



# High-cycle and very-high-cycle fatigue lifetime prediction of additively manufactured AlSi10Mg via crystal plasticity finite element method

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## ABSTRACT

The effects of defects and building directions in additive manufactured AlSi10Mg on its high-cycle fatigue and very-high-cycle fatigue performance are studied based on crystal plasticity finite element (CPFE). Among the three models provided in this work, the results of model 2 ( $N_{p2}$ ) are in good agreement with the experimental ones. It is found the fatigue life of the sample with defects are much lower than that without defects.  $0^\circ$  specimens have a better fatigue performance than  $90^\circ$  ones. This work is beneficial in determining the fatigue lifetime and helps to improve the fatigue behavior of AlSi10Mg.

## 1. Introduction

Aluminium (Al) and its alloys are characterized by their light weight, high strength, corrosion resistance, and good weldability, making them suitable for a range of applications in industries such as automotive, aerospace, machinery and tooling, defence, and construction [1,2]. Engineering components comprising Al alloys are traditionally fabricated by processes such as casting, forging, extrusion, and powder metallurgy [3]. In recent years, with the development of additive manufacturing (AM) technologies, aluminium–silicon-based alloys (Al–Si), specifically AlSi10Mg, owing to fabricability, have been fabricated by the selective laser melting (SLM) process, which is an AM technology [4,5].

SLM technologies are more environmentally friendly compared to traditional manufacturing processes, due to their rapid manufacturing processes, high material utilization and potential for a nearly 50% reduction in weight. However, the inherent defects resulting from the SLM process are inevitable. Thus SLM technology, despite its enormous potential, introduces uncertainty in the mechanical performance of the parts, which prohibits the use of these materials in safety-critical components [6,7]. Particularly, the defects resulting from SLM processes can induce crack initiation and thus significantly reduce the fatigue properties of the samples [8–11]. Thus, many researchers have considered the effects of surface roughness, AM process parameters, heat treatment processes and building directions on fatigue performance [12–15].

Previous studies have indicated that the size, location, and shape of defects are essentially responsible for the behavior of high-cycle fatigue (HCF) data of AM metals [16,17]. Generally, larger defects on or beneath the surface are more likely to drive fatigue failure as a result of concentrating high local stress. In such case, the fatigue strength is mainly governed by the largest defect within the surface volume [13,18], while excluding the collaborative effect of residual stress and surface quality [19]. And many factors can affect the defect population and its size: in particular, the platform heating [20], the scanning strategy and the process [21,22] and, above all, the part orientation with respect to the building direction [23]. While low-temperature heat treatments do not affect defect size [24].

Besides, AM building directions had an obvious impact on the fatigue crack propagation resistance and fatigue limits of the SLM-ed AlSi10Mg samples [9], and the fatigue limits of the  $45^\circ$  and  $90^\circ$  samples were lower than that of the  $0^\circ$  sample. This is because the  $45^\circ$  and  $90^\circ$  samples have a higher density of defects distributed on the crack propagation paths, which is parallel to the direction of the SLM deposition layers (or perpendicular to the building direction) [25]. Additionally, for the  $0^\circ$  samples the maximum defect area was far less than those of the  $45^\circ$  and  $90^\circ$  samples. Due to the highly directional columnar grain structures, the as-built materials also exhibit obvious anisotropic properties which can cause the premature failure of AM components during service [26].

Since the beginning of the 20th century, a lot of researchers proposed

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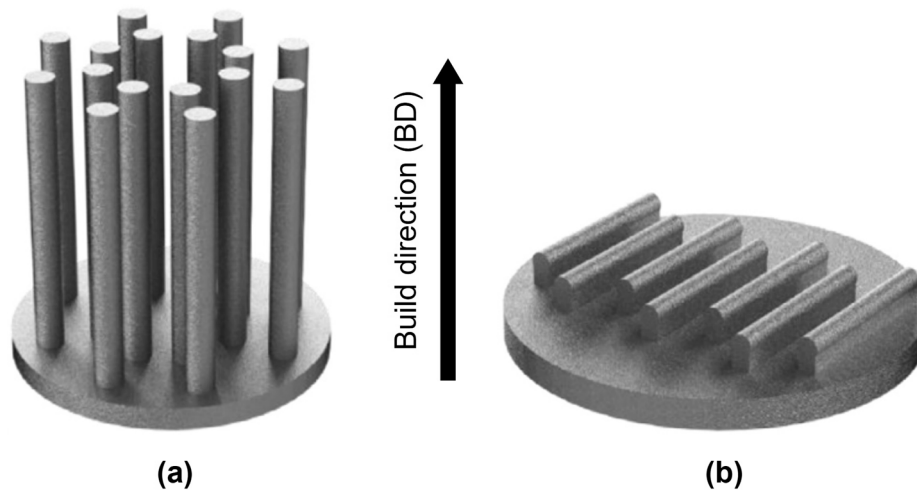


Fig. 1. The fatigue samples of SLM-ed AlSi10Mg alloy: (a) 90° BD sample; (b) 0° BD sample [11].

numerous criteria to predict fatigue life under different loading conditions. Basquin [27] offered a phenomenological model in which the stress amplitude and fatigue life are related via a power-law relationship. Later, Coffin [28] and Manson [29] emphasized the importance of plastic strain in predicting the fatigue life at low-cycle fatigue (LCF) regime. Then, a model connecting the plastic energy with fatigue life was proposed by Morrow [30], following whose footsteps a series of researchers employed energy-based approaches in fatigue life predicting [31–33].

Recently, with the increasing demands of safety requirements, more and more engineering components are designed to endure a fatigue life of more than  $10^7$  cycles (known as the very-high-cycle fatigue, VHCF), even up to  $10^8$  and  $10^9$  cycles [34]. As for LCF, only a few number of loading cycles is consumed to initiate cracks. However, in the HCF and VHCF regimes, more than 80–90% of fatigue life would be consumed in the crack initiation stage [35], which differs completely from that in LCF regimes. In addition, the unique feature of crack initiation for VHCF of high-strength alloys is that fatigue cracks initiate from the interior of material or specimen, which is the essential point that differs from LCF and HCF cases. Crack initiation of VHCF for metallic materials possesses a unique feature of fish-eye (FiE) which contains a fine-granular-area (FGA). It is regarded that FGA together with FiE is the characteristic region of crack initiation for VHCF, and the value of stress intensity factor range for this region keeps constant for a given material [36].

In the past two decades, several researchers proposed some models to explain the formation mechanism of crack initiation region in VHCF regimes [37–39]. Zhao et al. [40] analyzed the relationship between the plastic zone size ahead of FGA crack tip and the dimension of related microstructure. Murakami et al. [41] provided the formulas of the maximum value of stress intensity factor ( $K_{I_{max}}$ ) for the problems of a crack originating from surface defect or from interior defect. Recently, based on the revealed microscopic nature of crack initiation region of VHCF, Hong et al. [42] proposed a model of Numerous Cyclic Pressing (NCP) to explain the formation mechanism of FGA.

