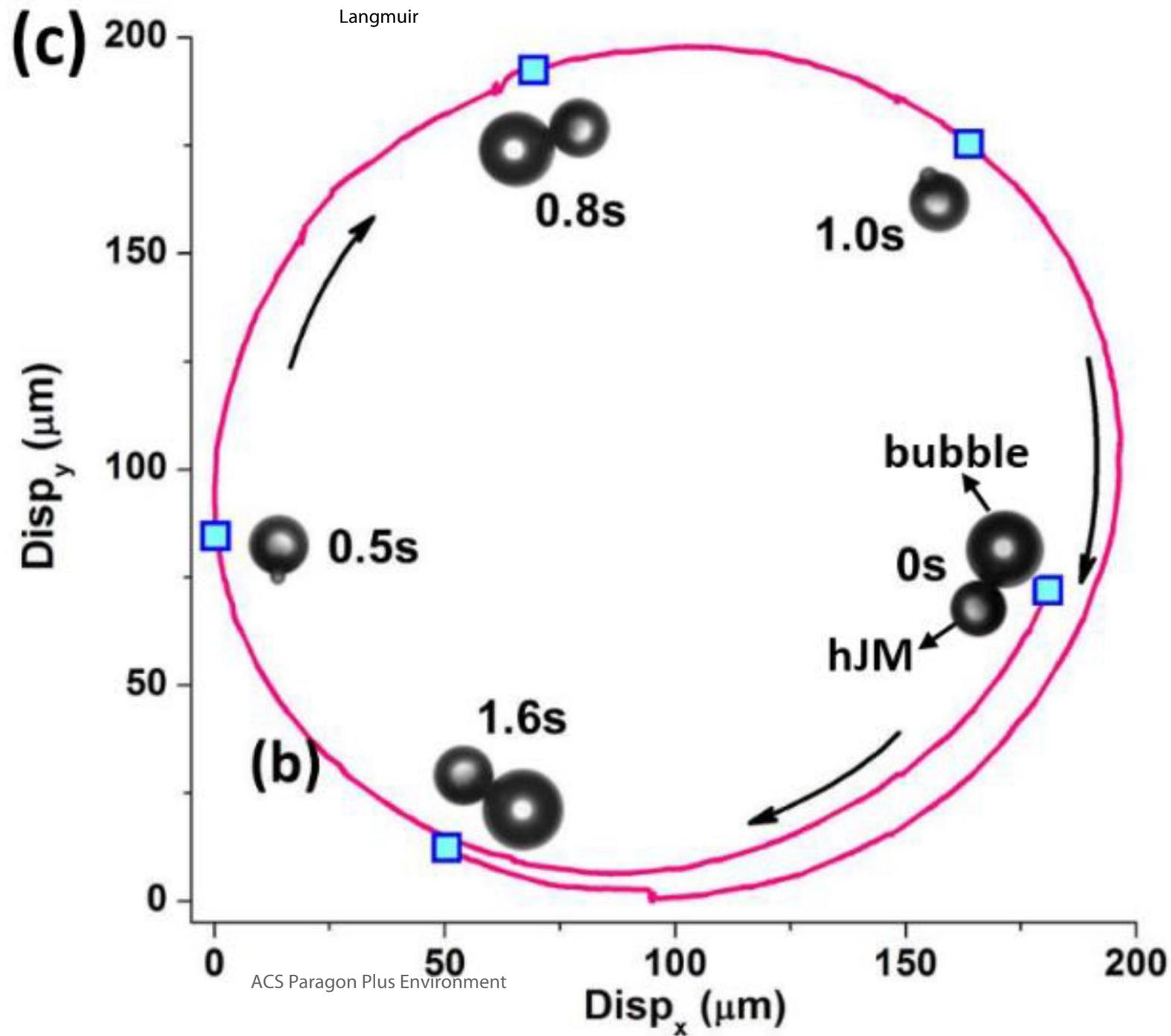
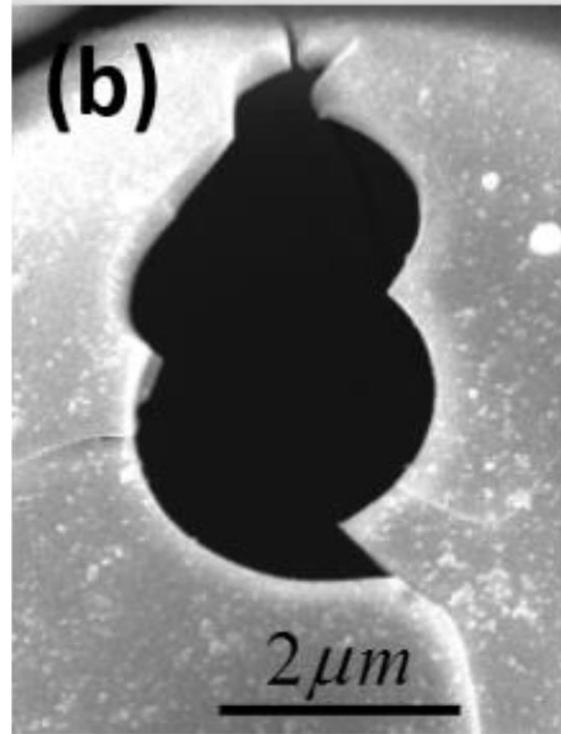
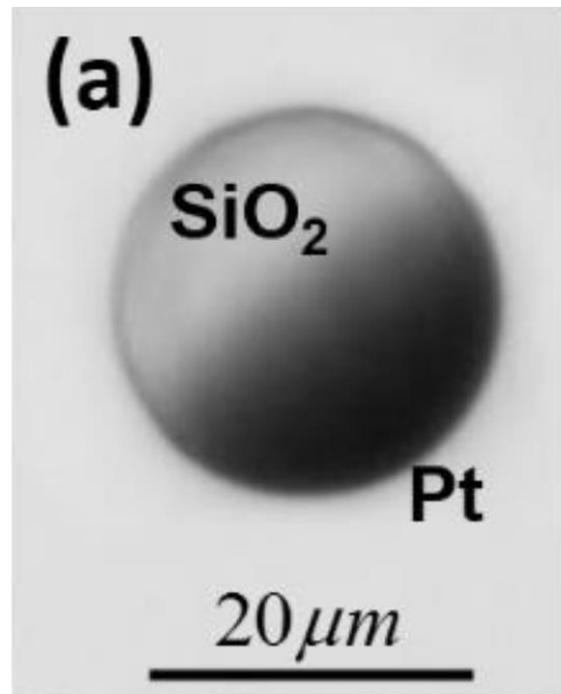
