



# Hardening Ni<sub>3</sub>Al via complex stacking faults and twinning boundary

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## ABSTRACT

Introducing nanoscale planar defects instead of adding alloying elements has been applied to improve the mechanical properties of materials. In this paper, we show that, from an atomistic perspective, hardness of nickel aluminide (Ni<sub>3</sub>Al) can be effectively enhanced by complex stacking faults and twinning boundary. The size effect of planar defects is induced by a competition between hardening because of regeneration of stacking faults and softening due to detwinning. The complex stacking faults have a better hardening effect than twinning boundaries with a spacing below 3.0 nm. These findings provide new insights into nanostructural design of aerospace materials with high hardness.

## 1. Introduction

Alloying metals and nanostructured materials with defects exhibit exceptional mechanical and physical properties that are promising in various applications [1–6]. As is known, alloying is usually applied to improve materials; however, it is more dependent on resources and not conducive to recycling and re-utilization. In contrast, by adjusting defects inside a material, nanoscale microstructural design can sustainably enhance its properties [7–10]. It is shown that planar defects like twinning boundary (TB) can simultaneously increase the hardness and stability of nanostructured diamond and cubic boron nitride [11,12], as well as other metallic materials [13–15]. Whereas, it is unclear whether stacking faults, another kind of common planar defect, can increase hardness of materials. To the best of our knowledge, there is still lack of studies on how stacking faults affect hardness of nanostructured materials.

Nickel aluminide (Ni<sub>3</sub>Al) is an intermetallic ordered alloy with the L1<sub>2</sub> structure. It has been widely applied in aerospace industries such as turbine blades and vanes in aircraft engines. However, a lower susceptibility to plastic deformation and a higher tendency to brittle cracking strongly limit its industrial applications [16–18]. To elucidate mechanisms of deformation and hardness of single crystal Ni<sub>3</sub>Al (SC-Ni<sub>3</sub>Al), extensive nanoindentation experiments and numerical simulations have been performed on, e.g., effects of crystallographic orientation,

temperature, indenter radius and incipient plasticity [19–25]. It is found out that the super-lattice structure of Ni<sub>3</sub>Al leads to a complexity of microstructures and consequently diverse modes of deformation. Depending on atomic arrangements in the L1<sub>2</sub> structure, there are two typical kinds of intrinsic planar defects in Ni<sub>3</sub>Al such as complex stacking faults (CSFs) and TBs [26,27]. Studying these planar defects is significant to a better understanding of hardness of nanostructured Ni<sub>3</sub>Al. Here, it is worth noting that the size of planar defects plays a major role in tuning dislocation activities, which drastically affects the hardness of L1<sub>2</sub> Ni<sub>3</sub>Al.

In this paper, we introduced CSFs into Ni<sub>3</sub>Al to investigate whether such configurations could harden Ni<sub>3</sub>Al substrate in comparison with TBs. By using molecular dynamic simulations, a series of SC-Ni<sub>3</sub>Al, CSF-Ni<sub>3</sub>Al, and TB-Ni<sub>3</sub>Al were modeled under nanoindentation with various spacings between parallel planar defects (hereafter referred to as the spacing). The size effect of planar defects on hardness and corresponding deformation mechanism at the atomistic level have been investigated.

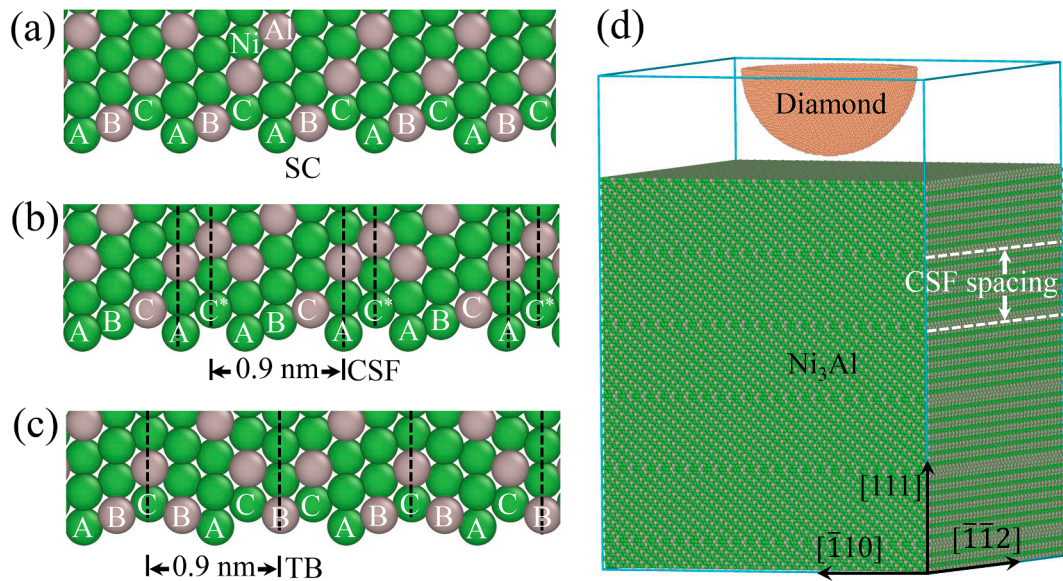
## 2. Methods

### 2.1. Nanostructured Ni<sub>3</sub>Al models

Generally, SC-, CSF- and TB-Ni<sub>3</sub>Al models were established on the fact that Ni<sub>3</sub>Al is a close-packed structure with an arrangement of three