Statistical extremes of fatigue lifetime distribution have been primarily based on large number of experimental data [43]. The experimental results have indicated a scatter in HCF and VHCF lifetime, which is because of the variability in microstructures and defect distribution [44]. However, both the data acquisition and microstructure

reconstruction in experiments are extremely slow and redundant. One best way to improve the prediction efficiency of fatigue performance for SLM-ed AlSi10Mg is to use the advanced computation techniques, crystal plasticity finite element (CPFE) frameworks [45,46]. CPFE method has enabled us to implement complex algorithms to model the non-linear material response on the *meso*-scale behavior of crystalline metallic systems with a better approximation [47,48]. Researchers have used CPFE simulation to offer microstructure-sensitive fatigue life prediction frameworks. For example, inspired by the critical plane approach proposed by Fatemi and Socie [49], McDowell and co-workers [50–54] suggested a fatigue indicative parameter accounting for microstructural heterogeneities with the CPFE simulations.

In this paper, the HCF and VHCF behaviors of SLM-ed AlSi10Mg alloy were studied based on CPFE simulations. The goal is to understand the effect and mechanism of build orientation and defects on the fatigue properties of the SLM-ed AlSi10Mg alloy. This paper is structured as follows. The material processing information is detailed in Section 2. The theoretical framework of crystal plasticity is described in Section 3. Section 4 offers the modeling process of CPFE simulations. In Section 5, we provide three fatigue indicator parameter (FIP) models to assess the HCF and VHCF properties of SLM-ed AlSi10Mg alloy. In Section 6, the results are discussed. Finally, concluding remarks are presented.

## 2. Materials and SLM-ed samples

In this study, the AlSi10Mg samples were fabricated in 0° and 90° building directions (BD), as shown in Fig. 1. The main chemical compositions of the alloy are listed in Table 1. The process parameters of SLM manufacturing are listed in Table 2. The mechanical properties of the AlSi10Mg samples (elastic modulus  $E$ , 0.2% offset yield strength  $\sigma_{0.2}$ , ultimate tensile strength  $\sigma_b$ , elongation after fracture  $\delta$ ) were obtained by the uniaxial tensile tests, and the data are listed in Table 3.

The geometries of the tensile and fatigue test specimens are respectively shown in Fig. 2. The design of the AlSi10Mg tensile test specimens was in accordance to the standard of GB/T228-2002. For each group of specimens, six specimens were tested at a tension rate of 2 mm/min. An ultrasonic fatigue machine with a resonance frequency of 20 kHz was used for the fatigue tests. The experiments were carried out by the displacement control in the range between 2.2  $\mu\text{m}$  and 21.5  $\mu\text{m}$ . The

Table 1  
Nominal chemical composition of AlSi10Mg alloy (wt.%) [55].

Al	Si	Mg	Fe	Ti	Cu	Cr	Mn	Ni
Bal.	9.75	0.22	0.092	0.011	<0.01	<0.01	<0.01	<0.01

**Table 2**  
SLM manufacturing parameters of the AlSi10Mg specimens.

Laser power [W]	Scanning speed [mm/s]	Scanning spacing [mm]	Preheating temperature [°C]	Layer thickness [mm]	Printing direction [°]	Laser profile
370	1300	0.19	35	0.05	0, 90	Gaussian

**Table 3**  
Mechanical properties of the SLMed-AlSi10Mg alloy.

Sample	$E$ , GPa	$\sigma_{0.2}$ , MPa	$\sigma_b$ , MPa	$\delta$ , %
90°	65.5 ± 3	234.3 ± 4	437 ± 6	4.7 ± 0.5
0°	62 ± 3	280 ± 4	465 ± 6	11.8 ± 0.5

AlSi10Mg specimens under three stress ratios ( $R = -1, 0, 0.5$ ) were used in the experiment. Ten specimens were tested under each stress ratio. Detailed experimental techniques and results can be found in [55].

Fig. 3 displays the electron backscattering diffraction (EBSD) for the initial microstructures of the SLM-ed samples. In Fig. 3(a), equiaxed grain morphology can be seen in the TD-RD plane which is perpendicular to BD. While Fig. 3(b) exhibits obviously columnar grain morphology in the BD-TD plane which is parallel to BD. Similar phenomena exist both in 0° and 90° specimens, thus only the results of 90° specimens were displayed in this paper. Both in Fig. 3(a) and (b), the pole figure maps on the right reflect that the microstructure of the SLM-ed samples did not show evident texture.

To better model the size and shape of the grains used in this study, we performed a statistical analysis of the columnar grain in the TD-RD plane and BD-TD plane with the EBSD results, as shown in Figs. 4 and 5. Fig. 4 shows the average grain size is 9.61  $\mu\text{m}$ , and Fig. 5 indicates the average aspect ratio of the columnar grain is 4.62. For convenience, in the subsequent simulations, we take the grain size as 10  $\mu\text{m}$  in the plane perpendicular to BD, and the aspect ratio as 5 for the columnar grain.

In this work, the failure modes due to crystallographic features and defects are primarily considered. The role of residual stresses was not considered. In addition, a uniform surface roughness (the maximum height of the profile  $R_a$ , the distance between the profile peak line and valley line, was approximately 2.746  $\mu\text{m}$ ) was achieved, which is much smaller than the size of the AlSi10Mg powders. Therefore, the effect of sample surface roughness on the fatigue properties of the SLM-ed AlSi10Mg alloy is ignored.

### 3. Crystal plasticity framework

In the following sections, a CPFEM framework accommodating finite deformation effects is used. The governing equations, for single crystals in a continuum framework, will be introduced to provide a background. The kinematics uses a multiplicative decomposition of the deformation gradient. And the phenomenological constitutive relationships incorporating microscopic behaviors in the material will then be given.

#### 3.1. Kinematics

The following kinematic theory is based on the work described in [56,57]. The total deformation gradient  $\mathbf{F}$  obeys a multiplicative decomposition is given in the following equation,

$$\mathbf{F} = \mathbf{F}_e \cdot \mathbf{F}_p \quad (1)$$

where  $\mathbf{F}_e$  represents the elastic deformation gradient associated with rigid body rotation and elastic stretching of the crystal lattice, and  $\mathbf{F}_p$  is the plastic deformation gradient associated with crystallographic slip.

