### **RESEARCH PAPER**



# **Experimental and numerical investigations into fow features in an intake duct for the waterjet propulsion under mooring conditions**

**Renfang Huang1 · Ruizhi Zhang2 · Yiwei Wang1,3 · Xianwu Luo4 · Lei Zhu5**

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### **Abstract**

The waterjet propulsion is widely applied in the marine vessels over 30 knots, and the intake duct is considered as an essential component that strongly relates to the propulsion performance. This paper sheds light on the fow features inside an intake duct under mooring conditions by using the particle image velocimetry (PIV) technique with three-dimensional (3D) numerical simulations. The hydraulic loss gradually increase as the fow-rate increases. According to analyses via the Bernoulli equation, the hydraulic loss is composed of the frictional head loss ( $h_f \sim V^{1.75}$ ) and the local head loss ( $h_j \sim V^{2.0}$ ). A recirculation region is observed near the duct lower wall with a high-velocity fow near the upper wall, and subsequently a shear fow presents in the horizontal straight pipe with an obvious velocity gradient. Three-dimensional simulations demonstrate that the vortex pair is very strong in the recirculation region and then it gradually decreases as the fuid fows downstream. With the fow-rate increasing, the non-uniformity at the duct outlet frstly increases to a peak and then slightly decreases, while the perpendicularity at the duct outlet dramatically decreases to a minimum and then increases. This work not only reveals some physics of the waterjet propulsion under mooring conditions, but also promotes its efficient operation.

**Keywords** Waterjet propulsion · Particle image velocimetry (PIV) · Intake duct · Waterjet pump · Mooring conditions





# **1 Introduction**

The waterjet propulsion has been widely applied in the marine vessel whose speed is over 30 knots due to its advantages such as high propulsive efficiency, good maneuverability, less vibration and noise, good anti-cavitation performance  $[1-4]$  $[1-4]$ . The intake duct is an essential component in the waterjet propulsion, since the water is inhaled through the intake duct, gets high kinetic energy from the waterjet pump, and then provides the thrust to the marine vessels. As a diversion component, about 7%–9% of the total energy is lost in the intake duct if there are unexpected fow patterns like flow separation and outflow non-uniformity  $[1,$ [2](#page-16-2), [5](#page-16-3)]. Moreover, the waterjet-hull interaction mainly occurs near the suction entrance of the intake duct, and its efect on the propulsive efficiency is over  $20\%$  [[6,](#page-16-4) [7](#page-16-5)]. Therefore, the intake duct plays an important role in the waterjet propulsion system, and many efforts have been made to investigate the intake duct from various aspects, i.e. the internal fow features, optimization design, the waterjet-hull interaction, etc.

Experimental fuid dynamics is a preferable approach to reveal physics [\[8](#page-16-6)[–10\]](#page-16-7). A planning hull test boat is used to measure the pump loading parameters, the static pressure, the ingested hull boundary layer characteristics, etc. [[11\]](#page-16-8). A scale waterjet intake duct model is mounted in a wind tunnel to study the dependence of the boundary layer thickness on the outfow quality [[12\]](#page-16-9). Results show that the thickened boundary layer would cause more extensive flow separation, and the cut-water separation fows under maneuvering conditions would choke the inlet and suppress the available maneuvering thrust [\[12](#page-16-9)]. The pressure distributions on the duct surfaces are measured by pressure tabs at three values of jet velocity ratio (JVR), and the velocity felds are measured at the symmetry plane of a prototype waterjet model via the particle image velocimetry (PIV) technique [[13\]](#page-16-10). A pair of counter-rotating vortices is visualized at the nozzle exit, and the fow inside the duct is faster near the lip than that near the upper wall [\[13](#page-16-10)]. A newly dynamometer is designed to collect the six force components and the non-uniform suction fow is generated by using a pipe bundle in the suction pipe  $[14]$  $[14]$ . The measurement results illustrate that effects of the suction non-uniformity on the energy performance and the hydrodynamic forces of the pump impeller. Early experiments are conducted in the wind tunnel by using pressure tabs and feld visualization techniques. However, the physical properties of water and air are diferent. For example, the density and viscosity of water are larger than that of air, and this causes larger drag and energy loss. Specially, the liquid water becomes vaporous water when the local pressure is lower than the saturated vapor pressure, which is known as cavitation and would cause the performance breakdown, but this cavitation phenomenon is not considered in the wind tunnel.

