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## Superior strength-ductility synergy by hetero-structuring high manganese steel

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### ABSTRACT

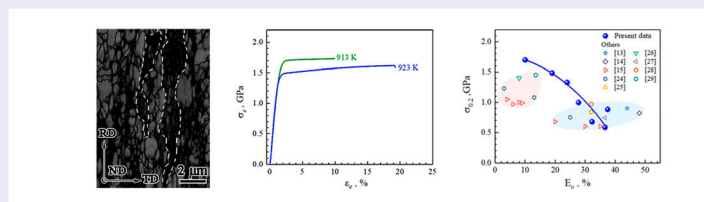
Lacking of forest hardening makes low ductility in steels long challenge particularly at high yield strength. Here, we report to make good use of hetero-structuring for superior strength-ductility synergy in high manganese steel. The point is to retain original deformed structure of large quantity, along with recrystallized ultrafine-grains and fine grains, jointly for most effective heterogeneous deformation-induced (HDI) hardening especially at high strength. The residual plastic strain of larger than 0.2% and large proportion of HDI stress over 60% indicate the crucial role in ductility by HDI hardening. This renders a significantly upgraded strength-ductility combination within high strength scope.

### ARTICLE HISTORY

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### KEYWORDS

Hetero-structuring; heterogeneous deformation-induced strain hardening; ductility; ultra-high strength steel; high manganese steel



### IMPACT STATEMENT

By using the hetero-structuring strategy, a superior strength-ductility synergy is realized specifically at ultra-high strength in high manganese steel.

In advanced high strength steels for structural applications, to pursue the superior ( $\sigma_y, \epsilon_u$ ) combination causes long concern [1–8], where  $\sigma_y$  is the yield strength and  $\epsilon_u$  is the tensile uniform strain. So far, the real challenge lies in low  $\epsilon_u$  particularly at high and even ultra-high  $\sigma_y$  [1–3], typical of the ( $\sigma_y, \epsilon_u$ ) trade-off. The crux of the problem is inadequate strain hardening, which can no longer keep up with high flow stress to circumvent plastic instability [6–8], i.e. necking via strain localization, as predicted by the Considère criterion. On one hand, high  $\sigma_y$  is usually obtained by either cold work or plastic deformation-induced grain refinement. However, such strengthening comes at the expense

of strain hardening [6–8], because intra-granular dislocation plasticity, a potent mechanism for strain hardening, almost disappears. On the other hand, several other strategies for strain hardening take effect mainly at low  $\sigma_y$  in coarse-grained structures, including the transformation-induced plasticity (TRIP) effect [1,5,9], twinning-induced plasticity effect [10,11], second phase [4], and nano-precipitates [3] etc. Even austenite, as ductile phase in steels, is no exception. For example,  $\epsilon_u$  almost disappears at  $\sigma_y$  of 1.45 GPa in 316L austenite stainless steel [12]. The high manganese steel of usually with Mn content larger than 10 wt% [13–15], along with recently well-developed medium-Mn (6–10 wt%) steels

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[1,16], features the TRIP effect for large  $\varepsilon_u$ . However, the TRIP effect will be out of operation at high  $\sigma_y$ . A few exceptions occur in medium-Mn steels due to special carbon partitioning [1], which is, however, not applicable to high-Mn steels.

Recently, the hetero-structure (HS) of varying kinds arouses an ongoing interest for distinct heterogeneous deformation-induced (HDI) hardening [17–20], which is particularly effective to elevate  $\varepsilon_u$  at high  $\sigma_y$  [19,20]. Several typical HSs demonstrate the key role by HDI hardening, including hetero-lamellar structure [19] and three-level grain heterogeneity [20]. The pre-requisite for HDI hardening is microstructural heterogeneities of contrasting mechanical responses upon straining [17,18]. Here we take the HS strategy one step further by pushing for a highly heterogeneous microstructure. The core idea is to reserve the deformed structure as much as possible for high  $\sigma_y$ , while only fewer recrystallized grains for effective HDI hardening. This tailored HS thus shows an extraordinary HDI hardening, providing perfectly acceptable  $\varepsilon_u$  of 10% at  $\sigma_y$  of 1.7 GPa, along with an upgrade ( $\sigma_y, \varepsilon_u$ ) synergy.