The velocity gradient in the current state can be calculated using the following equation,

$$\mathbf{L} = \dot{\mathbf{F}} \cdot \mathbf{F}^{-1} = \mathbf{L}_e + \mathbf{L}_p \quad (2)$$

where  $\mathbf{L}_e$  is the elastic velocity gradient, and  $\mathbf{L}_p$  is the plastic velocity gradient.  $\mathbf{L}$  can be then decomposed into two parts: the symmetric rate of stretching tensor  $\mathbf{D}$  and the antisymmetric spin tensor  $\mathbf{\Omega}$ . These two tensors can be decomposed into lattice parts (subscript e) and plastic parts (subscript p) as follows:

$$\mathbf{L} = \mathbf{D} + \mathbf{\Omega} \quad (3)$$

$$\mathbf{D} = \mathbf{D}_e + \mathbf{D}_p \quad (4)$$

$$\mathbf{\Omega} = \mathbf{\Omega}_e + \mathbf{\Omega}_p \quad (5)$$

$\mathbf{L}_e$  and  $\mathbf{L}_p$  can be calculated using the following equations,

$$\mathbf{L}_e = \mathbf{D}_e + \mathbf{\Omega}_e = \dot{\mathbf{F}}_e \cdot \mathbf{F}_e^{-1} \quad (6)$$

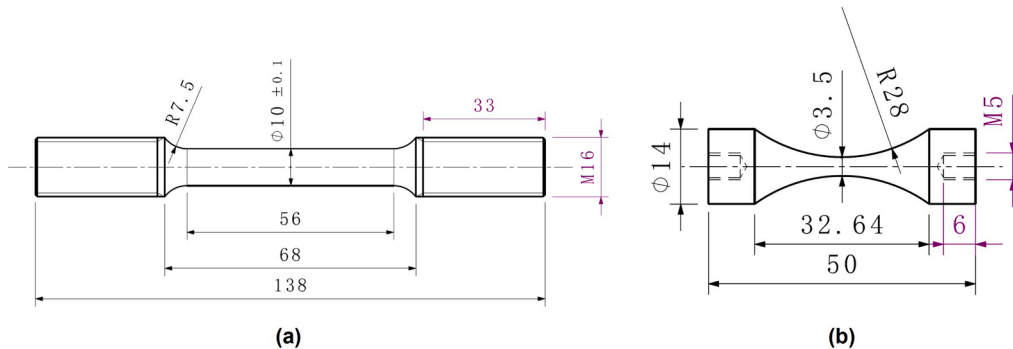
$$\mathbf{L}_p = \mathbf{D}_p + \mathbf{\Omega}_p = \dot{\mathbf{F}}_p \cdot \mathbf{F}_p^{-1} = \sum_{\alpha=1}^{N_s} \dot{\gamma}^\alpha \mathbf{s}^{*\alpha} \mathbf{m}^{*\alpha} \quad (7)$$

where  $N_s$  is the number of slip systems;  $\dot{\gamma}^\alpha$  is the slip rate on slip system  $\alpha$ ;  $\mathbf{s}^{*\alpha}$  and  $\mathbf{m}^{*\alpha}$  represent the vector along the slip direction and the vector normal to the slip plane of system  $\alpha$ , respectively, in the deformed configuration,

$$\mathbf{s}^{*\alpha} = \mathbf{F}_e \cdot \mathbf{s}^\alpha \quad (8)$$

$$\mathbf{m}^{*\alpha} = \mathbf{m}^\alpha \cdot \mathbf{F}_e^{-1} \quad (9)$$

where  $\mathbf{s}^\alpha$  and  $\mathbf{m}^\alpha$  are the unit vectors in the slip direction and normal to the slip plane in the reference configuration, respectively.



**Fig. 2.** Geometry of (a) tensile test specimens under monotonic quasi-static loading, and (b) fatigue test specimens under ultrasonic axial cycling (dimensions in mm) [55].

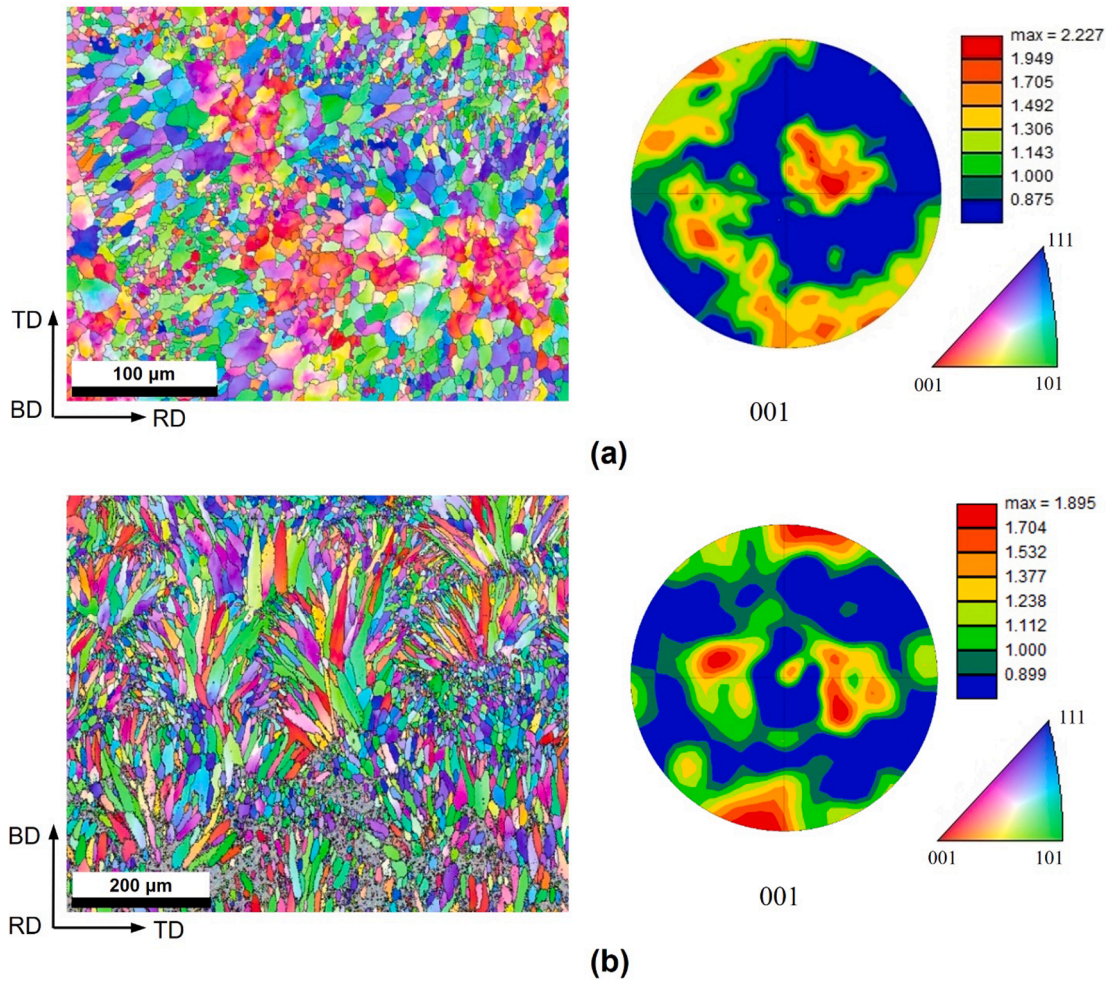


Fig. 3. The microstructure of AlSi10Mg alloy: (a) equiaxed grain morphology in the TD-RD plane; (b) columnar grain morphology in BD-TD plane. TD is the transverse direction, RD the rolling direction, and BD the building direction.