With the development of the computer science and technology, numerical simulation has gradually become a powerful approach for scientifc research and has been widely used in various engineering applications [\[15](#page-16-12)[–23](#page-16-13)]. Regarding the liquid water in the intake duct, internal fows are numerically studied by using the Reynolds-averaged Navier-Stokes (RANS) method together with wall functions, the calculated results achieve an acceptable accuracy and demonstrate that the infow non-uniformity is caused by the accumulating vorticity [[24\]](#page-16-14). Besides, Park et al. [\[25\]](#page-16-15) also numerically studied the fow features and the energy performance for a waterjet propulsion system by using the incompressible RANS method together with a sliding multi-block technique. Young et al. [[26\]](#page-16-16) numerically studied internal flows in a fully-coupled SES-waterjet system and the results demonstrate that the non-uniformity would cause load fuctuations and the unsteady cavitation [\[26\]](#page-16-16). This has also been confrmed by Duerr and von Ellenrieder [\[27\]](#page-16-17). Dependence of the pump performance on the non-uniform suction fow is numerically studied by Cao et al. [[28\]](#page-16-18), and results indicate that the large infow non-uniformity is characterized by a distinct swirl distortion and this would cause a dramatic drop in the pump head. Energy performance of an intake duct is numerically analyzed at various values of inlet velocity ratio (IVR), illustrating the cavitation is likely to occur at the upper side of the duct cutwater and the duct hydraulic efficiency is firstly increased and subsequently followed by a drop with an increase in IVR [[29](#page-16-19)]. Guo et al. [\[30\]](#page-16-20) conducted the self-propulsion computations of a trimaran and developed a prediction tool to obtain the capture area via tracking the streamlines upstream. The results demonstrate that the resistance increment and the waterjet thrust deduction fraction always have different signs and the total efficiency is strongly related to the ideal jet efficiency and the pump efficiency. Zhao et al.  $[31]$  numerically and experimentally investigated cavitating flow characteristics in an axial fow waterjet pump and revealed that the cavitation process not only afects the blade loading but also relates to the incidence angle at the leading edge which is responsible for the fow structures on the suction surface. Efects of the stabilizer fns on dynamics around a waterjet-propelled ship are numerically studied by model-scale and full-scale transient simulations, and the results indicate that stabilizer fns would change the turbulent boundary layer distribution around the hull and even afect the capture area of the waterjet [\[32](#page-16-22)]. The hull-waterjet interaction for a planning trimaran is numerically studied and discussed the thrust deduction and interaction efficiency in the speed range of  $0.32 < Fr<sub>L</sub>$  $< 2.87$  [[33\]](#page-16-23).

Besides, the numerical simulation is widely applied to optimize the duct since it can not only rapidly give an acceptable result but also save the manufacturing cost as well as time. Effects of the inlet grids on the duct performance are numerically studied by comparing the duct with no grids, three grids and eight grids, and the results indicate that the inlet grids would cause a decrease in the performance of the duct and the waterjet propulsion [[34\]](#page-16-24). The optimal setting angle of the grids is suggested to be 5° based on Luo's research [[35\]](#page-16-25), and the duct lip is recommended to be a more forward position with a sharper confguration for a better hydrodynamic performance based on the investigation by Liu and Huang [[36\]](#page-16-26). The inclination angle of the intake duct is discussed via numerical simulations and the results show that the duct efficiency is gradually decreased as the inclination angle increases [[37](#page-16-27), [38](#page-16-28)]. A parametric design method is proposed to design the intake duct and then the computational fuid dynamics (CFD) technique is applied to predict the duct performance such as the uniformity, fow separations, energy performance and hydraulic loss [[39](#page-16-29)]. Subsequently, the non-dominated sorting genetic algorithm-II (NSGA-II) is incorporated with the parametric design method and CFD technique to conduct the multi-objective optimization for the intake duct  $[1]$  $[1]$  $[1]$ . Guo et al.  $[40]$  $[40]$  $[40]$  conducted a multi-objective optimization of a waterjet-propelled trimaran with considering the waterjet-hull interaction, which is decomposed into the optimization of the waterjet system, the global hull shape, the local hull shape and the arrangement of the waterjet.

A brief review above demonstrates that the energy performance and internal fow features inside intake duct have been studied at specifed vessel speeds by using both numerical and experimental approaches. Besides, the intake duct is also operated under mooring conditions (zero vessel speed) when the marine vessel docks at the pier. However, we still have inadequate understandings on the whole fow features in the intake duct under such mooring conditions. In this paper, a water tank is built up and used to conduct experiments for a duct model under mooring states. Based on PIV observations, the numerical simulation is adopted to illustrate three-dimensional fow features in the model-scale duct. This paper is organized as follows. The experimental approach and numerical simulation method are described in Sects. [2](#page-2-0) and [3](#page-5-0), respectively. Section [4](#page-6-0) discusses the hydraulic loss, the planar velocity felds obtained by experiments and three-dimensional fow patterns calculated by numerical simulation. Last is the conclusions.

### <span id="page-2-0"></span>**2 Experimental approach**

The experiments are conducted to capture the velocity felds inside a model-scale duct and to measure the pressures under mooring conditions. The study is conducted at China Institute of Water Resources and Hydropower Research. The experimental apparatus is shown in Fig. [1,](#page-3-0) mainly including a water tank, an experimental model, PIV system and measurement system.

The water tank is 1236 mm  $\times$  524 mm  $\times$  650 mm (length  $\times$  width  $\times$  height) with a free surface. The water is driven by an ISW65-100IA centrifugal pump with the rated discharge of  $44 \text{ m}^3/\text{h}$  and the rated head of 10 m. A ball valve is mounted at the pump outlet pipe to adjust the fow-rate during the operation. Note that there are small ball valves at the bottom of the pump, the inlet pipe and the outlet pipe to discharge the residual water after each experimental run.