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**Fig 1.** The stacking sequence of nanostructured  $L1_2$   $Ni_3Al$  in (a) SC, (b) CSF and (c) TB with a spacing of 0.9 nm between parallel planar defects. (d) Sketch of a nanoindentation model for CSF- $Ni_3Al$  with a spacing of 3.9 nm between parallel CSFs.

successive planes, denoting as A, B and C, along the [111] direction (see Fig. 1a–c, which is also Fig. S1 for clarity of the supplementary data). Here, SC- $Ni_3Al$  models consist of periodically reproducing the ABC stacking sequence. Considering planar defects, a system should contain at least one ABC unit to keep integrity of the  $L1_2$  crystal structure. This gives the lower limit of a spacing, i.e., 0.9 nm. Specifically, CSF- $Ni_3Al$  models were formed by shearing C with  $a/6[11\bar{2}]$  (111), with  $a$  being the lattice constant of  $Ni_3Al$ . That is, CSF- $Ni_3Al$  with a spacing of 0.9 nm corresponds to a stacking sequence of ***AC\*ABC*** as a periodically repeating unit, where bold and italic letters represent planar defects. Here, the layer ***C\**** adopts an alternatively atomic arrangement in contrast to the layer C of SC- $Ni_3Al$  [26]. The corresponding periodic stacking sequence of TB- $Ni_3Al$  with a spacing of 0.9 nm is ***CBACBCAB***. Fig. 1d shows an initial configuration of CSF- $Ni_3Al$  with a spacing of 3.9 nm for indentation simulation. All  $Ni_3Al$  substrates were created in a cubic shape with a size of  $20 \times 20 \times 22$  nm<sup>3</sup> along the X- $[1\bar{1}0]$ , Y- $[11\bar{2}]$  and Z-[111] directions, containing  $\sim 800,000$  atoms. A hemisphere shell diamond indenter was used with a diameter of 10 nm ( $\sim 20,000$  atoms). During indentation, periodic boundary conditions were introduced in the X and Y crystallographic directions. The top surface was chosen as the one under indentation, while the region was fixed at bottom with a thickness of 1.0 nm.

## 2.2. Molecular dynamics simulations

For CSF- and TB- $Ni_3Al$  models, eight samples were simulated with various spacings (i.e., 0.9, 1.5, 2.1, 2.7, 3.9, 5.2, 6.4 and 10.7 nm). The SC- $Ni_3Al$  substrate was taken as a reference to investigate hardening effect of TBs and CSFs. Atomistic simulations were performed by using the Largescale Atomic/Molecular Massively Parallel Simulator [28]. The embedded-atom potential function for a Ni–Al system developed by Mishin [29] was taken to define the atomic interaction of  $Ni_3Al$ . In this function, the total energy,  $E$ , of a system can be described as

$$E = \sum_{\substack{ij \\ i \neq j}} V_{EAM}(r_{ij}) + \sum_i F(\bar{\rho}_i) \quad (1)$$

where  $V_{EAM}(r_{ij})$  is a pair potential represented as a function of the distance  $r_{ij}$  between atoms  $i$  and  $j$ , and  $F$  is the embedding energy of atom  $i$ , and  $\bar{\rho}_i$  is the electron density, which is given by

**Table 1**

Lennard-Jones potential function parameters for C–Ni and C–Al [30,31].

Parameters	C–Ni	C–Al
$\sigma_{ij}$ , Equilibrium distance (nm)	0.2852	0.2976
$\epsilon_{ij}$ , Cohesive energy ( $10^{-3}$ eV)	23.1	31.5
$r_0$ , Cutoff distance (nm)	0.8	0.8

$$\bar{\rho}_i = \sum_{\substack{j \\ i \neq j}} g_j(r_{ij}) \quad (2)$$

where  $g_j(r_{ij})$  is the electron density of atom  $j$ .

The force between a diamond indenter and substrate was described with a two-body Lennard-Jones potential function,

$$E = 4 \sum_{\substack{ij \\ i \neq j}} \epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right], r_{ij} < r_0 \quad (3)$$