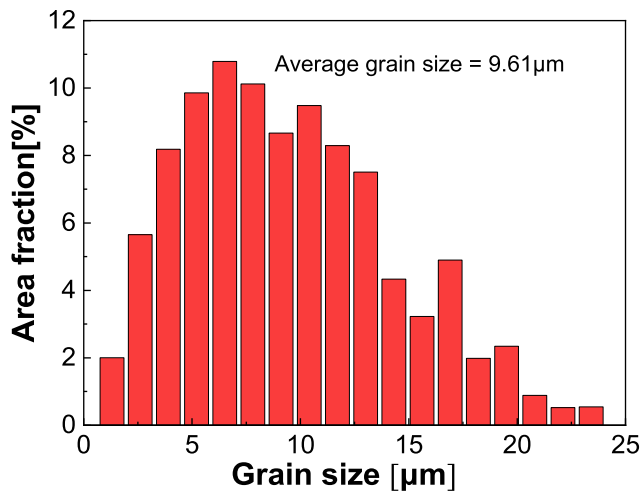


Fig. 4. Grain size distribution in the TD-RD plane.

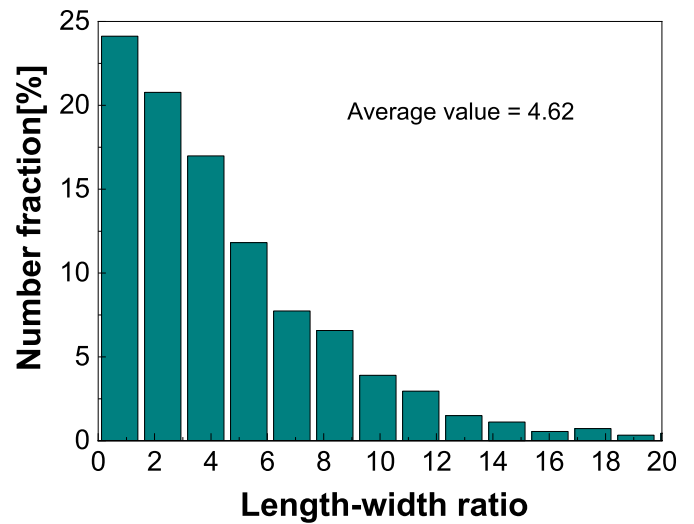


Fig. 5. The length-width ratio of the columnar grain in the BD-TD plane.

### 3.2. Constitutive models

Based on the Schmid law, the slipping rate  $\dot{\gamma}^\alpha$  of the  $\alpha$  slip system in a rate-dependent crystalline solid is determined by the corresponding resolved shear stress  $\tau^\alpha$  as proposed by Hutchinson [58],

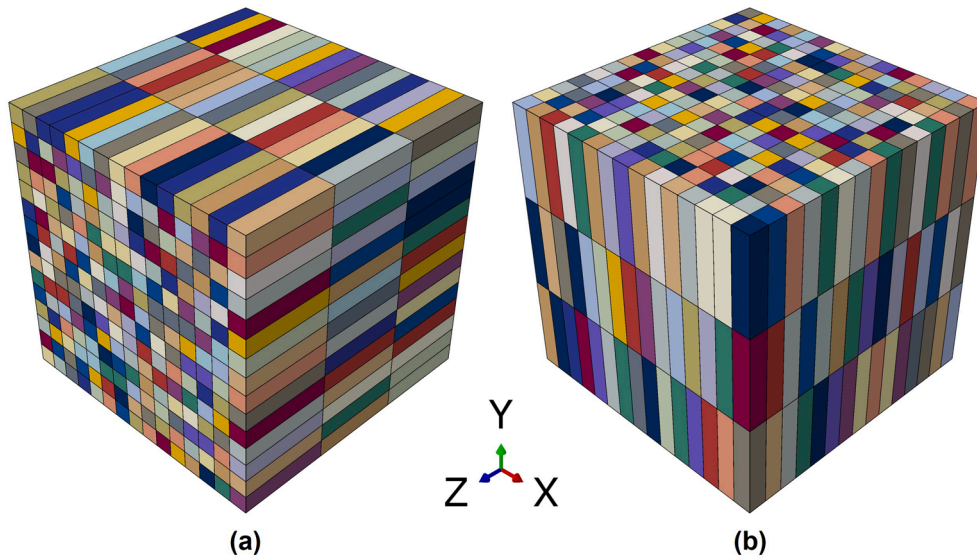


Fig. 6. The RVEs: (a) 90° sample; (b) 0° sample. The colors represent different grains within the volume.

$$\dot{\gamma}^\alpha = \dot{\gamma}_0 \left( \frac{\tau^\alpha}{g^\alpha} \right) \left| \frac{\tau^\alpha}{g^\alpha} \right|^{n-1} \quad (10)$$

where  $\dot{\gamma}_0$  is the reference shear strain rate;  $g^\alpha$  is a variable which describes the current strength of the system;  $n$  is the rate sensitivity exponent.

The strain hardening is characterized by the evolution of the strengths  $g^\alpha$  through the incremental relation,

$$\dot{g}^\alpha = \sum_{\beta=1}^{N_s} h_{\alpha\beta} |\dot{\gamma}^\beta| \quad (11)$$

where  $h_{\alpha\beta}$  are the latent hardening moduli. The expressions of latent hardening moduli  $h_{\alpha\beta}$  and self-hardening moduli  $h_{\alpha\alpha}$  in the studies by Pierce et al. [59] and Asaro [60] is adopted,

$$h_{\alpha\beta} = qh(\gamma) + (1 - q)h(\gamma)\delta_{\alpha\beta} \quad (12)$$

$$h_{\alpha\alpha} = h(\gamma) = h_0 \text{sech}^2 \left| \frac{h_0 \gamma}{\tau_s - \tau_0} \right| \quad (13)$$

$$\gamma = \sum_{\alpha=1}^{N_s} \int_0^\gamma |\dot{\gamma}^\alpha| dt \quad (14)$$

where  $q$  is a measure for latent hardening, in most cases its value is taken as 1.0 for coplanar slip systems  $\alpha$  and  $\beta$ , and 1.4 otherwise, which renders the hardening model anisotropic;  $h_0$  is the initial hardening modulus;  $\tau_0$  is the yield shear stress; and  $\tau_s$  is the saturated flow stress (or the break-through stress where large plastic flow initiates);  $\gamma$  is Taylor cumulative shear strain on all slip systems.

#### 4. Finite element simulation

To evaluate the mechanical and fatigue properties of the AlSi10Mg alloy produced by SLM, the simulations, under uniaxial tension and uniaxial cyclic loading conditions, were conducted using the software ABAQUS and a user-defined material subroutine (UMAT) program based on crystal plasticity theory introduced in Section 3. The AlSi10Mg alloy has a face center cubic (FCC) structure. Hence, the dislocation glide occurs on 12 possible slip systems in the material.

#### 4.1. Representative volume element (RVE)

In 1960s the concept of RVE was introduced as a microstructural sub/region, which is representative of the entire microstructure in an average sense. The material properties of a specimen larger than RVE can be treated equally to the average material properties of RVE. While, if a specimen is smaller than the RVE, its material properties vary according to its constituents (grains, phases, and so on) [61]. So, in order to combine micro-mechanical and coupled multi-scale approaches, an appropriate RVE of heterogeneous materials is required.

On one hand, an RVE must have enough number of grains to homogenize the variabilities arising from local microstructural features (texture, defects and chemical compositions). On the other hand, if the RVE is too big and contains too many grains, the FEM simulations can be extremely expensive. The definition of RVE size is thus extremely important for the mechanics and physics of heterogeneous materials. Numbers of approaches for the determination of RVEs have been described in the references [62-65].