The experimental model is an intake duct, which is made of the photosensitive resin composites by 3D printing technique and polish to a smooth fnish. The scale of the duct model is 1:4.88. Figure [2](#page-3-1) shows geometrical parameters of the intake duct, and the characteristic diameter is  $D = 50$ mm. The inhaling water flows towards the  $+z$  direction. The vertical and spanwise directions are designated by *y*-axis and *x*-axis, respectively.

Two YH203 pressure transducers are employed on the duct upper wall to measure the pressures under various fowrates. A YH-3051DP diferential pressure transducer is used to measure the diferential pressure between the pump outlet and inlet, and then the actual pump head is calculated. The pressure transducers are calibrated before experiments by using a piston gauge according to the JJG 882-2004 pressure transducer standard (PTS). The uncertainty of the YH203 pressure transducers is  $\pm 0.5\%$ , its frequency response range is 0–10 kHz with its natural frequency of  $1 \times 10^6$  Hz. The uncertainty of the YH-3051DP diferential pressure transducer is  $\pm 0.2\%$ . The flow-rate is measured by an AXF065G-E2AL1S-BD11-41B electromagnetic fowmeter, and it is installed at the pump outlet pipe. The uncertainty of the electromagnetic flowmeter is  $\pm 0.35\%$ .

The PIV system is composed of a computer, laser and charge coupled device (CCD) cameras. A Nd: YAG doublecavity laser is used to illuminate the fow feld with the output energy of 200 mJ and wavelength of 532 nm. The laser sheet is overlapped with the midplane of the intake duct, which is generated by a laser probe from the bottom up. The thickness of the laser sheet is about 2 mm. The tracer particles in water are glass hollow spheres with a mean diameter of 10 μm. The particle traceability is evaluated by the Stokes number  $St = \tau_p/\tau_f$ , where  $\tau_p$  is the particle response time and  $\tau_f$  is the turbulence time scale of water. *St* < 1 indicates the particle traceability is good enough to visualize the flow





**Fig. 1** Experimental apparatus for the intake duct including a water tank, particle image velocimetry (PIV) system and measurement system: **a** schematic diagram and **b** the on-site facility

<span id="page-3-0"></span>

<span id="page-3-1"></span>**Fig. 2** Intake duct model and the pressure transducer arrangement: **a** top view and **b** side view (unit: mm)

features. In our PIV experiments, the corresponding Stokes number is  $St = 0.0049 - 0.2165$ . The *St* values are smaller than 1, demonstrating that the hollow glass spheres meet the *St* requirement of tracer particles.

Two imager LX 8M CCD cameras (12 bit digital) are used to capture the particle images with the spatial resolution of  $3312 \times 2488$  pixels. Since the light intensity is quite diferent inside and outside the duct, so the fow feld of the midplane is divided into two regions to obtain high spatialresolution particle images, i.e. Region 1 in red dash line and Region 2 in blue dash line as shown in Fig. [3a](#page-4-0). Therefore, Region 1 focuses on the fow feld outside the duct, and Region 2 focuses on the flow features inside the duct. The planar flow fields in two regions have been measured separately with the flow-rate ranging from 2 to  $25 \text{ m}^3/\text{h}$ . With the fow-rate increasing, the fow velocity becomes higher, the particle movement between two light pulses is increased, so it is necessary to gradually decrease the parameter  $\sigma$  (the time interval between two laser pulses) to avoid the tracer particles moving too much between two light pulses. The purpose is to ensure the accuracy of PIV measurement. Experimental conditions and corresponding parameter *σ* are listed in Table [1.](#page-4-1) The distance from the measurement plane to the cameras is around 500 mm as illustrated in Fig. [3](#page-4-0)b.

The overall procedure is described as follows:

- 1. Degassing. Since the air in water can be illuminated and recorded as seeding particles, this would cause the experimental error. To avoid the experimental error caused by the air, it is necessary to eliminate the air from the experimental system at the beginning of each test.
- 2. Calibration. A calibration plate is used to calculate the relationship between the image coordinates and the physical coordinates, where the black dots with an interval of ten millimeters are located on a white background. The plate shape fts well with the midplane of the intake duct.

<span id="page-4-1"></span>

- 3. Particle image recording. Cameras are set as the doubleframe and double-pulse mode. The sampling rate is 100 Hz, and 400 frames are captured at each fow-rate. One pulse is set to 60% of the rated energy, and another pulse is set to 75%. Meanwhile, pressure data measured by the pressure transducers, and particle images are collected and stored in a computer.
- 4. Processing. As shown in Fig. [4](#page-5-1)a, the light intensity near the duct surface wall is much higher than that of the background, and this causes a bad velocity calculation. To solve this issue, a time flter is adopted to preprocess those particle images. The distribution of the minimum light intensity is calculated among *n* source images (*n* is filter length, herein  $n = 5$ ), and the processed particle image is obtained by subtracting the corresponding minimum value from each raw image. Figure [4b](#page-5-1) shows the particle image processing with the time flter. The light intensity is approximately the same on the particle image. The stereo cross-correlation method together with the multi-pass iterations is used to calculate the velocity felds. The initial interrogation window is 64  $\times$  64 pixels, the final interrogation window is 32  $\times$  32 pixels, and the overlap of both interrogations are 50%. Therefore, we can obtain about 4700 velocity vectors





<span id="page-4-0"></span>**Fig. 3 a** Measured regions for the intake duct and **b** the camera confgurations (unit: mm)



<span id="page-5-1"></span>**Fig. 4** Particle image: **a** without the time flter and **b** with the time flter

with 1.76 mm spacing for "Region 1" and 1600 velocity vectors for "Region 2". Take  $Q = 10$  m<sup>3</sup>/h for instance, the typical particle image displacement is 3.5 pixel, the maximum velocity gradient is 0.07 pixels/pixel, and the general velocity gradient is 0.02 pixels/pixel. Therefore, the uncertainty in the planar velocity component is about 6%.

