

## Full Length Article

## Effects of oxidizers on the ignition and combustion characteristics of aluminum nanoparticles

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## ABSTRACT

Ignition and combustion of Aluminum nanoparticles (ANPs) under complex environments are of great significance for various propulsion systems. In this study, we investigated the oxidation process of ANPs in O<sub>2</sub>, CO<sub>2</sub>, H<sub>2</sub>O, and their mixture atmospheres using reactive molecular dynamics. In the mixture atmospheres, ANPs experience a shorter ignition delay and parts of C and H atoms are involved in a new reaction named re-oxidation, where the nonbonded C and H inside ANPs detach from particle and re-bond with free O in the environment to produce extra CO and H<sub>2</sub>O. It reduces C and H in unreactive diffusion and increases O in reactive diffusion. Additionally, it is found that the ignition delay time and reaction heat release can be adjusted to achieve the optimal performance of ANPs combustion by tailoring the contents of O<sub>2</sub>, CO<sub>2</sub>, and H<sub>2</sub>O in the environment. Our works provide a theoretical basis for the precise regulation of ANPs energy release.

## 1. Introduction

Aluminum particles, owing to their high enthalpy, high specific energy density [1], and non-toxic products [2], have been widely used in a variety of propulsion systems [3–6]. The difficulty of ignition and combustion of aluminum microparticles [7] brings great challenges to their practical application. Therefore, Aluminum nanoparticles (ANPs) have attracted more and more attention for their remarkable performances, such as high specific surface area, low ignition temperature, and high reaction rate [8].

In recent decades, a lot of researches have been conducted on the reaction mechanism of ANPs, and the effects of alumina shell structures [9], diffusion rate of aluminum and oxygen atoms [10], particle size [11], phase transition [12], shell melting and core reacting [13], and environmental temperature and pressure [14,15] have been analyzed by experiments and simulations. Besides, the oxidizer property in the atmosphere is also a significant factor in the ignition and combustion process of ANPs. Oxygen is the most important oxidizer for ANPs combustion and has been extensively studied. Rai et al. [16] established the diffusion combustion model of ANPs in O<sub>2</sub>. They argued that oxygen diffused from the outer surface of the particle to the reaction surface during combustion, while aluminum diffused from the core/shell interface to the reaction surface. Based on the direct simulation Monte

Carlo (DSMC) and CFD simulations, Zou et al. [17] proposed a theoretical model to describe the ignition characteristics of aluminum particles burning in the O<sub>2</sub> atmosphere. Two formulas were obtained to predict the ignition temperature and ignition delay time for nano/microparticles. Zhang et al. [18] employed molecular dynamics simulations to explore the oxidation process of ANPs with a diameter of 5 nm under different oxygen concentrations. They observed that the oxidized ANPs would form three morphological structures as the oxygen content increased: core-shell structure, core-chain structure, and oxide cluster. Li et al. [19] found that when ANP was burning in a high-temperature, high-density O<sub>2</sub> atmosphere, a micro-explosion phenomenon occurred, accelerating the oxidation process. Experimental results of Tang et al. [20] also proved that ANP would experience mild oxidation to micro-explosion with the increase of O<sub>2</sub> concentration.

However, in practical applications, ANPs often burn in an oxygen-deprived environment. During Mars exploration, CO<sub>2</sub> is the primary oxidant to provide energy for the propulsion system [21]. In addition, the reaction between ANP and H<sub>2</sub>O is also a technical means of making hydrogen, a potential energy source [22,23]. Therefore, the reaction between ANP and CO<sub>2</sub>/H<sub>2</sub>O has gradually received researchers' interest. Chu et al. [24] simulated the burning of ANPs in three typical oxidizers (O<sub>2</sub>, CO<sub>2</sub>, and H<sub>2</sub>O). They revealed three modes of ANP oxidation, including physical and chemical adsorption on the surface and

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**Table 1**  
Information on six system settings.