In this work, we used the grain-based RVE model, in which each grain was described by many cubic elements, in order to effectively include more details about the grain shapes and sizes distribution in polycrystalline materials. From the statistical point of view, as the number of grains in the RVE increases, the response of the RVE converges to the macroscopic behaviors of the real materials.

Moussa Bouchedjra et al. [66] investigated the optimal size of RVE for polycrystal materials to predict the elastoplastic behavior using the crystal plasticity model. They validated the simulation results with corresponding experimental results on Aluminum alloy. They found that for the case (more than 200 grains), the prediction error of all quantities (tensile and cyclic tests) is less than 3%, except ratcheting strain and plastic range, which still have an error of relatively higher than 6%. For the tensile test and strain-controlled cyclic test, simulation results performed on RVE of 250 grains agree well with the experimental results. However, for the elastoplastic behavior during a stress-controlled cyclic test, the optimal RVE should have a size greater than 250 grains to assess the mechanical response of the material.

In this article, the RVE of a polycrystalline cube incorporating 675 grains were established, and random orientations were assigned to the grains within the volume (see Fig. 6), which is consistent with the EBSD results in Section 2. This RVE provides a good balance between the accuracy of the simulation results and reasonable computational efficiency. The height, width and thickness of the RVE model are all 150  $\mu\text{m}$ . The short size of the columnar crystals is 10  $\mu\text{m}$  according to the

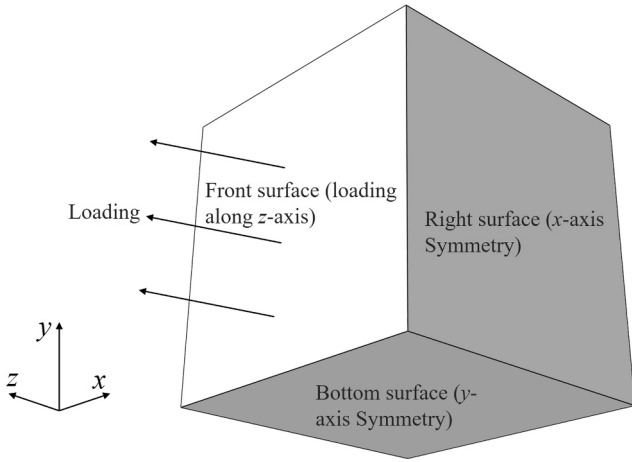


Fig. 7. Surface breakdown of the RVE to demonstrate the application of boundary conditions.

experimental results, and the long size is  $50 \mu\text{m}$  (see Section 2). The RVE was then meshed using 8-node linear brick elements (C3D8I).

#### 4.2. Boundary conditions

The boundary conditions of RVEs employed in the simulation are important to ensure their deformation response consistent with the macro-scale behavior of the material. In this study, we take 1/8 of the model and adopt the symmetric boundary conditions in the CPFEE simulations as demonstrated in Fig. 7: on the right surface  $U_x = UR_y = UR_z = 0$  (about x-axis symmetry); on the bottom surface  $U_y = UR_x = UR_z = 0$  (about y-axis symmetry); on the back surface  $U_z = UR_x = UR_y = 0$  (about z-axis symmetry); and on the front surface, the uniaxial tension or uniaxial cyclic loadings is applied along z-axis. The faces of RVEs that are not assigned a boundary condition can deform freely.

#### 4.3. Parameter calibration

In this section, the 8 parameters ( $C_{11}$ ,  $C_{12}$ ,  $C_{44}$ ,  $h_0$ ,  $\tau_0$ ,  $\tau_s$ ,  $n$ ,  $\dot{\gamma}_0$ )

Table 4  
Elasticity and crystal plasticity model parameters of the SLM-ed AlSi10Mg alloy.

Samples	$C_{11}$ [MPa]	$C_{12}$ [MPa]	$C_{44}$ [MPa]	$\dot{\gamma}_0$	$n$	$h_0$ [MPa]	$\tau_s$ [MPa]	$\tau_0$ [MPa]
90°	100,731	60,345	30,087	0.001	90	1400	180	90
0°	100,731	60,345	30,087	0.001	90	700	188	108

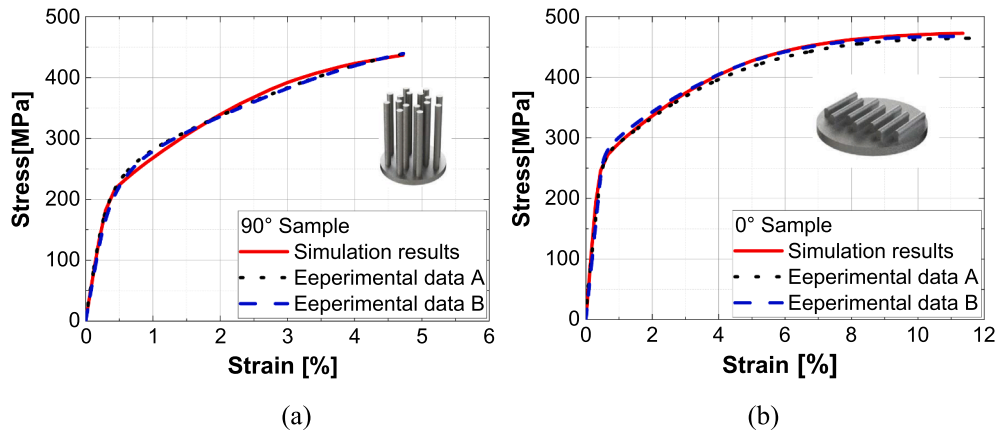


Fig. 8. Stress-strain evolution of AlSi10Mg specimens under uniaxial tensile loading: (a) 90° sample; (b) 0° sample.

adopted in the constitutive models are calibrated with the results of uniaxial tension tests, which is shown in Table 4. For AlSi10Mg alloy, it has three independent elastic constants,  $C_{11}$ ,  $C_{12}$ ,  $C_{44}$ , due to the FCC symmetry. The other model parameters can be referred to the crystal plasticity theory in Section 3.

In the uniaxial tension tests, both the 90° and 0° samples were loading under a strain rate of  $1 \times 10^{-3} \text{ s}^{-1}$ . The calibration of crystal plasticity model parameters was conducted following the try-and-error method by comparing with the tensile stress-strain curves of AlSi10Mg alloy in Fig. 8. For each of the simulation, 675 grains with different grain orientations were generated, following the same average grain size and the same set of crystal plasticity model parameters. It is seen that the tensile curve simulated by the crystal plasticity model coincided well with the experimental ones.

#### 5. Fatigue indicator parameter (FIP) and lifetime prediction

In this work, the FIP, which should be positive and monotonically increasing with the number of loading cycles, is used to predict the fatigue lifetime of SLM-ed AlSi10Mg alloy. Based on the previous studies, including Smith-Watson-Topper's (SWT) model [67,68], works by Prithvirajan and Sangid [46], and works by Gu and co-workers [69], we assess the fatigue lifetime using different FIPs, and compared the prediction results in Section 6.