### <span id="page-5-0"></span>**3 Numerical simulation method**

Numerical simulation is used to give a better understanding for the three-dimensional fows inside the intake duct. The continuity and momentum equations are expressed as follows,

$$
\frac{\partial \rho}{\partial t} + \frac{\partial (\rho u_j)}{\partial x_j} = 0,\tag{1}
$$

$$
\frac{\partial(\rho u_i)}{\partial t} + \frac{\partial(\rho u_i u_j)}{\partial x_j} = -\frac{\partial p}{\partial x_i} + \frac{\partial}{\partial x_j} \left[ (\mu + \mu_t) \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \right],
$$
\n(2)

where  $\rho$  is the density,  $p$  is the pressure,  $u_i$  is the *i*-th velocity, *u<sub>j</sub>* is the *j*-th velocity,  $\mu$  and  $\mu$ <sub>t</sub> is the laminar and turbulent eddy viscosity. The re-normalisation group (RNG) *k-ε* turbulence model is adopted to closure the governing equations, which provides an analytically-derived diferential formula for eddy viscosity and is suitable for both high-Reynolds number flows and low-Reynolds number flows [[41](#page-17-1)].

The computational domain is made up of the intake duct, the large water tank, the inlet pipe and the outlet pipe. Present numerical simulations are not considered effects of the centrifugal pump. When it comes to the boundary

conditions, the mass-fow-rate is set at the inlet, and the averaged static pressure is set at the outlet with the value measured from experiments. Free surface is set at the top of the water tank. No-slip wall is set at the other solid walls and the scalable wall function is used to solve the near wall flows. Three-dimensional flows inside the intake duct are calculated using the commercial software ANSYS CFX. Water at  $25 \text{ °C}$  is used as the liquid in the simulation, whose density is 997 kg/m<sup>3</sup> and dynamic viscosity is  $8.899 \times 10^{-4}$ kg·m<sup>-1</sup>·s<sup>-1</sup>. The convergence residual is less than  $1 \times 10^{-5}$ .

Hybrid grids are meshed for the whole computational domain. Unstructured grids are meshed in the intake duct and structured grids are meshed in the other computational parts. Mesh details around the intake duct are shown in Fig. [5.](#page-6-1)

Three grids in the intake duct are created with a constant grid refinement ratio  $r = 1.3$  in all three directions, the total element in the whole computational domain are quantifed in Table [2.](#page-6-2) The discretization uncertainty is evaluated with the factor of safety (FS) method [\[42](#page-17-2)] by monitoring the nonuniformity ( $\xi$ ) and perpendicularity ( $\varphi$ <sub>n</sub>) at the duct outlet, i.e. Plane 6. The non-uniformity  $\xi$  and perpendicularity  $\varphi_p$ are defined in Eqs. [\(3](#page-5-2)) and ([4\)](#page-5-3), where  $V<sub>z</sub>$  is the velocity in *z*-direction,  $\bar{V}_z$  is the averaged velocity component in *z*-direction,  $V_{xy}$  is the velocity component at *xy*-plane. Plane 6 is the outlet plane of the intake duct, as shown in Fig. [6](#page-6-3)

<span id="page-5-2"></span>
$$
\xi = \frac{1}{Q} \int_{\text{dA}} \left| V_z - \overline{V_z} \right| \text{dA},\tag{3}
$$

<span id="page-5-3"></span>
$$
\varphi_{\rm p} = \frac{1}{Q} \int_{\rm dA} V_{\rm z} \left[ 90^{\circ} - \arctan\left(\frac{V_{\rm xy}}{V_{\rm z}}\right) \right] \mathrm{d}A. \tag{4}
$$



<span id="page-6-1"></span>**Fig. 5** Mesh for the intake duct

<span id="page-6-2"></span>**Table 2** Discretization uncertainty of non-uniformity (*ξ*) and perpendicularity  $(\varphi_p)$  at the duct outlet, i.e. Plane 6

Mesh	Grid quantities		$\varphi_{\rm n}$
Fine	2.969.402	79.769	64.2272
Middle	2.118.331	79.2583	64.7303
Coarse	1,917,983	80.1958	65.0632



<span id="page-6-3"></span>**Fig. 6** Cross-section positions of the intake duct

As shown in Table [2,](#page-6-2) the uncertainty estimated by FS method is 7.57% for the non-uniformity and 9.26% for the perpendicularity, demonstrating that the simulation results are not sensitive to the grid resolution. Note that further grid refnement will lead to substantial increasing of computational cost and simulation instability [[43](#page-17-3)]. Thus, the middle mesh is determined as the fnal mesh with 2,118,331 elements.