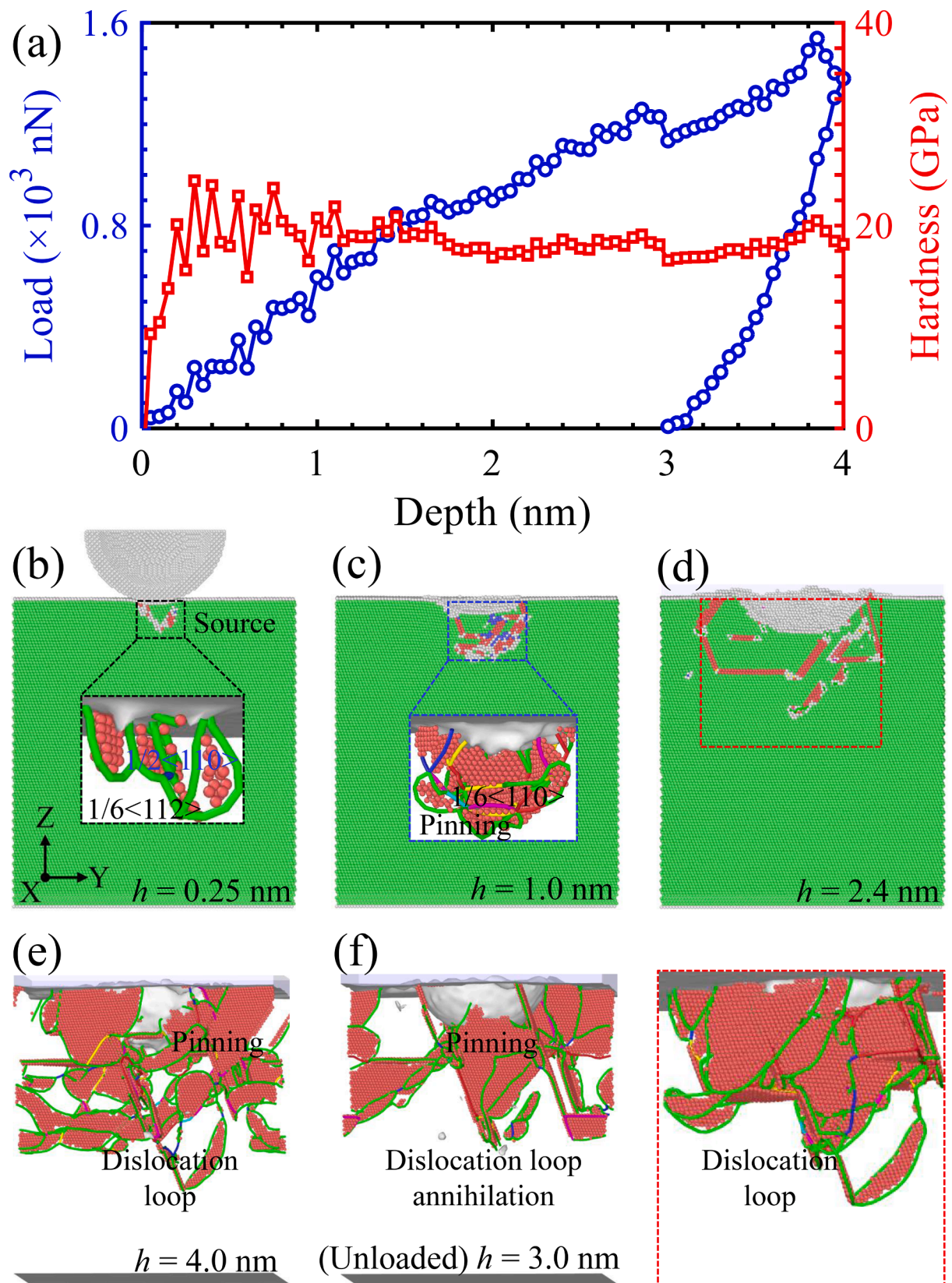
where  $\epsilon_{ij}$  is cohesive energy;  $\sigma_{ij}$  is the equilibrium distance and  $r_0$  is the cutoff distance [30,31]. Their values are listed in Table 1.

Simulations were carried out by integrating Newton's equations of motion for all atoms with a time step of 1 fs. At the start of simulation, initial configurations were energetically minimized by relaxing all samples for 50 ps at 300 K. To obtain hardness of nanostructural  $Ni_3Al$ , an indentation load was applied along the Z direction (perpendicular to planes of CSFs and TBs). The indentation speed and step increment were  $10 \text{ m s}^{-1}$  and  $5.0 \times 10^{-2}$  nm, respectively. The maximum indentation depth was 4.0 nm, smaller than the diameter of indenter. Deformation and defects of  $Ni_3Al$  substrate were recognized via the common neighbor and dislocation analysis and then, they were visualized with software OVITO [32].

## 2.3. Determining volume of plastic zones

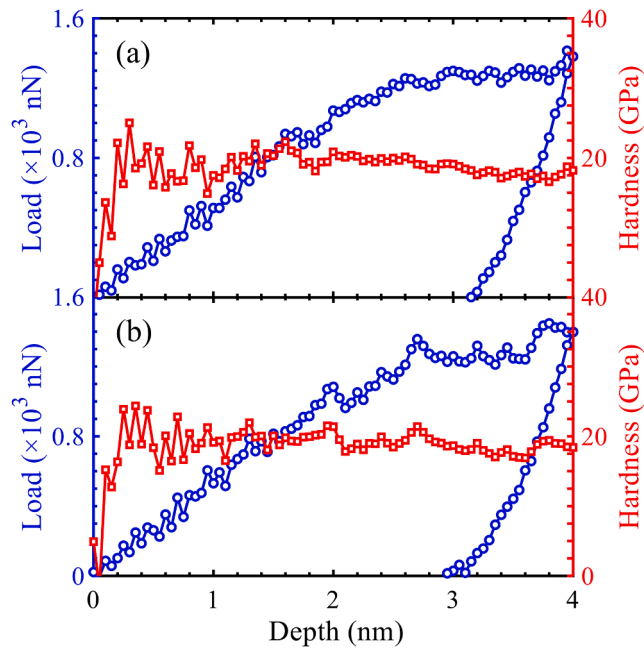
To assess the relative constraint of planar defects to expanding of a plastic zone, we resort to the Taylor relationship in which hardness ( $H$ ) can make a connection with the dislocation density ( $\delta$ ) by

$$H = M C \alpha G b \sqrt{\delta} \quad (4)$$



**Fig 2.** (a) Typical indentation load/hardness-depth relationships of SC-Ni<sub>3</sub>Al and the atomic configurations of an SC-Ni<sub>3</sub>Al at various indentation depths of (b) 0.25 nm, (c) 1.0 nm, (d) 2.4 nm, (e) 4.0 nm and (f) 3.0 nm (unloaded), where atoms were colored by common neighbor and dislocation analysis. Insets in (b)–(d) show structures of local dislocations visualized by dislocation analysis with green, blue, purple, yellow and red lines indicating  $1/6\langle 112 \rangle$  Shockley,  $1/2\langle 110 \rangle$  perfect,  $1/6\langle 110 \rangle$  stair-rod,  $1/3\langle 100 \rangle$  Hirth, and other kind of dislocations, respectively. FCC structures were removed for clarity in (e) and (f).