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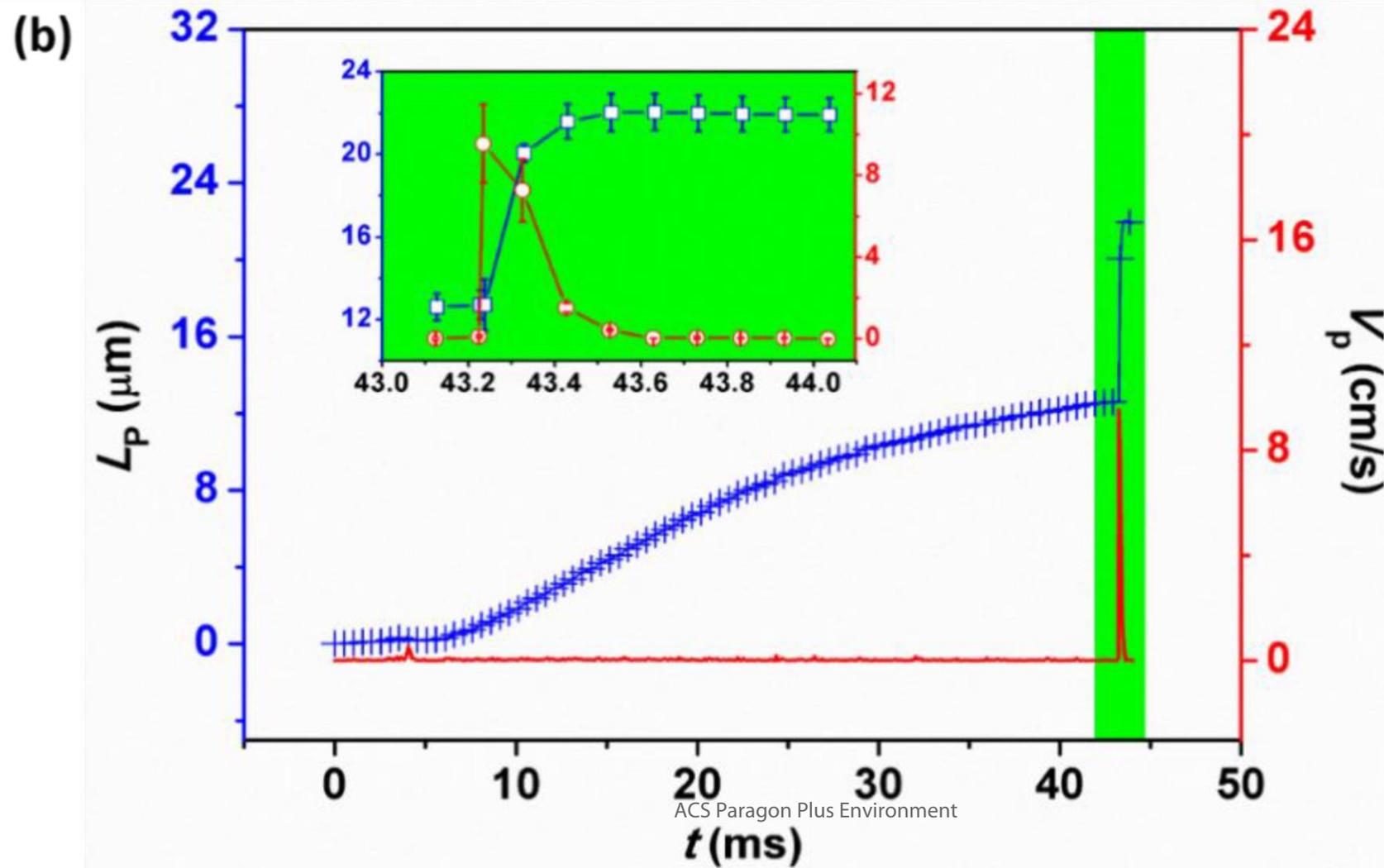
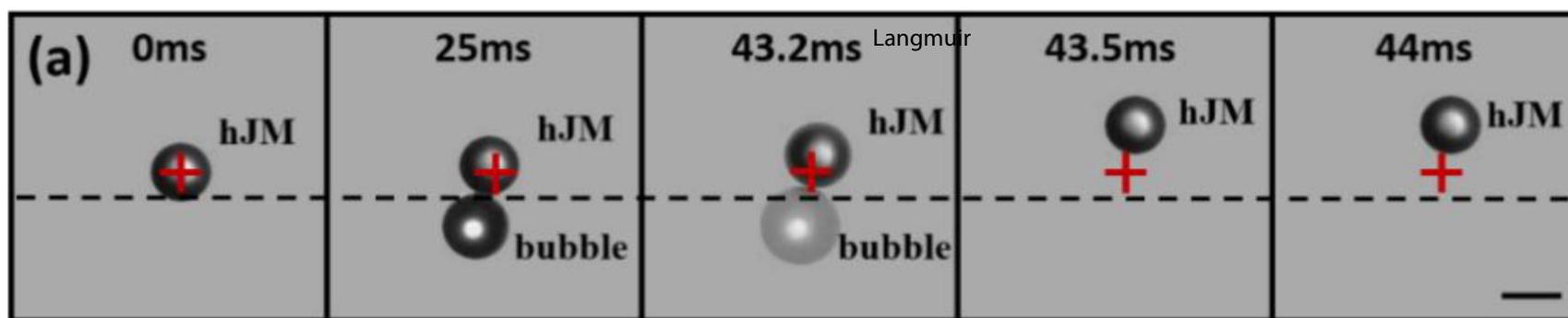
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### Table of Contents Graphic







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