System	$N_{O_2}$	$N_{CO_2}$	$N_{H_2O}$
ANP-O <sub>2</sub>	2700	0	0
ANP-CO <sub>2</sub>	0	2700	0
ANP-H <sub>2</sub> O	0	0	2700
ANP-O <sub>2</sub> + CO <sub>2</sub>	1350	1350	0
ANP-O <sub>2</sub> + H <sub>2</sub> O	1350	0	1350
ANP-O <sub>2</sub> + CO <sub>2</sub> + H <sub>2</sub> O	900	900	900

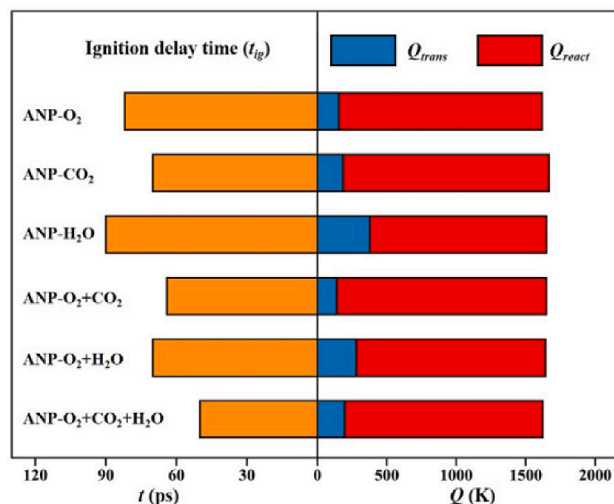
subsequent reactive diffusion inside the ANP. Meanwhile, They also observed that the reaction between ANP and CO<sub>2</sub> would produce CO gas, which was consistent with Masatoshi [25] and Brandstadt et al. [21]. Zhu et al. [26] studied the oxidation kinetics of ANP in CO<sub>2</sub> and obtained the activation energies of the two oxidation stages, which were 206.38 KJ/mol and 305.76 KJ/mol, respectively. In the study of reaction between ANP and H<sub>2</sub>O, Saceleanu et al. [27] reported that two rate-determining stages existed in the micro/nano aluminum powder-liquid water system. These two stages were controlled by redox reactions and mass transport, respectively. Simulations by Russo et al. [28] demonstrated that the concentration of H<sub>2</sub>O molecules had an important effect on the dissociation process of the ANP clusters.

In recent years, molecular dynamics (MD) simulations have been extensively performed to observe the behaviors of atoms during the oxidation process of ANP. However, most of the previous researches concentrate on the reaction of ANP with a single oxidant (O<sub>2</sub>, CO<sub>2</sub>, or H<sub>2</sub>O) [10,24,28]. As far as we know, there are few systematic simulations on the ignition and combustion of ANP in a complex mixture environment. In this work, the ReaxFF molecular dynamics method was employed to simulate the heat transfer and gas-particle reaction of core-shell ANP under different hot pure/mixture atmospheres. The effects of oxidant components on the ignition delay time and reaction heat release of ANP were obtained. The results of this paper are expected to provide theoretical guidance for the control of ANPs ignition and combustion in complex environments.