**Fig. 3.** Indentation load/hardness-depth relationships of (a) TB- $\text{Ni}_3\text{Al}$  and (b) CSF- $\text{Ni}_3\text{Al}$  with a spacing of 3.9 nm between parallel defects.

where  $M$  is the Taylor factor,  $C$  represents constraint imposed by the elastically deformed area surrounding an indenter,  $\alpha$  is a constant,  $G$  is the shear modulus, and  $b$  is Burgers vector [33].

In simulations, the  $1/6\langle 112 \rangle$  Shockley dislocation accounts for an overwhelming percentage, thus we assume that there is only one value for  $b$ . Here, let  $MC\alpha Gb = k$  ( $k$  can be regarded as a constant), and then Eq. (4) can be simplified to

$$H = k \times \sqrt{\frac{L}{V}} \quad (5)$$

where  $L$  and  $V$  indicate the total length of dislocation lines and the volume of a plastic zone, respectively. By selecting  $V$  of SC- $\text{Ni}_3\text{Al}$  as a reference, the volumes of TB- $\text{Ni}_3\text{Al}$  and CSF- $\text{Ni}_3\text{Al}$  can be subsequently determined according to Eq. (5) since  $L$  can be directly measured by dislocation analysis.

### 3. Results

#### 3.1. Deformation mechanisms of SC- $\text{Ni}_3\text{Al}$

As shown in Fig. 2a, there is an upward trend with many slight drops

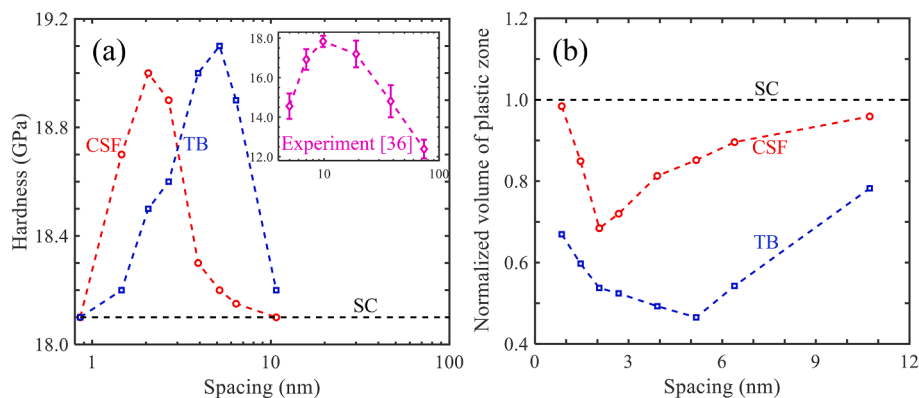
or fluctuations in a typical indentation load-depth curve, corresponding to multiple dislocation events, until the ultimate depth of 4.0 nm. Subsequently, with the indenter retracted by 1.0 nm, load gradually decreases to 0 GPa at a depth of 3.0 nm. However, the hardness-depth curve increases sharply at the beginning and reaches the peak value of 24.5 GPa. Then, it gradually fluctuates and tends to be stable. Hardness of SC- $\text{Ni}_3\text{Al}$  was measured as 18.1 GPa, which is an average value between indentation depths of 2.0–4.0 nm and the same strategy was adopted to characterize hardness of nanostructural  $\text{Ni}_3\text{Al}$ .

To clarify the deformation mechanism of SC- $\text{Ni}_3\text{Al}$ , microstructures with various depths ( $h$ ) were extracted by using the common neighbor and dislocation analysis (see Fig. 2b–f). At a depth of 0.25 nm, a few  $1/6\langle 112 \rangle$  Shockley dislocations nucleate on the surface of SC- $\text{Ni}_3\text{Al}$  substrate beneath the indenter, and then a  $1/2\langle 110 \rangle$  perfect dislocation emerges to pin dislocations (Fig. 2b). Further, with depth increasing, more  $1/6\langle 112 \rangle$  Shockley dislocations (accounting for 57.4% density of dislocation lines) nucleate below the surface and propagate inward. Reaction between  $1/6\langle 112 \rangle$  Shockley dislocations forms  $1/6\langle 110 \rangle$  stair-rod dislocations (with a density of 6.4%) at their junction areas, which results in dislocation pinning (Fig. 2c). As depth reaches 2.4 nm,  $1/6\langle 112 \rangle$  Shockley dislocations continuously nucleate, grow, slip and interact, generating dislocation loops at deeper positions in  $\text{Ni}_3\text{Al}$  substrate (Fig. 2d). Further increase in depth induces more dislocation activities as shown in Fig. 2e. At the depth of 4.0 nm, dislocations in SC- $\text{Ni}_3\text{Al}$  substrate are mainly  $1/6\langle 112 \rangle$  (accounting for 77.1%), together with a small amount of  $1/6\langle 110 \rangle$  stair-rod,  $1/3\langle 100 \rangle$  Hirth,  $1/3\langle 111 \rangle$  perfect and  $1/2\langle 110 \rangle$  perfect. Finally, as the indenter retracts from 4.0 nm to 3.0 nm, annihilation and contraction of dislocation loops are seen with the length of dislocation lines reducing from  $9.7 \times 10^2$  to  $5.3 \times 10^2$  nm (see Fig. 2e and f).