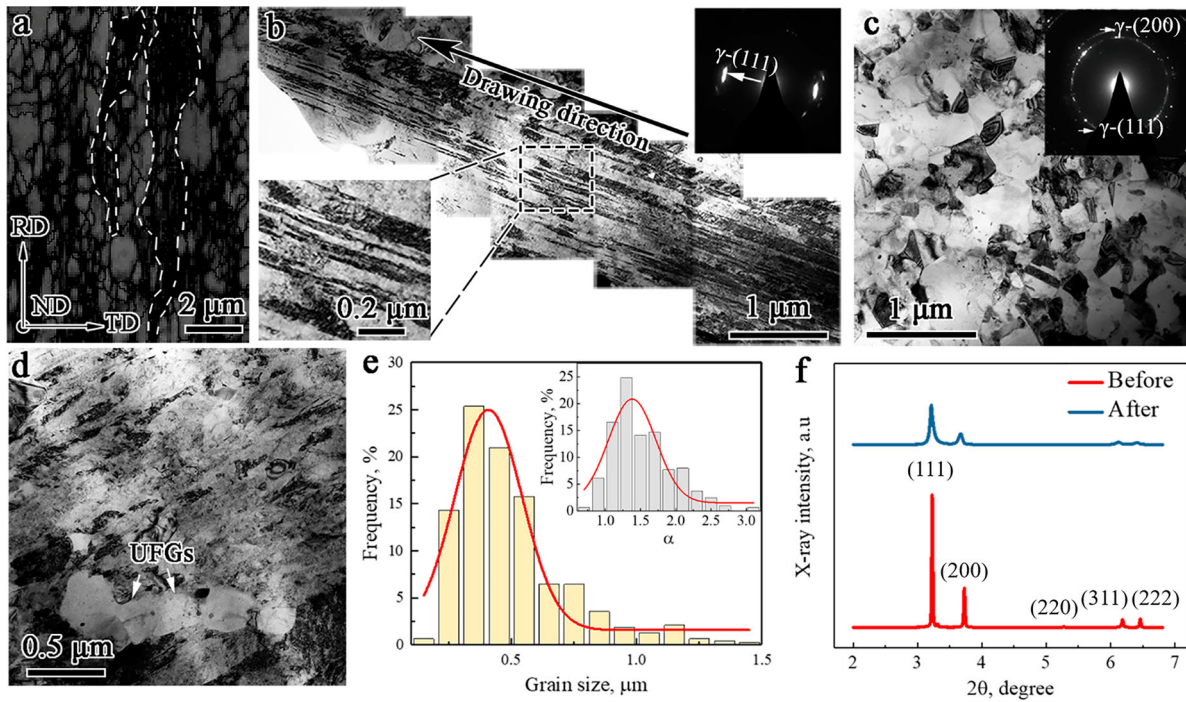
The high-Mn steel is a good model to work with, having face-centered-cubic structured single-phase austenite. The chemical composition was Fe-16Mn-0.5C, weight percent. The starting bar ingot was cast through vacuum smelting, which was hot-forged and then hot-drawn into wires of 0.67 mm in diameter, followed by solution treatment at 1423 K for 2 h and water cooling. The wire was then cold-drawn to 0.33 mm in diameter followed by recrystallization annealing at various temperatures for 10 min. Tensile testing was carried out at strain rate of  $1 \times 10^{-3} \text{ s}^{-1}$  at room temperature. The gauge length of the tensile samples was 50 mm. The extenso-meter was used for strain measurement. Microstructural characterization was conducted by using ZEISS Supra 55 scanning electron microscope (SEM) with electron backscatter diffraction (EBSD) detector and FEI Tecnai G2 F20 TEM. TEM specimens were prepared by mechanical grinding, polishing and low energy ion milling. The synchrotron-based high energy XRD *in situ* experiments were performed at Advanced Photon Source (APS), Argonne National Laboratory, USA. Refer to Ref. [21] for the experimental details.