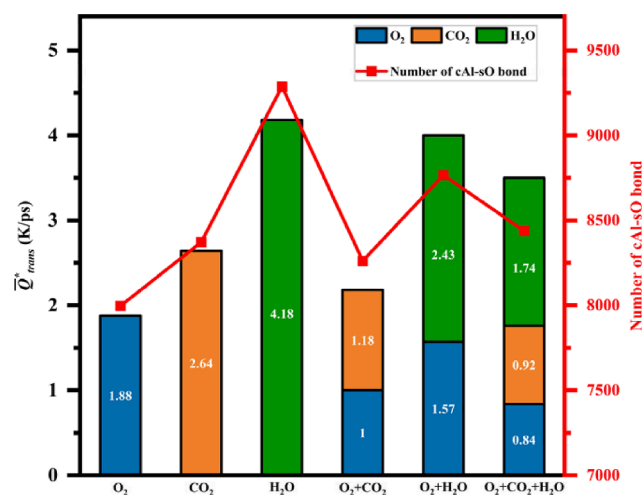
## 2. Method

### 2.1. Reactive force field

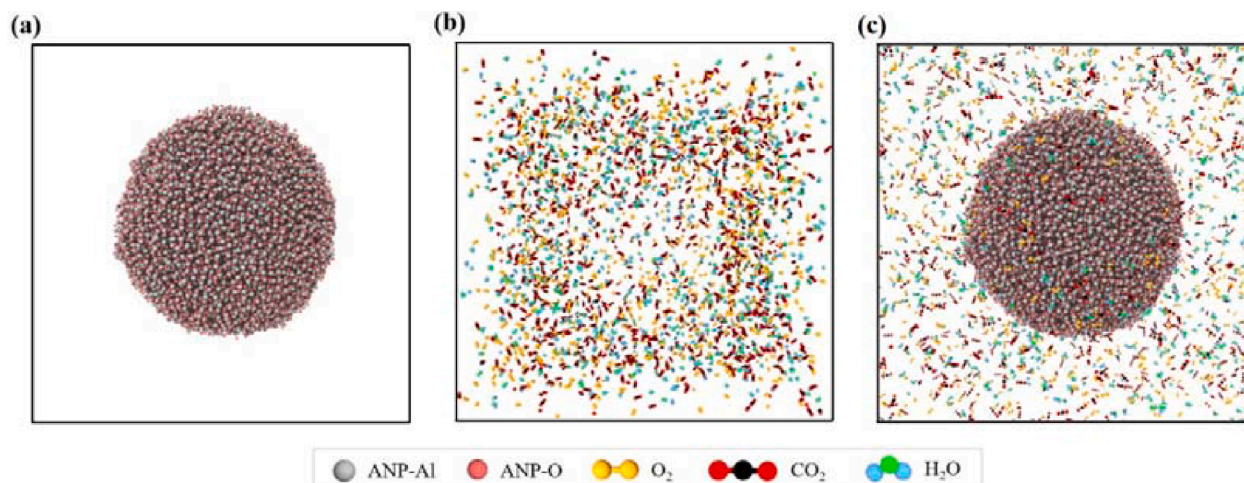
The ReaxFF reactive force field is commonly used in molecular dynamics, and it is performed in the simulations of most elements in the periodic table [29–33]. The parameters of ReaxFF are derived from experimental results and the principles of quantum mechanics. ReaxFF reactive force field is based on a bond-order mechanism to describe the



**Fig. 2.** Ignition delay time (left part) and contributions of heat transfer and reaction heat release before ignition (right part) in the six atmospheres.



**Fig. 3.** Average heat transfer rate of oxidizers before ignition (the left axis) and the number of cAl-sO bond at ignition (the right axis) in the six atmospheres.



**Fig. 1.** Snapshots of models: (a) the core-shell ANP; (b) the oxidizers mixtures of O<sub>2</sub>, CO<sub>2</sub>, and H<sub>2</sub>O; (c) the initial configuration of ANP surrounded by oxidizers.