<span id="page-6-4"></span>**Fig. 7** Experimental conditions at **a** Run#1 and **b** Run#2

# <span id="page-6-0"></span>**4 Results and discussions**

### **4.1 Hydraulic loss in the intake duct**

As depicted in Fig. [7,](#page-6-4) the experimental conditions are conducted at two runs. The fow felds in Region 1 are measured

at Run#1 with  $Q = 2{\text -}25$  m<sup>3</sup>/h, and the flow fields in Region 2 are measured at Run#2 with  $Q = 2-25$  m<sup>3</sup>/h. The operation conditions are almost the same at both Run#1 and Run#2. The pump head  $(H)$  is gradually decreased as the flow-rate (*Q*) increases. The maximal standard deviation of the pump head is 0.091 m at Run#1 and 0.096 m at Run#2. Therefore, the entire experimental apparatus generally runs stably with high reliability during  $Q = 2-25$  m<sup>3</sup>/h.

Figure [8a](#page-7-0) shows the measured and simulated pressures at various fow-rates. The measured pressure at Run#1 is the same with that at Run#2. When compared with the numerical simulation, the measured  $p_1$  is in pretty good accordance with the simulated  $p_1$ . On the other hand, there are discrepancies in  $p<sub>2</sub>$  between the numerical simulation and the experiment, although the variation tendency is the same. Both  $p_1$  and  $p_2$  are gradually decreased as the flow-rate  $(Q)$ increases. Applying the Bernoulli equation to  $p_1$  and  $p_2$ , it comes to Eq. ([5\)](#page-7-1), where *V*, *p*, *z* is the fuid velocity, pressure, height, respectively;  $h_w$  is the hydraulic loss, including the frictional head loss  $h_f$  and the local head loss  $h_j$ ; *a* is the correction factor for the kinetic energy,  $a = 1.05-1.10$ ; subscript



<span id="page-7-0"></span>**Fig. 8** Measured and simulated pressures at **a** pressure transducer 1 and **b** pressure transducer 2

1 and 2 correspond to the location of pressure transducer 1 and pressure transducer 2

<span id="page-7-1"></span>
$$
z_1 + \frac{p_1}{\rho g} + \frac{a_1 V_1^2}{2g} = z_2 + \frac{p_2}{\rho g} + \frac{a_2 V_2^2}{2g} + h_w.
$$
 (5)

Therefore,  $\Delta p = p_1 - p_2$  is the pressure difference between the two pressure transducers, including the diference in the potential energy, the kinetic energy and the hydraulic loss, as expressed in Eq. ([6\)](#page-7-2),

$$
\Delta p = (p_1 - p_2) = \rho g (z_2 - z_1) + \rho \left( \frac{a_2 V_2^2}{2} - \frac{a_1 V_1^2}{2} \right) + h_w.
$$
\n(6)

<span id="page-7-2"></span>The Reynolds numbers range in  $1.39 \times 10^4$ – $1.77 \times 10^5$ , the relative roughness factor of the material and the manufacturing process is around  $3 \times 10^{-4}$ . Based on previous studies [\[44](#page-17-4)], the fow inside the intake duct is turbulent and the frictional head loss  $h_f$  is proportional to  $V^{1.75}$ , i.e.,  $h_f \sim V^{1.75}$ . Besides, the local head loss  $h_j$  is proportional to the square of the flow-rate, so it can be written as  $h_j \sim V^{2.0}$ . Therefore, the hydraulic loss  $h_w$  is made up of the frictional head loss  $(h_f \sim V^{1.75})$  and the local head loss  $(h_j \sim V^{2.0})$ .

Ignore the position diference, Eq. [\(6](#page-7-2)) is simplifed as,

$$
\Delta p \approx \rho \left( \frac{a_2 V_2^2}{2} - \frac{a_1 V_1^2}{2} \right) + h_w \to V^2 + V^{1.75}.
$$
 (7)

Figure [9](#page-7-3) shows the variations of pressure difference  $(\Delta p)$  over the flow-rate (*Q*). With increasing the flow-rate, the pressure difference  $(\Delta p)$  by experiments is gradually increased, which can be ftted by Eq. ([8\)](#page-8-0) and plotted in blue curve in Fig. [9](#page-7-3). The theoretical predictions by Eq. [\(8](#page-8-0)) is very close to the experimental data, and the root mean square (RMS) between the measured data and the theoretical predicted value is 9.4062



<span id="page-7-3"></span>**Fig. 9** Variations of pressure diference (Δ*p*) at Run#1 and the hydraulic loss  $h_w$  over the flow-rate (*Q*)

$$
\Delta p = 9.142Q^2 - 4.412Q^{1.75} + C. \tag{8}
$$

#### **4.2 Flow features at the midplane by PIV technique**

As "Region 1" and "Region 2" are measured in two experiments, it is necessary to check whether velocity felds in the two regions match well or not. Herein, velocity profle on line 1 is extracted from the PIV measurement, noting that line 1 is located in the overlap region of the two regions (Fig. [3](#page-4-0)). Besides, the simulated velocity on line 1 is used for comparisons. As shown in Fig. [10,](#page-8-1) the results indicate that the high velocity near the upper wall and the lower velocity near the lip of intake duct are obtained by two measurements as well as present numerical simulations. Basically, it is confrmed that velocity felds in the two regions can match well, and the numerical simulation performs well to capture the velocity profle on line 1.