#### 3.2. Effects of the spacing between planar defects

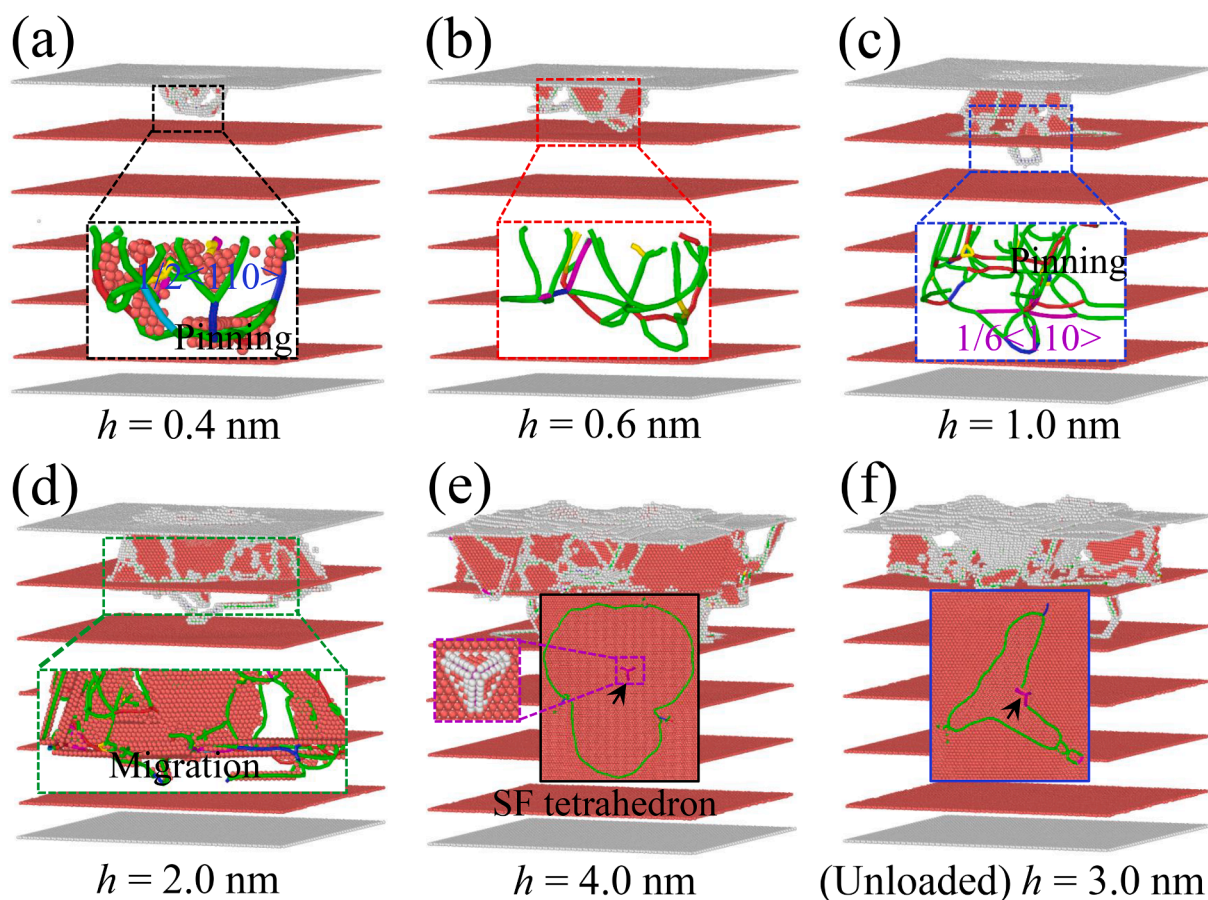
The typical curves of indentation load (hardness) versus depth in TB- $\text{Ni}_3\text{Al}$  and CSF- $\text{Ni}_3\text{Al}$  are illustrated in Fig. 3a and b, with a spacing of 3.9 nm between parallel defects. It is shown that, in contrast to SC, nanostructures such as TBs and CSFs improve hardness of  $\text{Ni}_3\text{Al}$ , as summarized in Fig. 4a. Specifically, hardness of CSF- $\text{Ni}_3\text{Al}$  increases from 18.1 GPa (the same as that of SC- $\text{Ni}_3\text{Al}$ ) to 19.0 GPa as spacing decreases from 10.7 nm to 2.1 nm, indicating the Hall-Petch effect. However, hardness of CSF- $\text{Ni}_3\text{Al}$  falls to 18.1 GPa with the spacing further decreasing to 0.9 nm, exhibiting the inverse Hall-Petch effect. For TB- $\text{Ni}_3\text{Al}$ , the maximal value of hardness, 19.1 GPa, is attained at a spacing of 5.2 nm. The similar inverse Hall-Petch effect was also observed with a lower spacing. Here it is worth noting that hardness of CSF- $\text{Ni}_3\text{Al}$  or TB- $\text{Ni}_3\text{Al}$  is beyond that of SC- $\text{Ni}_3\text{Al}$ . Moreover, CSFs have a stronger hardening effect with a spacing less than 3.0 nm, while TBs are in the lead with a spacing more than this value (see Fig. 4a).