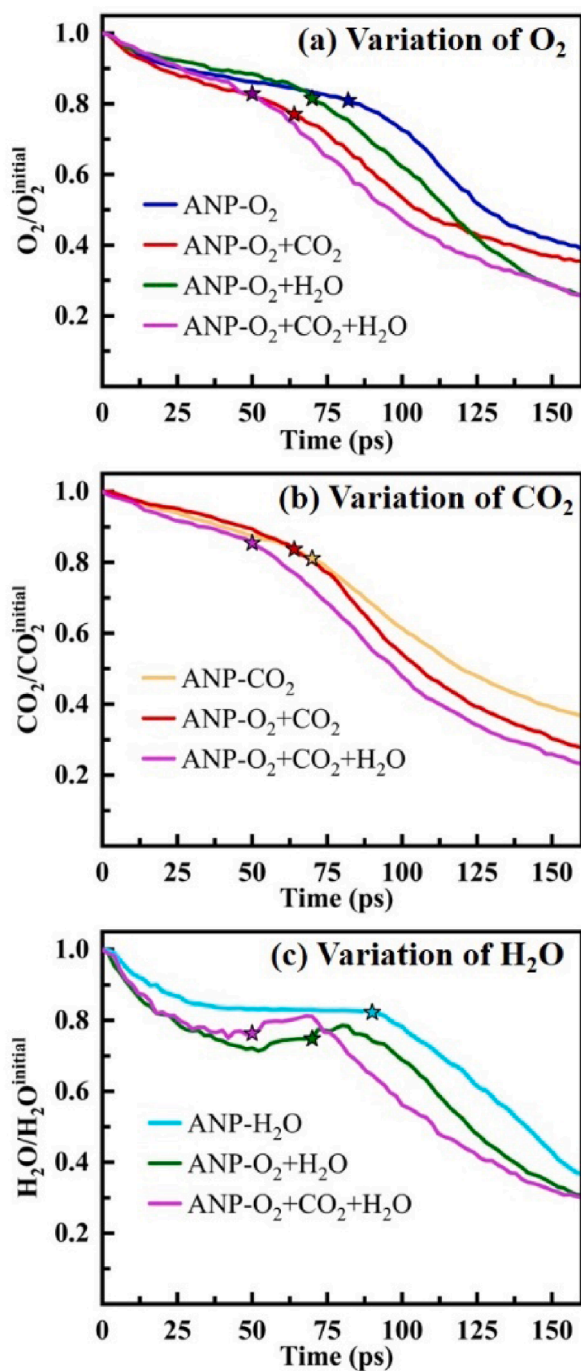


Fig. 4. Variation of (a)  $O_2$ , (b)  $CO_2$ , and (c)  $H_2O$  in six environments. The oxidizer concentrations are normalized by initial values. The star symbols represent ignition time.

formation and breaking of chemical bonds [34], and it is capable to compute the large-scale reactive systems (>1000 atoms), which is challenging to be described by DFT or nonreactive force fields. It has been proved that ReaxFF reactive force field can precisely characterize the microstructure of metal particles and it is suitable for simulating the physicochemical evolution of metal particles burning in oxidizers [35]. A systematic overview of the development, applications, and future directions of ReaxFF can be seen in reference [36] by Senftle et al. [36].

Bond-order between atom  $i$  and  $j$  ( $BO_{ij}$ ) can be directly calculated from the distance  $r_{ij}$ . The computation method is given as

$$BO_{ij} = BO_{ij}^{\sigma} + BO_{ij}^{\pi} + BO_{ij}^{\pi\pi} \\ = \exp[p_{bo1}(\frac{r_{ij}}{r_0^{\sigma}})^{p_{bo2}}] + \exp[p_{bo3}(\frac{r_{ij}}{r_0^{\pi}})^{p_{bo4}}] + \exp[p_{bo5}(\frac{r_{ij}}{r_0^{\pi\pi}})^{p_{bo6}}] \quad (1)$$

where  $p_{bo}$  terms are empirical parameters.  $r_0^{\sigma}$ ,  $r_0^{\pi}$ ,  $r_0^{\pi\pi}$  are equilibrium bond lengths of  $\sigma$ ,  $\pi$  and  $\pi\pi$  bond character, respectively.

Due to the description of bond formation and breaking, the expression for total energy used in the ReaxFF is calculated by

$$E_{system} = E_{bond} + E_{over} + E_{under} + E_{lp} + E_{val} + E_{tors} + E_{vdWaaals} + E_{Coulomb} \quad (2)$$

in which  $E_{system}$  is the total energy of the system.  $E_{bonds}$ ,  $E_{over}$ ,  $E_{under}$ ,  $E_{lp}$ ,  $E_{val}$ ,  $E_{tors}$  denote bond energy, overcoordination energy, undercoordination energy, lone pair energy, valence angle energy, and torsion angle energy, respectively. All of the above are bonding interactions energy, the van der Waals energy ( $E_{vdWaaals}$ ) and Coulomb energy ( $E_{Coulomb}$ ) are nonbonded interactions energy, which are calculated separately.

The parameters of ReaxFF adopted in this paper can be found in the literature by Hong and van Duin et al. [37]. The same parameters were conducted by many other scholars to explore ANPs' ignition and combustion [38], aggregation and sintering [39], and ethanol oxidation over ANP [40].