Figure [11](#page-9-0) shows the time-averaged velocity distributions measured by the PIV technique in Region 1. When the flowrate is varied from  $Q = 2 \text{ m}^3/\text{h}$  to  $Q = 25 \text{ m}^3/\text{h}$ , the flow structure is almost similar in Region 1. The fuid is mainly inhaled from the lower left of the intake duct, and the fuid velocity presents a uniform distribution outside the duct, which is also reported in Ref.  $[25]$  $[25]$ . The fluid flows into the duct due to its guidance effects. A flow separation is represented as a low-velocity zone near the duct lip. As a result, the effective flow area inside the intake duct is reduced, and the fuid near the duct upper wall is accelerated with an obvious velocity gradient from the duct upper wall towards the lower wall. Due to the fuid viscosity, the high-velocity fuid drives the low-velocity fuid and moves along the streamwise direction together.

Figure [12](#page-10-0) shows time-averaged velocity distributions measured by the PIV technique in Region 2. The flow inside the intake duct can be completely illustrated since Region 2 includes the elbow section of the duct and the horizontal



<span id="page-8-1"></span>**Fig. 10** Velocity comparisons on line 1 ( $Q = 10 \text{ m}^3/\text{h}$ )

<span id="page-8-0"></span> $\beta$ <sup>2</sup><sub>*p*</sub> straight section. As shown in Fig. [12](#page-10-0), there is another lowvelocity zone near the pressure transducer 1, whose velocity is much larger than that near the duct lip. This may be caused by the impact of the upper wall on the fuid when the water fows through the elbow. Besides, the low-velocity separation fow and the high-velocity fow are clearly observed by the PIV technique. As the fuid further fows downstream, the fow separation disappears and meanwhile a shear fow exists in the horizontal straight section with an obvious velocity gradient from the duct upper wall towards the lower wall. This indicates the intake duct is characterized by the outfow non-uniformity which strongly afects the pump performance at the downstream based on the previous investigation [[18\]](#page-16-30) .

Relative vorticity fields  $(\Omega'_x)$  in Region 2 are illustrated in Fig. [13](#page-10-1). In the range of  $Q = 2{\text -}25$  m<sup>3</sup>/h, the vorticity features stay unchanged in Region 2. The separation fow presents very low vorticity, and there is positive-vorticity zone above the separation fow, which forms a vortex pair near the duct lip. The zone of the vortex pair is gradually increased with the fow-rate. Besides, the vorticity is close to zero near the upper wall, indicating that the secondary fow along *x*-axis is very small near the duct upper wall.

The normalized helicity  $(H_n)$  is introduced to analyze the interaction between the vorticity and the velocity. It is defined in Eq. [\(9\)](#page-8-2), where  $\Omega$  is the vorticity,  $\Omega = \nabla \times V$ ,  $H_n$ is the normalized helicity ranging from  $-1$  to  $+1$ . If the normalized helicity is positive, the vorticity and the velocity is in the same direction, so the vortex is enhanced. In contrast, the negative helicity demonstrates the vorticity and the velocity is in opposite direction, so the vortex is suppressed. As shown in Fig. [14,](#page-11-0) the normalized helicity presents a similar distribution with increasing the fow-rate. The normalized helicity is positive near the upper wall, while it has negative values in the middle of the flow passage, demonstrating the vortex is promoted along with the water suction process and this will be depicted from the three-dimensional perspective in Sect. [4.3](#page-8-3)

<span id="page-8-2"></span>
$$
H_{\rm n} = \frac{V \cdot \Omega}{|V||\Omega|}.\tag{9}
$$

### <span id="page-8-3"></span>**4.3 Simulated fow felds inside the intake duct**

Based on the pressure analysis in Fig. [8](#page-7-0), the simulated pressure is in good agreement with the experiments. There is a small discrepancy in the  $p<sub>2</sub>$  value between simulations and experiments, but it is permitted in engineering practices. The calculated flow fields are shown in Fig. [15](#page-12-0) and compared with the PIV results. It is indicated the numerical simulation can well predict those fow features including the velocity gradient inside the duct, the separation fow near



<span id="page-9-0"></span>**Fig.** 11 Time-averaged velocity distributions measured by the PIV technique in Region 1. **a**  $Q = 2$  m<sup>3</sup>/h, **b**  $Q = 6$  m<sup>3</sup>/h, **c**  $Q = 10$  m<sup>3</sup>/h, **d**  $Q = 14$ m<sup>3</sup>/h, **e**  $Q = 20$  m<sup>3</sup>/h, **f**  $Q = 25$  m<sup>3</sup>/h

the lower wall and the high-velocity fow near the upper wall, and those features are in good accordance with those observed in experiments. Both the numerical simulation and the PIV approach mutually demonstrate the fow patterns at the midplane of the intake duct as shown in Fig. [16](#page-12-1). The fuid is mainly inhaled from lower left side below the intake duct. Subsequently, it strikes the duct upper right wall and separates to form two streams with a stagnation point. Two streams are in the opposite directions, one is drawn into the duct and the other continually flows towards the right side. The drawn flow is separated into a recirculation region near the lower wall and a high-velocity fow near the upper wall, and finally forms a shear flow in the horizontal straight pipe with an obvious velocity gradient.