Figure 1(a) is the EBSD quality image showing the HS after annealing at 923 K. The HS consists of the fiber-like deformed structure (outlined by dotted line in white) and crystallized equiaxed grains. TEM images show elongated structure of tangled dislocations, see Figure 1(b), and crystallized grains, see Figure 1(c), respectively. Both insets are selected area electron diffraction (SAED) patterns, indicating face-centered cubic structured  $\gamma$ -austenite. This is in line with XRD spectrum tested before

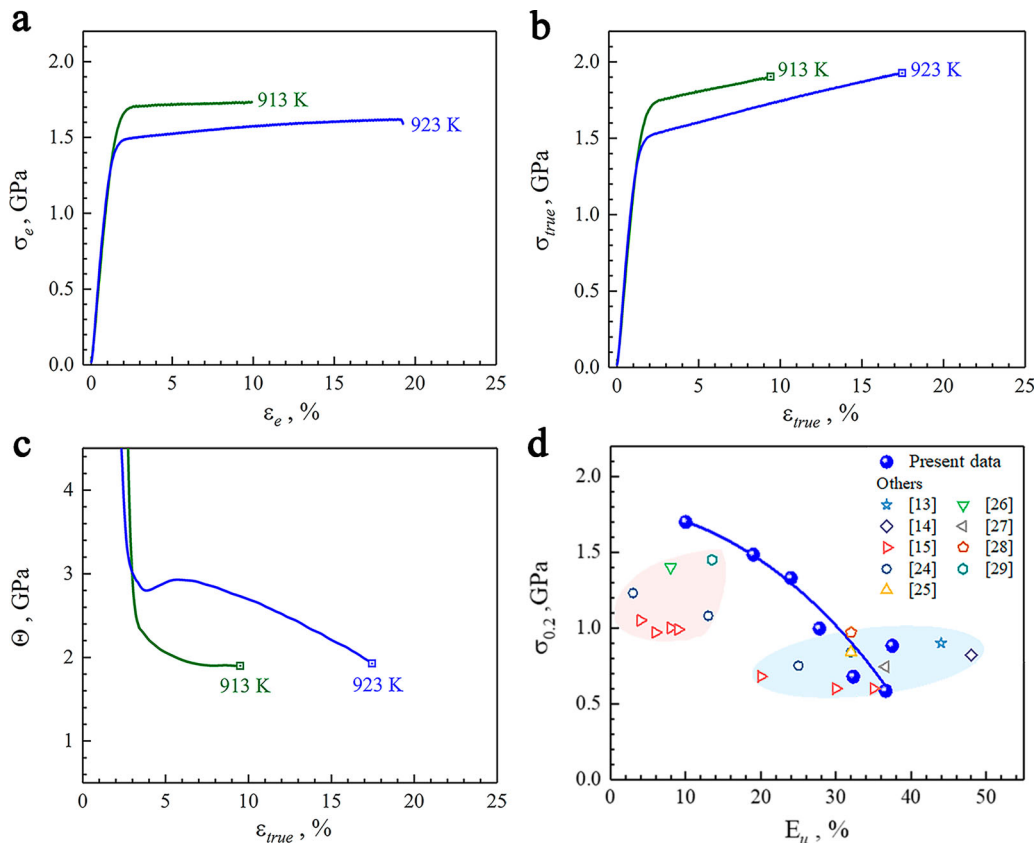
and after tensile testing, see Figure 1(f). The single-phase  $\gamma$ -austenite exists, without detectable either hcp or bcc phase. Figure 1(d) is TEM image showing another HS after annealing at 913 K. The similar microstructural feature is visible to that at 923 K. Figure 1(e) shows size distribution of recrystallized grains in HS after annealing at 923 K based on statistic data of several hundreds of grains from EBSD and TEM images. Inset is the distribution of aspect ratio of long to short axis,  $\alpha$ . Obviously, the HS is trans-scale, with grain sizes spanning UFG to FG. The UFG has an average grain size  $d_{UFG}$ , of 0.34  $\mu\text{m}$ , number density  $\rho_{UFG}$  (number/ $\mu\text{m}^2$ ) of 92.2%, and volume fraction  $f_{vol}$  of 67%. The corresponding data for FG is, respectively,  $\sim 1.2 \mu\text{m}$ , 7.8%, and  $\sim 33\%$ . The mean aspect ratio is 1.37, much larger than 1. Moreover, the volume fraction of recrystallized grains is 48.3% and 17.5%, respectively, in HS after annealing at 923 and 913 K. This indicates that the HS is in a severely deformed state, with a mass of deformed structure preserved.