## 2.2. Simulation details

To simulate the ANP combustion in different atmospheres, a core-shell structure ANP model with a diameter of 6 nm Al core and 1 nm thickness alumina shell was first constructed. The oxide shell of ANP was amorphous, which was formed by annealing the  $\alpha$ -alumina. The number of core Al (cAl), shell Al (sAl), and shell O (sO) were 5388, 5778, and 8540, respectively. Then, the core-shell ANP relaxed for 160 ps under canonical ensemble (keep the number of atoms, volume, and temperature conserved, denoted as *NVT*) to obtain a more stable structure. The initial temperature of ANP was set as 300 K, and it was placed in the center of a  $160 \times 160 \times 160$  Å cubic box with periodic boundaries in all three directions. Moreover, a variety of typical oxidizers atmospheres models were established. Molecules in all atmospheres were randomly distributed, with a total number of 2700. All the oxidizers models were relaxed for 40 ps under *NVT* at 2000 K. The temperature of ANP and oxidizers were controlled by a Nose/Hoover thermostat. Finally, initial pre-oxidation systems were completed by combining the low-temperature core-shell ANP with the high-temperature oxidizers. The oxidation of ANP under different atmospheres was carried out in the microcanonical ensemble (keep the number of atoms, volume, and total energy conserved, denoted as *NVE*) with a timestep of 0.2 fs for 160 ps. This Non-Equilibrium Reactive Molecular Dynamics simulations were also employed by Rajabpour et al. to examine the heat transfer between a silver nanoparticle and surrounding water [41]. The timestep was proved to be suitable in references [15] and [39]. The temperature damping parameter was chosen to be 20 fs, 100 times of timestep. Detailed information on different systems is listed in Table 1. System ANP- $O_2$  means the ANP is surrounded by oxidizers consisting of  $O_2$  and so on.  $N_{O_2}$ ,  $N_{CO_2}$ , and  $N_{H_2O}$  represent the number of  $O_2$ ,  $CO_2$ , and  $H_2O$ . Fig. 1 shows the ANP model, oxidizers model, and initial configuration ready for subsequent oxidation simulation in system ANP- $O_2 + CO_2 + H_2O$ . All the molecular dynamics simulations and visualization in this paper were performed by LAMMPS [42,43] and OVITO [44], respectively.

## 3. Results and discussion

### 3.1. Heat transfer and reaction heat release before ignition

In the early oxidation stage, a lot of heat will be transferred to ANP due to the high gas temperature. In addition, accompanied by the re-