It is believed that plastic strain and local stresses are important in predicting the crack initiation events. The accumulation of plastic strain,  $P_{ac}$ , indicates the cumulative slip deformation due to the shear stresses in all slip systems.  $P_{ac}$  can be obtained by the integral of the double dot product of the plastic velocity gradient  $L_p$ , and used in the fatigue life prediction.

$$P_{ac} = \int \sqrt{\frac{2}{3}} L_p : L_p dt \quad (15)$$

The first parameter  $FIP_1$  is taken as the increment of  $P_{ac}$  in the stable loading cycles [46],

$$FIP_1 = \Delta P_{ac} = P_{ac}|_{N+1} - P_{ac}|_N \quad (16)$$

$$N_{p1} = \frac{P_{ac,c} - P_{ac,N}}{FIP_1} \quad (17)$$

**Table 5**  
The results of ultrasonic fatigue tests for SLMed-AlSi10Mg alloy.

Number	BD	Stress ratio R	Stress amplitude $\sigma_a$ (MPa)	Defect size ( $\mu\text{m}$ )	Experimental fatigue life
1	0° sample	-1	93	55.09	4.20E+08
2		-1	93	63.66	3.67E+08
3		-1	114	64.88	3.70E+07
4		-1	125	85.51	4.40E+07
5		0	60	71.42	6.22E+08
6		0	70	85.39	4.23E+08
7		0	80	67.29	3.32E+08
8		0.5	50	64.88	1.67E+09
9		0.5	60	50.38	1.10E+09
10		0.5	60	32.88	1.10E+09
11	90° sample	0.5	65	72.26	4.74E+08
12		-1	60	206.22	3.63E+08
13		-1	70	105.01	1.17E+09
14		-1	75	93.69	5.81E+08
15		-1	80	184.91	1.05E+08
16		0	40	210.96	3.82E+08
17		0	40	103.3	1.11E+09
18		0	40	160	1.09E+05
19		0	50	159.28	2.15E+08

where  $P_{ac, c}$  is the critical plastic strain when the fracture failure occurs, which can be obtained by tests;  $P_{ac, N}$  represents the plastic strain after which the value of  $\Delta P_{ac}$  becomes a constant, as is seen Fig. 11, in this study we take the subscript  $N$  as 20;  $N_{p1}$  is the corresponding fatigue lifetime.

The second model is taken as:

$$FIP_2 = FIP_1 \tag{18}$$

$$N_{p2} = \frac{\alpha_p}{d_{gr}(FIP_2)^2} \tag{19}$$

where  $d_{gr}$  is a reference constant, which is on the order of the grain size to represent the microstructure, in this study it is  $3 \times 10^{-5}$ ;  $\alpha_p$  is a fitting constant, which equals  $3 \times 10^{-5}$  in  $90^\circ$  specimens,  $2.5 \times 10^{-4}$  in  $0^\circ$  specimens.

The third parameter  $FIP_3$  is taken as the constant  $\sigma_{max}\epsilon_a$  in Smith-Watson-Topper (SWT) model. The HCF and VHCF regimes correspond to stress amplitudes below the macroscopic yield stress, thus we take the elastic part of SWT model to study the corresponding extreme fatigue life.

$$FIP_3 = \sigma_{max}\epsilon_a \tag{20}$$

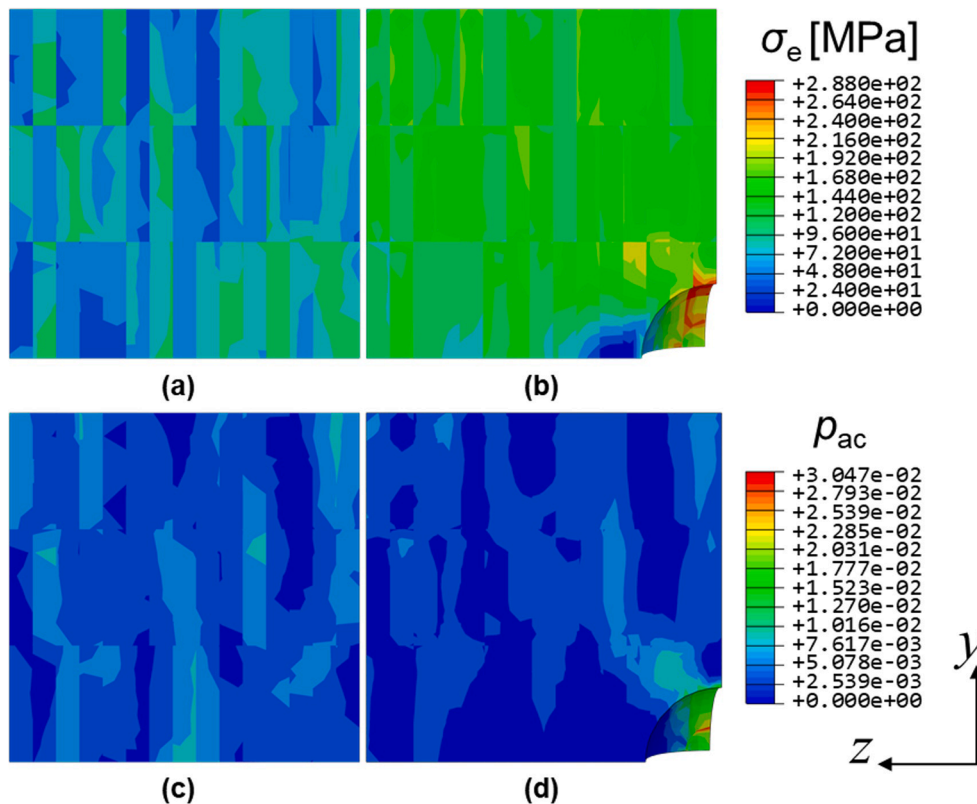
$$FIP_3 = \frac{(\sigma'_f)^2}{E}(2N_{p3})^{2b} \tag{21}$$

where  $\epsilon_a$  is the elastic strain amplitude;  $\sigma'_f$  is the fatigue strength coefficient;  $E$  is the elastic modulus; and  $b$  is the fatigue strength exponent. In  $90^\circ$  specimens,  $E = 62$  GPa;  $\sigma'_f = 440$  MPa;  $b = -0.067$ . In  $0^\circ$  specimens,  $E = 65$  GPa;  $\sigma'_f = 470$  MPa;  $b = -0.056$ .

The calibration of the above parameters was conducted following the try-and-error method by comparing the simulation results with the experimental ones to make sure that the error is minimal. These three metrics will be used subsequently to identify the location of failure within an RVE and predict the fatigue life of each RVE.

### 6. Results and discussion

The frequency of ultrasonic fatigue tests is 20 kHz, thus both the  $90^\circ$  and  $0^\circ$  samples were loading under the same frequency. The results of ultrasonic fatigue tests for SLMed AlSi10Mg alloy are listed in Table 5. After the ultrasonic fatigue tests, fracture surfaces of all the broken specimens were carefully examined by SEM. The areas of the defects are equivalent to that of circles whose diameters are also listed in Table 5.