Figure 2(a) shows two tensile engineering stress-strain ( $\sigma_e - \varepsilon_e$ ) curves.  $\sigma_y$  is 1450 MPa and  $\varepsilon_u$  is 20% after annealing at 923 K.  $\sigma_y$  increases to 1700 MPa,  $\varepsilon_u$  still keeps 10% at annealing temperature at 913 K. Continuous yielding appears, which differs from yield-drop followed by an extended Lüders plateau in nearly all medium-Mn steels at elevated  $\sigma_y$  [1,16]. All ( $\sigma_e - \varepsilon_e$ ) curves at varying annealing temperatures are shown in Fig. S1 in Supplementary. Figure 2(b,c) are, respectively, true stress-strain ( $\sigma_{true} - \varepsilon_{true}$ ) curves and strain hardening rate ( $\vartheta = \partial\sigma/\partial\varepsilon$ )- $\varepsilon_{true}$  curves. Interestingly, an upturn of  $\vartheta$  appears during the early stage of small strains in sample after annealing at 923 K. The upturn of  $\vartheta$  is widely observed in varying microstructures with varying deformation physics [14,19,22,23]. The trans-scale HS facilitates a largely extended elasto-plastic transition when HDI hardening already works. This is probably the reason of upturn in  $\vartheta$  [19,22]. Figure 2(d) shows the ( $\sigma_y, \varepsilon_u$ ) combination of all HSs. The data are also summarized of other high-Mn steels for comparison [13–15,24–29]. Two areas are distinguishable of high and low  $\sigma_y$ . Our data stand out with enhanced  $\varepsilon_u$  within the range of high  $\sigma_y$ , leading to upgraded ( $\sigma_y, \varepsilon_u$ ) synergy. This is indicative of special advantage of the present HS for strain hardening.

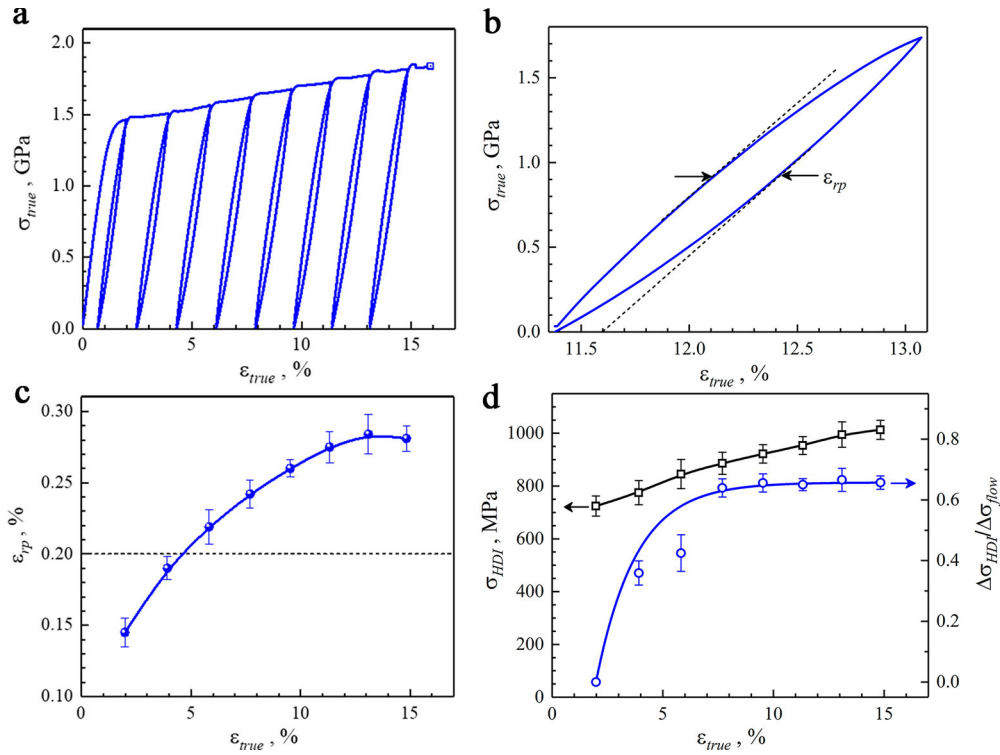
The interrupted unload-reload tensile tests were conducted to reveal strain hardening, see Figure 3(a). The hysteresis loops recur during each unloading-reloading cycle. This signals the Bauschinger effect. The loop width is characterized by residual plastic strain,  $\varepsilon_{rp}$ , following elastic unload, see Figure 3(b). Of special note is record-wide loops.  $\varepsilon_{rp}$  is even larger than 0.2% starting from unload strain of 5%, see Figure 3(c). This indicates that the compressive plastic flow sets in already upon elastic unload, even though applied stress is still under