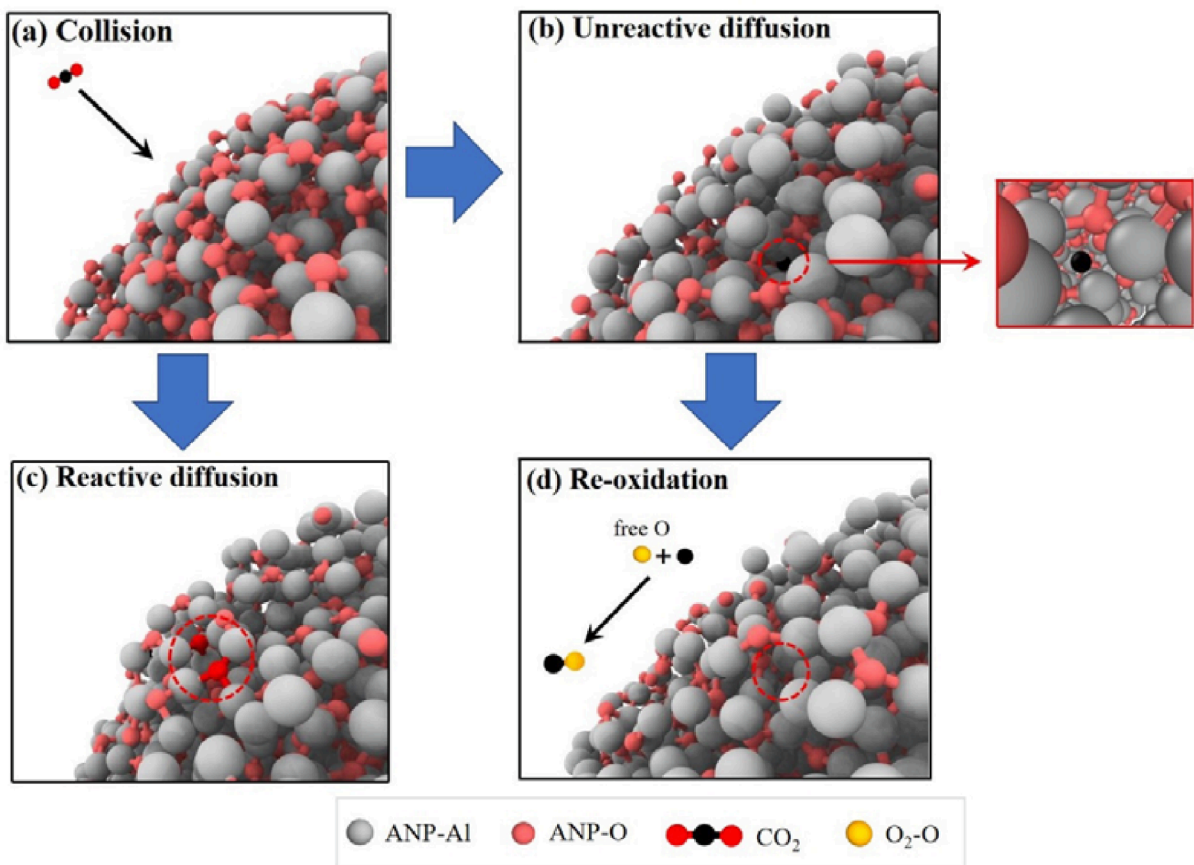


Fig. 5. Schematic diagram of (a) collision, (b) unreactive diffusion, (c) reactive diffusion, and (d) re-oxidation in system ANP-O<sub>2</sub> + CO<sub>2</sub>.

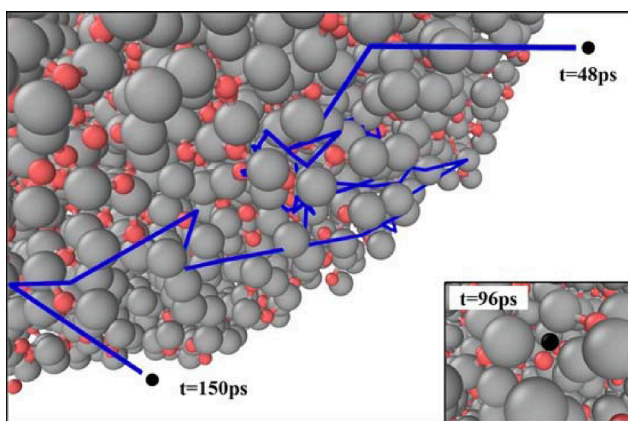


Fig. 6. Trajectory capturing the unreactive diffusion and detachment of C atom (grey, Al atom; red, O atom; black, C atom). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

action between ANP and oxidizers, a large amount of reaction heat will be generated. Both the heat transfer ( $Q_{trans}$ ) and reaction heat release ( $Q_{react}$ ) will increase the temperature of ANP, resulting in ANP ignition (the moment of core Al atoms consumption rate reaches its maximum). Thus, the ignition delay time ( $t_{ig}$ ),  $Q_{trans}$  and  $Q_{react}$  before ANP ignition in the six atmospheres were examined, and the results are shown in Fig. 2. The contribution of  $Q_{trans}$  and  $Q_{react}$  is calculated by [45]

$$Q = \frac{\Delta E}{3N_p k_B} \quad (3)$$

where  $N_p$  is the number of ANP atoms, and  $k_B$  is the Boltzman constant.  $\Delta E$  represents the energy variation of the oxidizers kinetic and system potential energy in the calculations of  $Q_{trans}$  and  $Q_{react}$ .

It can be seen in Fig. 2 that  $t_{ig}$  of mixed oxidizers environments are shorter than that in pure oxidizers environments. For example,  $t_{ig}$  of system ANP-O<sub>2</sub> + CO<sub>2</sub> is smaller than that of system ANP-O<sub>2</sub> and system ANP-CO<sub>2</sub>, as well as system ANP-O<sub>2</sub> + H<sub>2</sub>O, ANP-O<sub>2</sub>, and ANP-H<sub>2</sub>O. And  $t_{ig}$  of system ANP-O<sub>2</sub> + CO<sub>2</sub> + H<sub>2</sub>O is the shortest. Additionally, the right part of Fig. 2 shows that the total energy of ignition in different initial atmospheres is almost the same. It indicates that the ignition of ANP is independent on the oxidizers, which is consistent with the results of Chu et al. [24]. In the pure oxidizer systems (ANP-O<sub>2</sub>, ANP-CO<sub>2</sub>, and ANP-H<sub>2</sub>O), heat transfer to ANP in the H<sub>2</sub>O environment is much larger than that in the O<sub>2</sub> and CO<sub>2</sub>. Even in the mixed oxidizers systems (ANP-O<sub>2</sub> + CO<sub>2</sub>, ANP-O<sub>2</sub> + H<sub>2</sub>O, and ANP-O<sub>2</sub> + CO<sub>2</sub> + H<sub>2</sub>O),  $Q_{trans}$  increases when the oxidizing environment contains H<sub>2</sub>O molecules. However, compared with heat transfer, reaction heat release plays a more significant role in particle's ignition. Though  $Q_{trans}$  of system ANP-H<sub>2</sub>O is more than others, it experiences a long ignition delay time.