**Fig. 9.** The stress and plastic strain  $P_{ac}$  fields in CPFEM models of the  $0^\circ$  specimens under uniaxial cycle loadings, with a stress ratio of  $R = 0.5$  and a stress amplitude of  $\sigma_a = 50$  MPa for 50 cycles: (a, c) complete models without defects; (b, d) models with a pore of  $d = 64.88 \mu\text{m}$ .

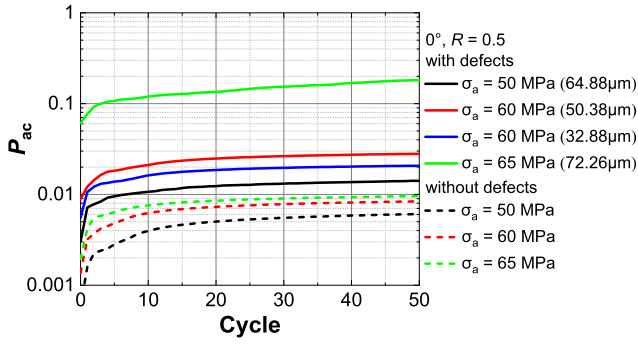


Fig. 10. The variation of  $P_{ac}$  in  $0^\circ$  specimens with the cycle number under different stress amplitudes  $\sigma_a$ .  $R$  is the stress ratio. And the defect diameters are presented in the brackets.

And in CPFEM simulations, the 3D defects in RVEs are modelled as spheres whose diameters equal to that of the circles. All the cases in Table 5 have the feature that the fatigue cracks initiate from the interior of the specimens.

### 6.1. Stress and strain fields

The fields of Mises stress  $\sigma_e$  and plastic strain  $P_{ac}$  in different CPFEM models for  $0^\circ$  specimens are shown in Fig. 9. It is clear that defects can cause stress and strain concentrations. In Fig. 9 (b) and (d), near the pore, along its vertical sides (parallel to  $y$ -axis), which is perpendicular to the loading direction (parallel to  $z$ -axis), stress and strain concentrations occur. This is consistent with the phenomenon observed in experiments that the cracks initiate from a pore on the fracture surface. And the pore can be regarded as a special case of non-sharp crack. In this case, the up and bottom regions of the pore act as the blunt crack tips, which are corresponding to the largest stress concentration regions. The stress and plastic strain fields, in different CPFEM models under uniaxial cycle loadings with a stress ratio of  $R = -1$  and  $0$ , have a similar phenomenon with the case of  $R = 0.5$  in  $0^\circ$  specimens. And the same phenomenon can also be seen in  $90^\circ$  specimens. Thus this section only offers the results in one case.

### 6.2. The plastic accumulated strain $P_{ac}$

Fig. 10 shows the variation of  $P_{ac}$  for CPFEM polycrystalline models in  $0^\circ$  specimens under uniaxial cyclic loadings with different stress amplitudes  $\sigma_a$ . It is evident that  $P_{ac}$  increases with the accumulation of loading cycles. And the larger the stress amplitudes  $\sigma_a$  is, the greater the plastic strain  $P_{ac}$  is. When the loading conditions are completely consistent, the larger the defect size is in the specimen, the greater the

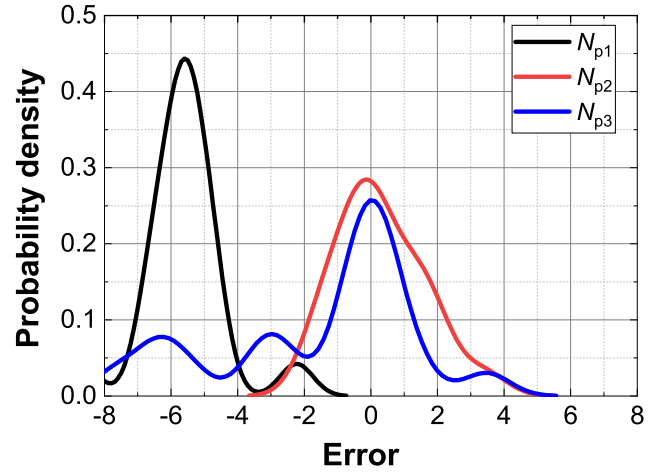


Fig. 12. Normal distribution of the error for fatigue life predicted by different models.

plastic strain  $P_{ac}$  is, as is shown with the red solid line and blue one.

From Fig. 10, it can be seen that after the 20th loading cycle, the growth of  $P_{ac}$  is steady and slow, and the increment  $\Delta P_{ac}$  almost remains constant. This is consistent with the study of Gillner and Münstermann [70] that the increment of local accumulated plastic shear strain kept almost constant after the initial several cycles. Then in the following study, we take the increment of plastic strain  $\Delta P_{ac}$  at the 20th loading cycle, as the parameter  $FIP_1$  (see Section 5).

The values of  $P_{ac}$ , in different CPFEM models under uniaxial cycle loadings with a stress ratio of  $R = 0$  and  $-1$ , have a similar phenomenon with the case of  $R = 0.5$ , and the variation of  $P_{ac}$  in  $90^\circ$  sample is similar to that in the  $0^\circ$  sample, thus this section only offers the results in one case.

### 6.3. Fatigue life prediction

In Fig. 11, the predicted fatigue lives by different models (see Section 5,  $N_{p1}$ ,  $N_{p2}$ ,  $N_{p3}$ ) are compared with the experimental results. It is shown that there are some fatigue life data points in models  $FIP_1$  and  $FIP_3$  locate without the scatter band between the two dotted lines ( $\pm 2$  error); while in model  $N_{p2}$ , almost all the fatigue life data points located within the scatter band. Thus, the fatigue lifetime predicted by model  $N_{p2}$  is satisfactory and more accurate than the other two models. The only datum above the scatter band in Fig. 11 (b), represents the case of  $R = 0$ ,  $\sigma_a = 40$  MPa, experimental fatigue life =  $1.09 \times 10^5$ , which is far less than other values and without the VHCF regime. This could be because that there are sharp defects within the specimen.

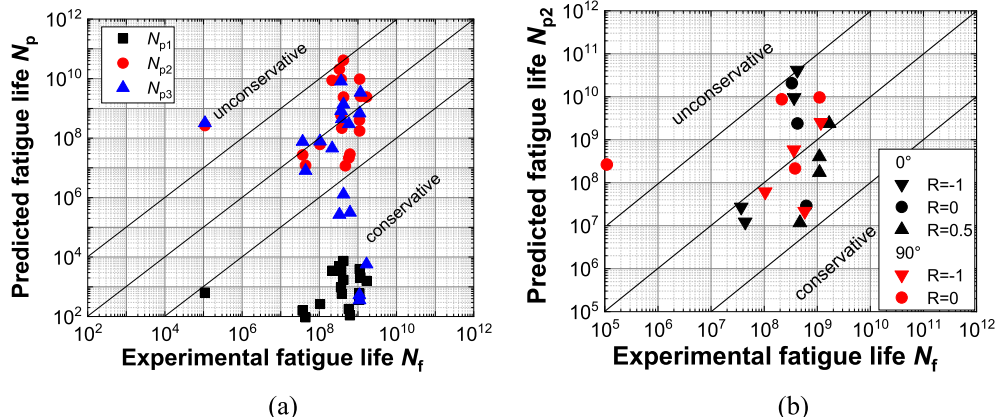


Fig. 11. Comparison of the predicted fatigue lives by different models versus the experimental ones.