**Figure 1.** Heterogeneous structure (HS). All for HS after annealing at 923 K except for (c) at 913 K. (a) EBSD quality image. A few areas encircled by dotted line are fiber-like deformed structure. (b), (c), and (d) TEM images showing elongated lamellae and recrystallized grains. Insets in (b) and (c) are SAED pattern. (e) Statistic grain size distribution and aspect ratio (inset) for recrystallized grains. (f) XRD spectrum before and after tensile testing.



**Figure 2.** Tensile property. (a)  $\sigma_e - \varepsilon_e$  curves after annealing at 913 and 923 K. (b)  $\sigma_{true} - \varepsilon_{true}$  curves. (c)  $\sigma - \varepsilon_{true}$  curves. (d)  $(\sigma_y, \varepsilon_u)$  synergy.



**Figure 3.** HDI stress. (a) Tensile  $\sigma_{true} - \varepsilon_{true}$  curve. (b) Hysteresis loop at unloading strain of 13%. (c)  $\varepsilon_{rp}$  versus  $\varepsilon_{true}$  curve. (d)  $\Delta\sigma_{HDI}$  and  $\Delta\sigma_{HDI}/\Delta\sigma_{flow}$  versus  $\varepsilon_{true}$  curve.

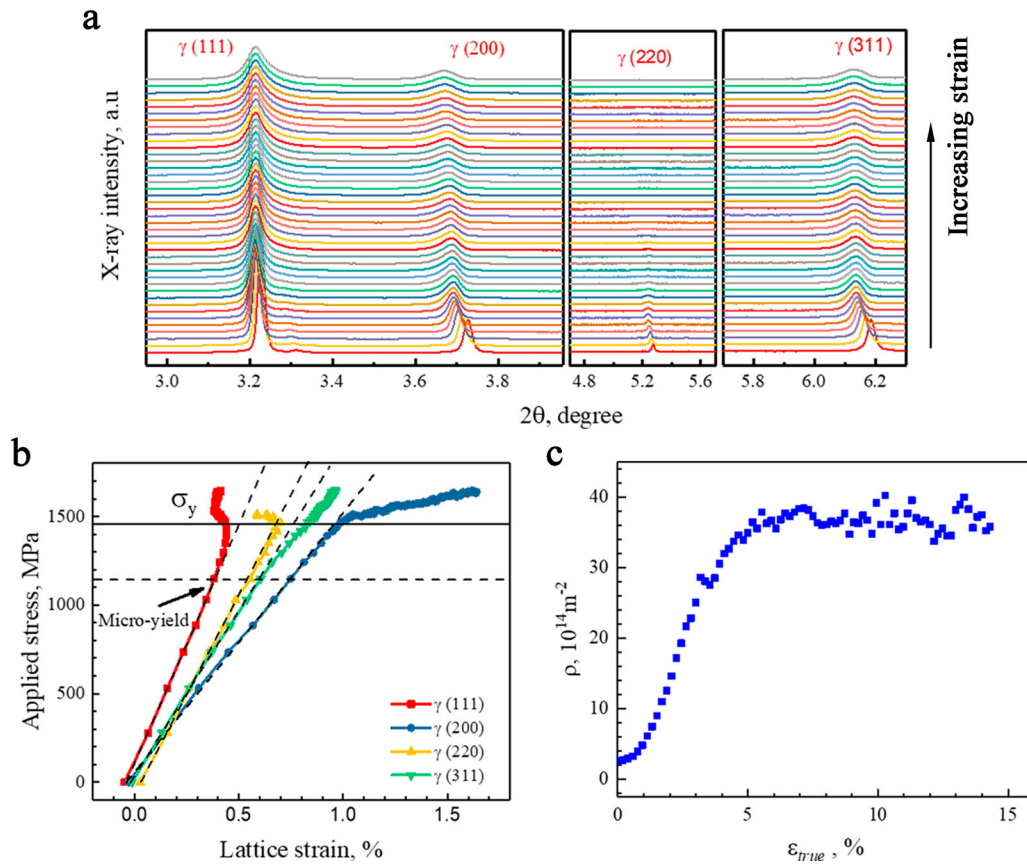
tension. This is an unambiguous sign which unequivocally demonstrates the key effect of back stress, as a part of HDI stress ( $\sigma_{HDI}$ ) [19,30,31]. Further, both the heterogeneous deformation-induced (HDI) stress,  $\sigma_{HDI}$ , together with the proportion,  $\lambda$ , of  $\Delta\sigma_{HDI}$  to  $\Delta\sigma_{flow}$  were calculated, see Figure 3(d), where  $\Delta\sigma_{HDI}$  and  $\Delta\sigma_{flow}$  are the increment of both  $\sigma_{HDI}$  and  $\sigma_{flow}$  after yielding, respectively, by subtracting  $\sigma_{HDI}$  and  $\sigma_{flow}$  at offset strain of 0.2%. Refer to Ref. [30] for the method of calculating  $\Delta\sigma_{HDI}$ . It is visible that  $\sigma_{HDI}$  increases with tensile strain. At the same time,  $\lambda$  rises rapidly to 65% at first and then levels off. The trend of both  $\sigma_{HDI}$  and  $\lambda$  is well in line with that in other HSs [19,20], indicating the crucial role by HDI hardening throughout tensile deformation.