To further illustrate the heat transfer capacity of oxidizer molecules in the early stage of oxidation of ANP, the average heat transfer rate of different ambient gases (denoted as  $\bar{Q}_{trans}^*$ ) before ignition was investigated. (Since the duration of heat transfer from gas to ANP before ignition is different in the six environments,  $\bar{Q}_{trans}^*$  can better reflect the heat transfer capacity of different oxidizers.) As shown in Fig. 3, in the environment of three pure oxidizers, the relationship of heat transfer capacity can be expressed as  $\bar{Q}_{trans}^{H_2O} > \bar{Q}_{trans}^{CO_2} > \bar{Q}_{trans}^{O_2}$ . In the mixed oxidizers,  $\bar{Q}_{trans}^{O_2+H_2O} > \bar{Q}_{trans}^{O_2+CO_2+H_2O} > \bar{Q}_{trans}^{O_2+CO_2}$ . In addition,  $\bar{Q}_{trans}^{O_2} > \bar{Q}_{trans}^{CO_2}$  and  $\bar{Q}_{trans}^{H_2O}$  in the mixed oxidizers still follow the relationship in the pure oxidizers. The red curve in Fig. 3 shows the number of cAl-sO bond at ignition, which can reflect the core-shell reaction to a certain extent. It can be

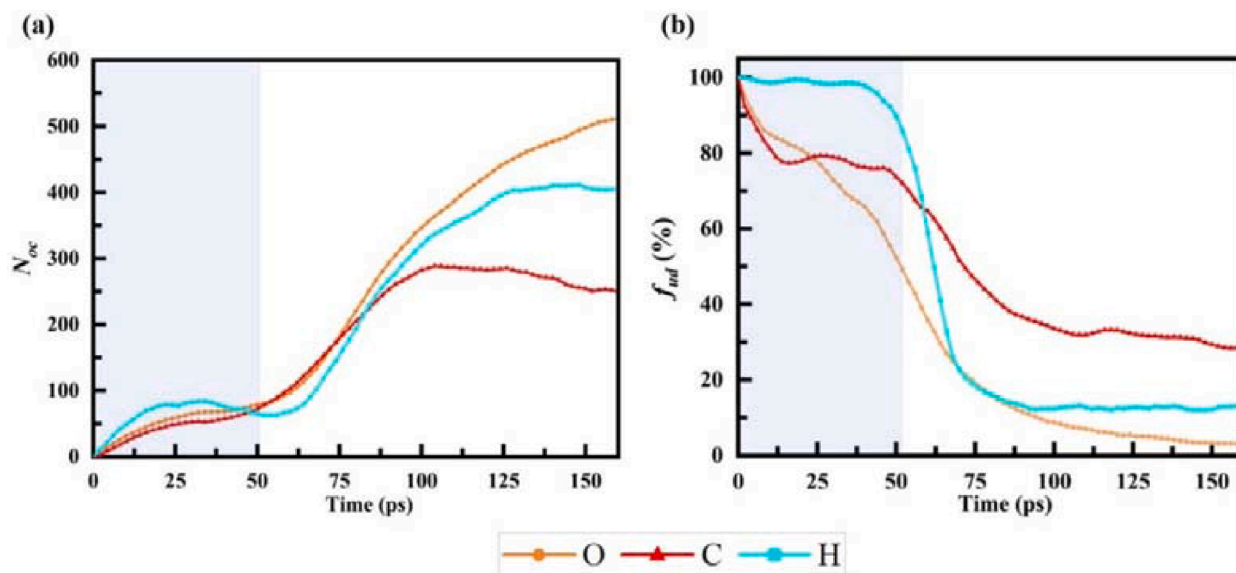


Fig. 7. (a) The number of oxidizer atoms collide into particle ( $N_{oc}$ ), and (b) corresponding fraction of oxidizer atoms in unreactive diffusion in the system ANP-O<sub>2</sub> + CO<sub>2</sub> + H<sub>2</sub>O. The shadow region represents the ignition stage.