The three-dimensional fows inside the duct are depicted at fve cross-sections in Fig. [6.](#page-6-3) Plane 1 is near the suction inlet; Plane 4 is around the elbow position and Plane 5 is in the horizontal straight pipe. The velocity distributions



<span id="page-10-0"></span>**Fig. 12** Time-averaged velocity distributions measured by the PIV technique in Region 2. **a**  $Q = 2$  m<sup>3</sup>/h, **b**  $Q = 6$  m<sup>3</sup>/h, **c**  $Q = 10$  m<sup>3</sup>/h, **d**  $Q = 14$ m<sup>3</sup>/h, **e**  $Q = 20$  m<sup>3</sup>/h, **f**  $Q = 25$  m<sup>3</sup>/h



<span id="page-10-1"></span>**Fig. 13** Relative vorticity fields  $(Q'_x)$  in Region 2. **a**  $Q = 2 \text{ m}^3/\text{h}$ , **b**  $Q = 10 \text{ m}^3/\text{h}$ , **c**  $Q = 16 \text{ m}^3/\text{h}$ , **d**  $Q = 25 \text{ m}^3/\text{h}$ 



<span id="page-11-0"></span>**Fig. 14** Normalized helicity  $(H_n)$  distributions in Region 2. **a**  $Q = 2 \text{ m}^3/\text{h}$ , **b**  $Q = 10 \text{ m}^3/\text{h}$ , **c**  $Q = 16 \text{ m}^3/\text{h}$ , **d**  $Q = 25 \text{ m}^3/\text{h}$ 

and streamlines at various cross-sections are depicted in Fig. [17.](#page-13-0) There is a clearly velocity gradient from the upper wall towards the lower wall, and the velocity distribution is axisymmetric at those cross-sections. The streamlines at Plane 1 demonstrate that the fow is mostly drawn into the duct from the lower left side. Due to the existence of the recirculation region in the inclined straight section, a vortex pair is observed at Plane 3. Subsequently, when the fow strikes the upper wall in the elbow section, two vortex pairs are observed at Plane 4, and then the fow is very complex at Plane 5. The vortex pair is very strong in the recirculation region and then it gradually decreases along with the fuid flowing downstream.

The outflow quality is quantified by the non-uniformity *ξ* and perpendicularity *φ*p. Figure [18](#page-14-0) shows the variations of non-uniformity and perpendicularity at the duct outlet (i.e. Plane 6). As the fow-rate increases, the non-uniformity gradually increases, reaches a peak at  $Q = 10 \text{ m}^3/\text{h}$  and then shows a very slight decrease. The non-uniformity represents the diference between the local *z*-velocity and the averaged *z*-velocity, indicating the velocity fuctuations in *z*-direction. As shown in Fig. [19,](#page-14-1) fuctuations of the *z*-velocity component present high values at the lower part of Plane 6 and the high-value region is enlarged from  $Q = 2$  m<sup>3</sup>/h to  $Q =$  $10 \text{ m}^3$ /h. From Fig. [19](#page-14-1)f-h, the velocity difference shows a similar distribution, causing a similar non-uniformity.

Figure [20](#page-15-0) shows the distributions of  $V_{xy}/V_{z}$  at the duct outlet (i.e. Plane 6), There is an increasing high-value region of *xy*-velocity component  $(V_{xy}/V_z)$  from  $Q = 2$  m<sup>3</sup>/h to  $Q = 8$ m<sup>3</sup>/h, and the distribution is similar during  $Q = 10-25$  m<sup>3</sup>/h. The angle  $(90^{\circ}-\arctan(V_{xy}/V_{z}))$  is shown in Fig. [21.](#page-15-1) The angle of 90° indicates that the local velocity is perpendicular to Plane 6. The red region in Fig. [21](#page-15-1) corresponding to the large angle (i.e., 90°−arctan (*V*xy/*V*z)) gradually decreases to a minimum at  $Q = 6$  m<sup>3</sup>/h and then exhibits similar distributions during  $Q = 10-25$  m<sup>3</sup>/h. As a result, the perpendicularity at Plane 6 decreases firstly to a minimum value at  $Q = 6$ m<sup>3</sup>/h and then gradually increases from  $Q = 10$  m<sup>3</sup>/h to  $Q =$  $25 \text{ m}^3/\text{h}$ , as depicted in Fig. [18](#page-14-0).