As shown in Fig. 4b, the volume of a plastic zone is strongly



**Fig. 4.** (a) Hardness of nanostructured  $\text{Ni}_3\text{Al}$  and (b) normalized volume of plastic zones versus spacing between parallel planar defects.





**Fig 5.** Evolution of microstructures in TB- $\text{Ni}_3\text{Al}$  with a spacing of 3.9 nm between parallel TBs at various indentation depths of (a) 0.4 nm, (b) 0.6 nm, (c) 1.0 nm, (d) 2.0 nm, (e) 4.0 nm and (f) 3.0 nm (unloaded), where atoms were colored by dislocation analysis with FCC structures removed for clarity. Insets in (a)–(d) show structures of local dislocations. Insets with black and blue edges represent the bottom views below the second TB layer in (e) and (f), respectively. Black arrows mark SF tetrahedrons. Inset with a purple dashed edge in (e) shows the three-dimensional structure of SF tetrahedron.

dependent on spacing. The plastic zone volume of CSF- $\text{Ni}_3\text{Al}$  decreases to its minimum, as spacing increases from 0.9 nm to 2.1 nm, and then, it increases and closes to the corresponding value of SC- $\text{Ni}_3\text{Al}$  with spacing rising to 10.7 nm. For TB- $\text{Ni}_3\text{Al}$ , there is a similar trend, and the volume firstly reduces as spacing decreases from 10.7 to 5.2 nm. Then, it climbs as spacing is reduced to 0.9 nm. This is just opposite to that of hardness, and as shown in Fig. 4a, the volumes of plastic zones and hardness reach their minimum and maximum values at the same spacing, respectively.

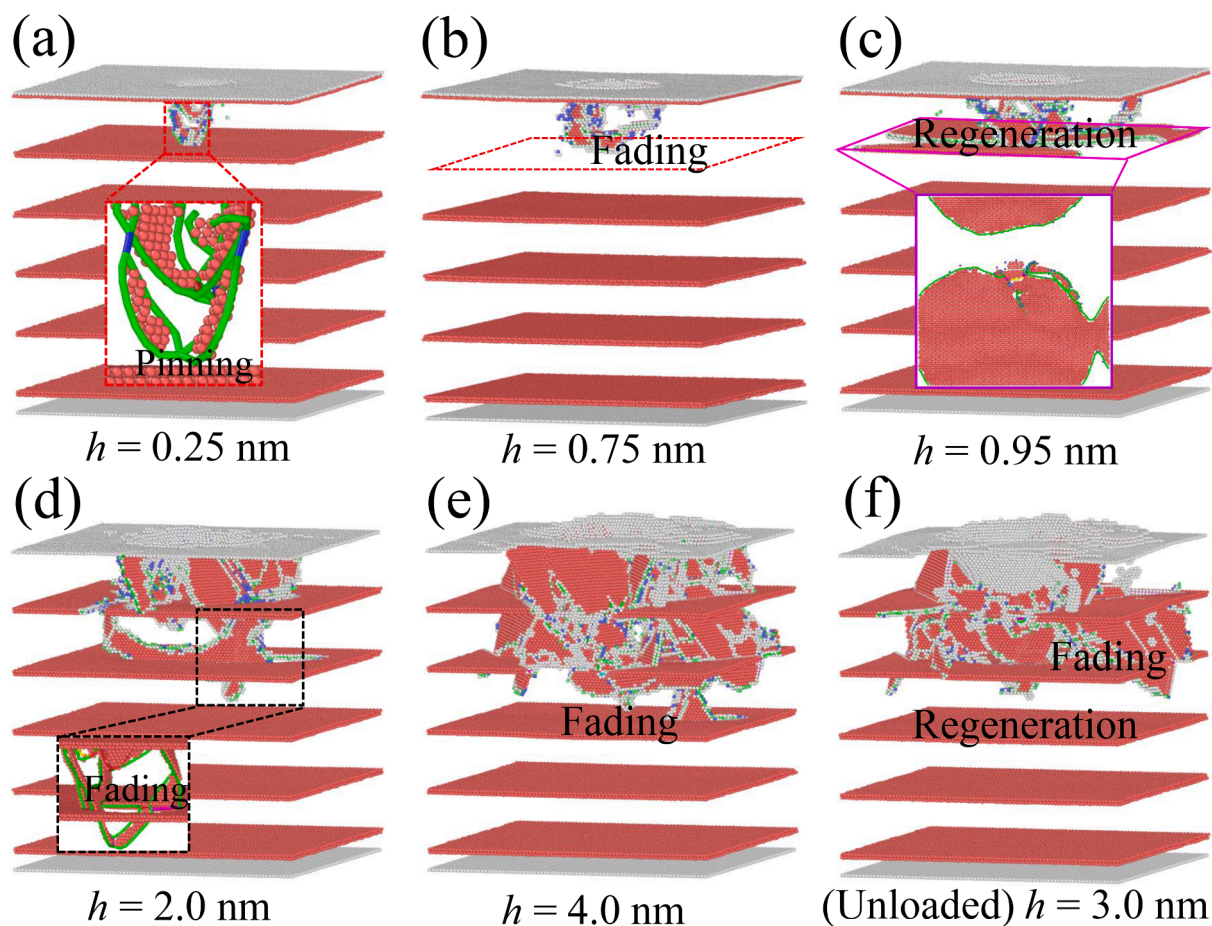
### 3.3. Deformation mechanisms of TB- $\text{Ni}_3\text{Al}$