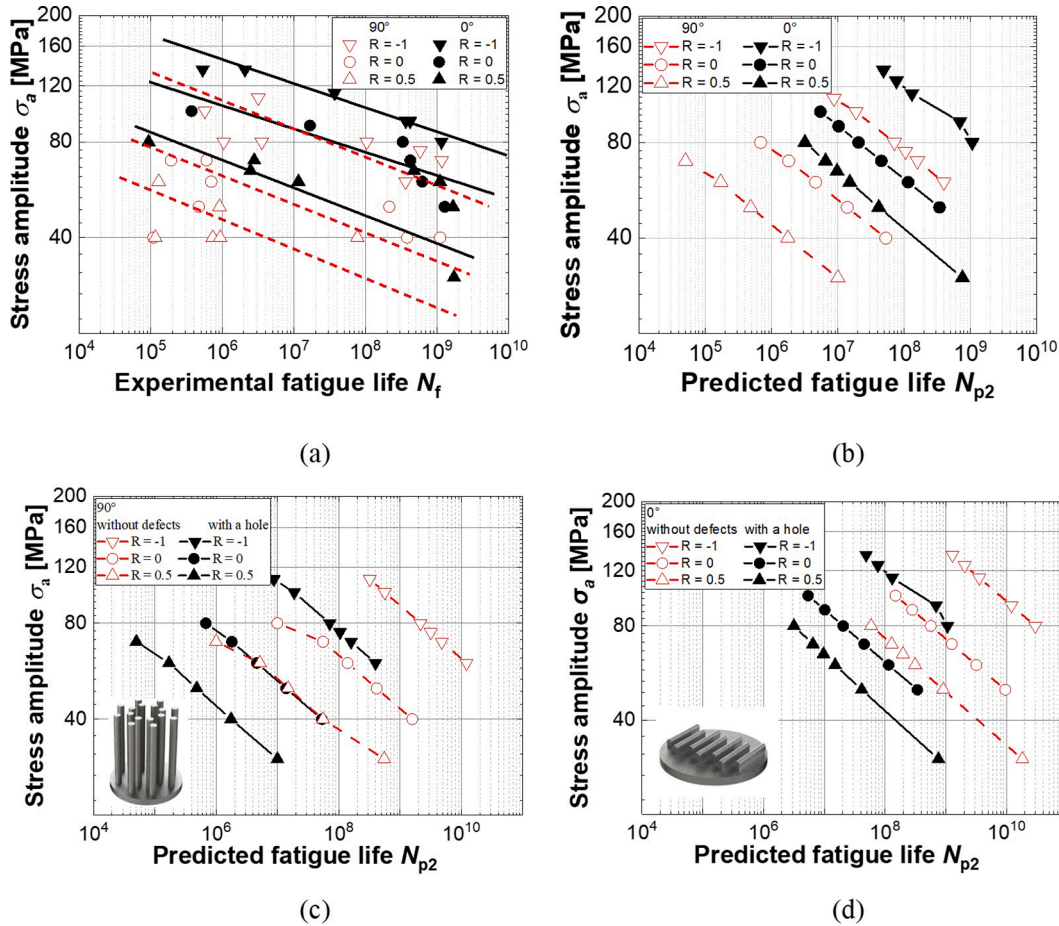


Fig. 13. S-N curves by different models for AlSi10Mg specimens: (a) experimental data; (b) predicted values by model  $N_{p2}$  with a hole in the specimen; (c) comparison between the results predicted by model  $N_{p2}$  in  $90^\circ$  specimens with a hole and without defects; (d) comparison between the results predicted by model  $N_{p2}$  in  $0^\circ$  specimens with a hole and without defects.

In Fig. 12, the normal distribution of the error for fatigue life predicted by different models is presented. The peak values of these three curves represent the probability of their average error. So, the closer the average error is to 0, the more accurate the fatigue life prediction is. From Fig. 12, it is obvious that models  $N_{p2}$  and  $N_{p3}$  are better than model  $N_{p1}$ . In addition, the error distributions of model  $N_{p1}$  and  $N_{p3}$  have a larger range, indicating that the variance of the predicted fatigue life is greater. So, the prediction values of model  $N_{p1}$  and  $N_{p3}$  are instability. In contrast, the fatigue life prediction of model  $N_{p2}$  is more reliable.

In summary, the prediction of fatigue life by model  $N_{p2}$  is in good agreement with the test results. Therefore, model  $N_{p2}$  is recommended for fatigue life prediction of SLM-ed AlSi10Mg in VHCF regime.

$$\text{error} = \log_{10}(N_p) - \log_{10}(N_f) \quad (22)$$

where  $N_p$  is the predicted fatigue life, and  $N_f$  is the experimental fatigue life under the same loading condition.

Fig. 13 shows the S-N curves predicted by different models for SLM-ed AlSi10Mg specimens. In Fig. 13 (a), the experimental results indicate that the stress ratio plays an important role in HCF and VHCF properties. With the increase of the stress ratio, the fatigue strength decreases. In addition, the build orientation has an important effect on the fatigue property. The fatigue strength of  $90^\circ$  specimens is obviously lower than that of  $0^\circ$  specimens. In Fig. 13 (b), the predicted results by model  $N_{p2}$  show similar phenomena with Fig. 13 (a). Fig. 13 (c) and (d) demonstrate that defects can obviously reduce the HCF and VHCF fatigue performance of the specimen. The fatigue life of the sample with a hole is about 2 orders lower than that of the sample with no defects. The effect

of defects on the  $90^\circ$  built specimens is a little larger than that of  $0^\circ$  built specimens. There are two reasons for this. One reason is that both in  $90^\circ$  and  $0^\circ$  built specimens the stresses is applied along z-axis. However, the long axis directions of columnar crystals in  $90^\circ$  and  $0^\circ$  specimens are along z-axis and y-axis, respectively, due to the different building directions. The other reason is that the defect size of  $90^\circ$  built specimens is larger than that of  $0^\circ$  built specimens.

## 7. Conclusions

In the present study, the crystal plasticity finite element model is used to study the cyclic plasticity behavior and high-cycle fatigue and very-high-cycle fatigue properties of AlSi10Mg alloy fabricated by the selective laser melting process. The following conclusions have been obtained:

- (1) The HCF and VHCF fatigue life of the alloy predicted by model  $N_{p2}$  is in good agreement with the experimental results and the model  $N_{p2}$  is relatively reliable.
- (2) The build orientation has a great effect on the fatigue performance of SLM-ed AlSi10Mg.  $0^\circ$  specimens have a better performance than  $90^\circ$  specimens.
- (3) Defects significantly reduce the HCF and VHCF fatigue performance of the specimens. The fatigue lifetime of the sample with a hole is about 2 orders lower than that of the sample without defect. The effect of defects on the  $90^\circ$  built specimens is slightly larger than that of  $0^\circ$  built specimens.

- (4) The stress ratio plays an important role in HCF and VHCF properties. With the increase of the stress ratio, the fatigue strength decreases.

### Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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