### **5 Concluding remarks**

The intake duct is essential in the waterjet propulsion system, which inhales water from the hull bottom and provide it to the waterjet pump. The intake duct is strongly connected with the performance of the waterjet pump and even the complete waterjet propulsion system. This paper aims to shed light on the internal flow features inside the intake duct and reveal the hydraulic loss mechanism under the mooring conditions (zero vessel speed). The planar velocity felds are measured at the duct midplane by using the PIV technique,



<span id="page-12-0"></span>**Fig. 15** Comparisons of the velocity fields obtained by the PIV technique (left) and the numerical simulations (right). **a**  $Q = 2$  m<sup>3</sup>/h, **b**  $Q = 10$ m<sup>3</sup>/h, **c**  $Q = 16$  m<sup>3</sup>/h, **d**  $Q = 25$  m<sup>3</sup>/h



<span id="page-12-1"></span>**Fig. 16** Flow patterns at the midplane of the intake duct ( $Q = 16$  $m^3/h$ )

pressures on the duct upper wall are collected through two pressure transducers, and then three-dimensional fow patterns are simulated by using the RNG *k*-*ε* turbulence model with the scalable wall function. Based on analyses of the flow features at the midplane and various cross-sections, some conclusions can be drawn:

(1) As the fow-rate increases, the hydraulic loss is gradually increased. According to analyses via the Bernoulli equation, the hydraulic loss  $h_w$  is composed of the fric-



<span id="page-13-0"></span>**Fig.** 17 Velocity fields and streamlines at Plane 1–Plane 5  $(Q = 16 \text{ m}^3/\text{h})$ . **a** Plane 1, **b** Plane 2, **c** Plane 3, **d** Plane 4, **e** Plane 5

tional head loss ( $h_f \sim V^{1.75}$ ) and the local head loss ( $h_j \sim$ *V*2.0).

(2) Both experimental measurements and numerical simulations mutually demonstrate the fow features at the duct midplane. Outside the intake duct, the fuid is mainly inhaled from lower left side below the intake duct. Subsequently, the fuid strikes the hull upper right wall, coming into two streams with a stagnation



<span id="page-14-0"></span>**Fig. 18 a** Non-uniformity and **b** perpendicularity at the duct outlet, i.e. Plane 6

is drawn into the duct and the other continually moves towards the right side. Inside the intake duct, the suction flow is separated into a recirculation region near the duct lower wall and a high-velocity fow near the upper wall. Finally, a shear flow presents in the horizontal straight pipe with an obvious velocity gradient.

- (3) The velocity distribution is axisymmetric at fve crosssections. A vortex pair is observed in the inclined straight section due to the existence of the recirculation region. Subsequently, when the fow strikes the duct upper wall, two vortex pairs are observed in the elbow, and then the fow is strongly turbulent in the horizontal straight pipe. Three-dimensional numerical results demonstrate that the vortex pair is very strong in the recirculation region and then it gradually decreases as the fuid fows downstream.
- (4) With the fow-rate increasing, the non-uniformity at the duct outlet gradually increases to a peak at  $Q = 10 \text{ m}^3/\text{h}$ and then slightly decreases during  $Q = 10-25$  m<sup>3</sup>/h. Besides, the perpendicularity at the duct outlet dramatically decreases to a minimum at  $Q = 6$  m<sup>3</sup>/h and then increases as the fow-rate increases.



<span id="page-14-1"></span>Fig. 19 Fluctuations of z-velocity component  $(V_z - \overline{V_z})$  at the duct outlet, i.e. Plane 6. a  $Q = 2$  m<sup>3</sup>/h, b  $Q = 4$  m<sup>3</sup>/h, c  $Q = 6$  m<sup>3</sup>/h, d  $Q = 8$ m<sup>3</sup>/h, **e**  $Q = 10 \text{ m}^3$ /h, **f**  $Q = 16 \text{ m}^3$ /h, **g**  $Q = 20 \text{ m}^3$ /h, **h**  $\dot{Q} = 25 \text{ m}^3$ /h

point. Two streams are in the opposite directions, one



<span id="page-15-0"></span>Fig. 20 Distributions of xy-velocity component  $(V_{xy}/V_z)$  at the duct outlet, i.e. Plane 6. a  $Q = 2$  m<sup>3</sup>/h, b  $Q = 4$  m<sup>3</sup>/h, c  $Q = 6$  m<sup>3</sup>/h, d  $Q = 8$  m<sup>3</sup>/h, **e**  $Q = 10 \text{ m}^3/\text{h}$ , **f**  $Q = 16 \text{ m}^3/\text{h}$ , **g**  $Q = 20 \text{ m}^3/\text{h}$ , **h**  $Q = 25 \text{ m}^3/\text{h}$ 



<span id="page-15-1"></span>Fig. 21 Distributions of the angle (90°-arctan( $V_{xy}/V_2$ )) at the duct outlet, i.e. Plane 6. a  $Q = 2$  m<sup>3</sup>/h, b  $Q = 4$  m<sup>3</sup>/h, c  $Q = 6$  m<sup>3</sup>/h, d  $Q = 8$  m<sup>3</sup>/h, **e**  $Q = 10 \text{ m}^3/\text{h}$ , **f**  $Q = 16 \text{ m}^3/\text{h}$ , **g**  $Q = 20 \text{ m}^3/\text{h}$ , **h**  $\dot{Q} = 25 \text{ m}^3/\text{h}$ 

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