To understand the hardening effect, dislocation activities were monitored. Fig. 5 shows atomic configurations of deformed TB- $\text{Ni}_3\text{Al}$  with a spacing of 3.9 nm during indentation. Dislocations first nucleate on indentation surface beneath the indenter and then spread inward in  $\text{Ni}_3\text{Al}$  substrate. Several  $1/6\langle 112 \rangle$  Shockley dislocations continuously grow, slip and interact, forming a  $1/2\langle 110 \rangle$  perfect dislocation to pin a small amount of  $1/6\langle 112 \rangle$  Shockley dislocations (Fig. 5a). Then, with depth increasing, several  $1/6\langle 112 \rangle$  Shockley dislocations spread down and meet the first TB layer (Fig. 5b). As dislocations move to TB, they are impeded and react with TB. Reaction brings  $1/6\langle 110 \rangle$  stair-rod,  $1/2\langle 110 \rangle$  perfect and  $1/3\langle 100 \rangle$  Hirth dislocations, accounting for the density of dislocation lines of 9.2%, 5.3% and 4.1%, respectively (see Fig. 5c). Reaction also sets off migration of TB as shown in Fig. 5d. As TB migrates downward, the pinning effect was observed above it. Dislocations participating pinning are mainly  $1/6\langle 112 \rangle$  Shockley (61.5%) and a small amount of  $1/6\langle 110 \rangle$  stair-rod,  $1/3\langle 100 \rangle$  Hirth,  $1/3\langle 111 \rangle$  Frank and  $1/2\langle 110 \rangle$  perfect. With depth increasing to 4.0 nm, dislocations move to

the second TB layer, where they are obstructed and interact with TB. Reaction of dislocations results in an SF tetrahedron in the middle of the second TB layer (see Fig. 5e). Finally, as shown in Fig. 5f, with the indenter retracting to a depth of 3.0 nm, the length of dislocation lines in  $\text{Ni}_3\text{Al}$  substrate reduces from  $5.3 \times 10^2$  to  $2.6 \times 10^2$  nm due to stress release. Meanwhile, the  $1/6\langle 112 \rangle$  Shockley dislocation loop on the second TB layer gradually contract and the SF tetrahedron is left on the second TB layer. Supplementary Movie. 1 offers structural evolution of TB- $\text{Ni}_3\text{Al}$  with the spacing of 3.9 nm during indentation process.

### 3.4. Deformation mechanisms of CSF- $\text{Ni}_3\text{Al}$

For a comparison, the microstructural evolution of a CSF- $\text{Ni}_3\text{Al}$  with a spacing of 3.9 nm is shown in Fig. 6. At a depth of 0.25 nm, several  $1/6\langle 112 \rangle$  Shockley dislocations nucleate on surface of  $\text{Ni}_3\text{Al}$  substrate and spread inward. Interaction between  $1/6\langle 112 \rangle$  Shockley dislocations leads to formation of  $1/2\langle 110 \rangle$  perfect dislocations at their junction areas. The interaction pins a small amount of  $1/6\langle 112 \rangle$  dislocations below the indenter (Fig. 6a). Then, with depth increasing, unpinned  $1/6\langle 112 \rangle$  dislocations propagate downwards and meet the first CSF. Such an activity stimulates a  $1/6\langle 112 \rangle$  Shockley dislocation loop on the CSF in-plane. Transverse propagation of the stimulated  $1/6\langle 112 \rangle$  dislocation loop causes fading of CSF. Subsequently, the entire first CSF layer is faded directly (see Fig. 6b). However, as depth increases to 0.95 nm, part of the first CSF layer is regenerated (see Fig. 6c). At this moment, due to impediment of the first CSF, all dislocations in  $\text{Ni}_3\text{Al}$  substrate exist above the first CSF layer without propagating downward. Then, with depth further increasing to 2.0 nm,  $1/6\langle 112 \rangle$  dislocations pass through



**Fig 6.** Configurations were analyzed by dislocation analysis in CSF-Ni<sub>3</sub>Al with a spacing of 3.9 nm between parallel CSFs at various indentation depths of (a) 0.25 nm, (b) 0.75 nm, c) 0.95 nm, (d) 2.0 nm, (e) 4.0 nm and (f) 3.0 nm (unloaded). Insets in (a) and (d) show structures of local dislocations. The red dashed parallelogram in (b) represents the faded first CSF. Bottom view below the first CSF layer in (c) is shown in inset with purple solid edges.

the first CSF layer and propagate downward, contacting and interacting with the second CSF layer, resulting in partial fading of the second CSF (see Fig. 6d). However, a  $1/6\langle 110 \rangle$  stair-rod dislocation is formed at the edge of the faded part of the second CSF layer (see amplified regions in Fig. 6d). The  $1/6\langle 110 \rangle$  stair-rod hinders further fading of the second CSF. With depth increasing to 4.0 nm, dislocations continue to spread, multiply, pinning and interact with each other. Meanwhile, fading and regeneration of CSFs emerge ceaselessly (Fig. 6e). Dislocations participating pinning are mainly  $1/6\langle 112 \rangle$  Shockley (66.1%),  $1/6\langle 110 \rangle$  stair-rod (11.9%), and a small amount of  $1/3\langle 111 \rangle$  Frank,  $1/3\langle 100 \rangle$  Hirth and  $1/2\langle 110 \rangle$  perfect. After retraction, the faded part of the third CSF layer is completely regenerated (Fig. 6f). Here it is worth noting that fading and regeneration of CSF are independent of the spacing. Supplementary Movie. 2 provides structural evolution of CSF-Ni<sub>3</sub>Al with the spacing of 3.9 nm.