The microscopic plastic response was further investigated by using synchrotron-based high energy *in situ* XRD tensile load, see Figure 4(a). The change of axial lattice strain with applied stress is shown in Figure 4(b). The equation for lattice strain calculation is given in Supplementary. Interestingly, lattice strain of (111) grain family begins to deviate from linearity at stress of 1150 MPa, in contrast to macroscopic  $\sigma_y$  of 1450 MPa. This is micro-yielding which happens at first in (111) grain family. This indicates an extended elasto-plastic transition, inherent to the trans-scale HS [19,20]. After global yielding, the rate of increase in lattice strain speeds up in (200) and (311) grain family, tilting linear lattice strain to the right.

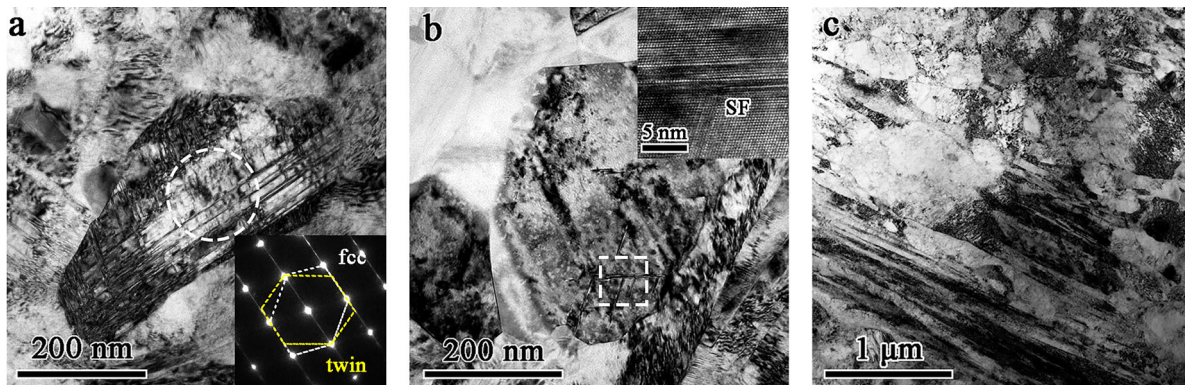
(200) grain family comes fastest, (311) second, in sharp contrast to the trend in (111) and (220) families. This indicates load partitioning during tensile deformation. Namely, (111) and (220) grain families carry less loads, whilst (200) and (311) will bear a proportionally increasing fraction of applied loads. The load partitioning is, actually, the direct result of HDI stress [19,20]. Moreover, the dislocation density,  $\rho$ , is measured according to the modified Williamson-Hall (W-H) equation [32], see Supplementary for the calculation method.  $\rho$  shows an initial rapid rise and then level-off during tensile deformation, see Figure 4(c).

Finally, TEM observations show that the deformation nanotwins (Figure 5(a)), stacking faults (Figure 5(b)), and tangled high-density dislocations (Figure 5(c)) are all formed inside recrystallized grains during tensile deformation.

The present HS consists of the deformed structure in large amounts, together with recrystallized UFGs and FGs. Therein, contrasting plastic responses of two kinds are seen. One is  $\sigma_y$ , from big to small in the order of the deformed structure, UFGs, and FGs. This is the reason for micro-yielding, which happens at first in (111) grain family at 1150 MPa,  $\sim 300$  MPa below global  $\sigma_y$ . The other is strain hardening, which is almost absent in deformed structure, limited in UFGs [6,7], while extraordinary in FGs. This induces the polarization of strain



**Figure 4.** Synchrotron-based *in situ* XRD tensile loading. (a) XRD spectrum in varying crystal planes. (b) Applied stress vs lattice strain curves. Arrow indicates the onset of micro-yield in (111) grain family. (c)  $\rho$  vs  $\epsilon_{true}$  curve.



**Figure 5.** TEM observations of microstructural evolution. (a) Deformation twins. Inset: SAED pattern showing twin relationship. (b) Stacking faults (SFs). Inset: high-resolution TEM image showing lattice image of SF. (c) Tangled dislocations of high density.

localization versus plastic stability. As a result, tensile deformation is highly heterogeneous inside the HS. This causes a local, additional stress, defined as HDI stress [18], at hetero-interfaces between grains of contrasting plastic responses. The HDI stress is a pair of balancing forces: back stress imposed on ductile FGs and opposite forward stress on the strong deformed structure. The dislocation model of back stress is proposed for strain hardening in terms of the pile-up of geometrically necessary dislocations (GNDs) [18,33–36]. Correspondingly,

HDI hardening is experimentally evidenced later [18], serving as a combined effect induced by back stress and forward stress [37].

The HDI hardening is dominant in the present HS. It is worthy to note the initial rise followed by level-off for both  $\lambda$  (Figure 3(d)) and  $\rho$  (Figure 4(c)) as tensile strain increases, in contrast to the monotonic rise in both  $\epsilon_{rp}$  (Figure 3(c)) and  $\sigma_{HDI}$  (Figure 3(d)). The initial rise in  $\rho$  is due to the storage of dislocations into FGs, while that for the remaining is ascribed to the onset of HDI

hardening as early as micro-yielding. With further straining, the rise of both  $\sigma_{\text{HDI}}$  and  $\varepsilon_{rp}$  indicates that HDI hardening continues to play a key role during tensile deformation. At this stage, the dislocation cross slip happens such that both the generation and annihilation of dislocations co-exist, typical of Stage III of strain hardening [38]. This is the reason of level-off in  $\rho$ . It is further argued that the softening effect emerges in deformed structure and even UFGs due to forward stress. Namely, forest hardening weakens gradually. Therefore, the percentage of  $\sigma_{\text{HDI}}$  (Figure 3(d)), as a comprehensive effect of strain hardening by back stress and softening, levels off. In other words, HDI hardening plays an increasing role throughout tensile deformation, in line with growing  $\sigma_{\text{HDI}}$ . In addition, HDI hardening is in action already during micro-yielding, which leads to strengthening to increase  $\sigma_y$  [19,20,31].

FGs play a key role in strain hardening by back stress in the present HS. Specifically, the smaller grain size within the micron-scale regime, the stronger effect of dislocation pile-up for strain hardening [35,36], and hence, the stronger HDI hardening will be. Therefore, FGs of  $\bar{d}$  of 1.2  $\mu\text{m}$  play a significant role in ductility. Reasonably, the less volume fraction of FGs, the weaker HDI hardening will be. This is probably the reason of less uniform strain in HS after annealing at 913 K than that at 923 K. Yet, yield strength increases by 250 MPa.

In summary, the hetero-structuring strategy is applied to an old high-Mn steel for ductility at high yield strength. The HDI hardening plays a dominant role in ductility. The present study helps out for understanding deformation physics in the HS for tailoring the microstructure to upgrade the strength and ductility combination.

## Disclosure statement

No potential conflict of interest was reported by the author(s).

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