#### 4. Discussions

As mentioned above, the volume of a plastic zone and hardness of nanostructural Ni<sub>3</sub>Al significantly depend on spacing. At the critical value of spacing, hardness approaches its maximum while the volume of a plastic zone falls to its minimum. Beyond this value, hardness follows the Hall-Petch relationship since the plastic zone is restricted by planar defects. However, the inverse Hall-Petch relationship emerges below the critical spacing because planar defects cannot constrain plastic zones. The trend of hardness is well consistent with that in hierarchically nanotwinned FCC metals [34], Cu/Ni nanotwinned multilayer films [35] and Ni<sub>3</sub>Al/Ni multilayers [36]. The discrepancy between values of

hardness mainly results from the two facts: one is pure Ni<sub>3</sub>Al and the other is the shape of a hemisphere indenter with a diameter of 10.0 nm in our work. However, the Berkovich indenter was used for Ni<sub>3</sub>Al/Ni multilayers [36]. It has been confirmed that hardness varies with the size and shape of an indenter [23]. In addition, since hardness is a measure of materials for their resisting plastic deformation, a smaller plastic zone produces a higher hardness. This explains the opposite trend between the volume of a plastic zone and hardness.

Planar defects result in hardening and softening. The former includes impediment of planar defects to propagation of dislocations, pinning of dislocations and regeneration of CSFs. The latter consists of detwinning, migration of TBs and fading of CSFs. Specifically, For TB-Ni<sub>3</sub>Al, as spacing is less than 5.2 nm, softening mechanisms, such as detwinning and migration of TBs, dominate deformation of plastic zones (see Fig. S2a–d for deformed atomic configurations in TB-Ni<sub>3</sub>Al with spacing of 0.9 nm and 6.4 nm, respectively). Beyond 5.2 nm, hardening deformation mechanisms include impediment of TBs to propagation of dislocations, pinning of dislocations at a local region. This is consistent with results measured from nanotwinned Cu [34]. However, softening and hardening mechanisms by CSFs are different from that of TBs. The critical value of spacing is 2.1 nm. Below this value, the softening mechanism results from fading of the entire layer of CSFs (see Fig. S3a and b for deformed atomic configurations of CSF-Ni<sub>3</sub>Al with a spacing of 0.9 nm). Beyond 2.1 nm, deformation is dominated by hardening mechanisms such as impediment of CSFs to propagation of dislocations, pinning of dislocations and partial regeneration of CSFs (see Fig. S3c and d for configurations of CSF-Ni<sub>3</sub>Al with a spacing of 6.4 nm at various indentation depths). Applying SFs to improve strength has been realized



in Mg alloys [37–39] and other metals [40]. Since hardness roughly increases with the increase of strength, this provides an indirect evidence for hardening materials by SFs. In contrast, SC-Ni<sub>3</sub>Al without planar defects produces a lower hardness due to lack of microstructures to offer hardening mechanisms to restrict development of plastic zones.

It is of interest to note that CSF-Ni<sub>3</sub>Al and TB-Ni<sub>3</sub>Al generate the same hardness of 18.7 GPa at a spacing of 3.0 nm (see Fig. 4a). This is because when hardening mechanisms play a role in CSF-Ni<sub>3</sub>Al, softening factors take over deformation of TB-Ni<sub>3</sub>Al, with the reduction of spacing. It is shown that, at a spacing of 3.0 nm, TBs lose control on development of a plastic zone, which undergoes a rise with the decrease of spacing. However, the volume of a plastic zone in CSF-Ni<sub>3</sub>Al still follows a reducing trend at the same spacing range. That is, competition between softening and hardening results in a better hardening effect of CSFs than TBs with a spacing below 3.0 nm, and vice versa.

## 5. Conclusions

Hardness of nanostructural Ni<sub>3</sub>Al has been investigated under nanoindentation by a series of molecular dynamics simulations, with spacing between parallel planar defects being a key variable. It is shown that, hardening can be achieved by planar defects such as CSFs and TBs with SC as a reference. The conclusions are as follows:

- (1) There is the same hardness of CSFs and TBs at a critical spacing of 3.0 nm between parallel planar defects. Below the spacing value, the hardening effect of CSFs is stronger than TBs.
- (2) Hardening factors are attributed to impediment of planar defects to propagation of dislocations, regeneration of CSFs and pinning effect resulting from the interaction between dislocations and planar defects.
- (3) Softening aspects include fading of CSFs, detwinning and migration of TBs.

These findings provide new insights into a deep understanding on deformation mechanisms of nanostructured Ni<sub>3</sub>Al and benefit its optimal design and wide applications in aerospace industries.

## 6. Data availability

The data that support the findings within this paper are available from the corresponding authors upon reasonable request.

## CRedit authorship contribution statement

**Zhiwei Zhang:** Investigation, Methodology, Data curation, Writing - original draft. **Qiang Fu:** Formal analysis. **Jun Wang:** Conceptualization, Supervision, Writing - review & editing, Funding acquisition. **Pan Xiao:** Funding acquisition, Methodology. **Fujiu Ke:** Conceptualization, Writing - review & editing. **Chunsheng Lu:** Writing - review & editing.

## Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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## Appendix A. Supplementary data

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