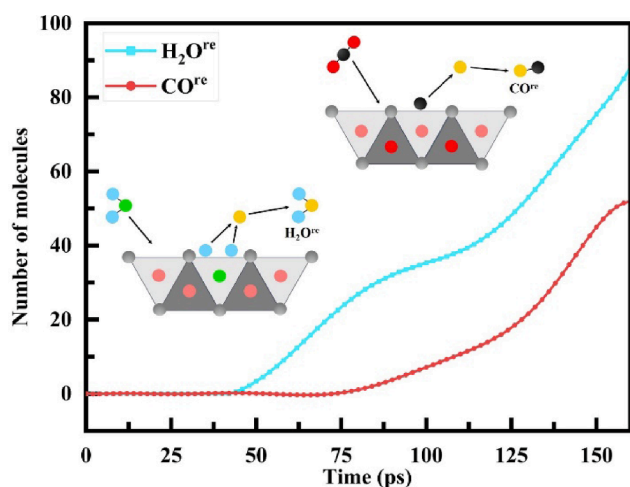


Fig. 8. Variations of H<sub>2</sub>O<sup>re</sup> and CO<sup>re</sup> during the re-oxidation process in the system ANP-O<sub>2</sub> + CO<sub>2</sub> + H<sub>2</sub>O. The illustration shows the formation of H<sub>2</sub>O<sup>re</sup> and CO<sup>re</sup> on ANP surface.

seen that the cAl-sO bond will be more in the atmosphere with a high average heat transfer rate. This is because the gas transfers more heat to the particle, causing the atoms in the particle move more violently. Then, the outward diffusion of cAl and the inward diffusion of sO are accelerated, and the cAl-sO bond will be created more easily.

### 3.2. Reaction mechanism between ANP and oxidizer mixtures

#### 3.2.1. Number of oxidizer molecules

As mentioned in Section 3.1, the reaction heat release is the main factor in the ignition of ANP. In this section, the number of oxidizer molecules during the oxidation will be discussed. The variation of ambient gas molecules is plotted in Fig. 4. Normalization was performed due to the difference in the number of initial gas molecules ( $O_2^{\text{initial}}$ ,  $CO_2^{\text{initial}}$ , and  $H_2O^{\text{initial}}$ ) in the six environments. In Fig. 4 (a) and (b), O<sub>2</sub> and CO<sub>2</sub> are consumed lightly before ignition. After ignition, the consumption rate of the two increase rapidly with the acceleration of the reaction. In the mixed oxidizer environments, the consumption fraction

of O<sub>2</sub> and CO<sub>2</sub> are larger than that in the pure oxidizer environments. Unlike O<sub>2</sub> and CO<sub>2</sub>, the number of H<sub>2</sub>O molecules (Fig. 4c) decrease quickly in the early stage. In the system ANP-H<sub>2</sub>O, after a sharp drop, the number of H<sub>2</sub>O molecules remain stable until ignition, indicating no extra H<sub>2</sub>O participate in the ANP oxidation at this stage. However, in the system ANP-O<sub>2</sub> + H<sub>2</sub>O and ANP-O<sub>2</sub> + CO<sub>2</sub> + H<sub>2</sub>O, the number of H<sub>2</sub>O increases slightly around ignition. It means that a few H<sub>2</sub>O molecules are generated during this period. Then, just like O<sub>2</sub> and CO<sub>2</sub>, H<sub>2</sub>O molecules also undergo a process of rapid consumption. At the end of the simulation, it is also observed that the proportion of H<sub>2</sub>O consumed in the mixed oxidizer environments are more significant than that in the pure H<sub>2</sub>O environment. In short, compared with pure oxidizer atmospheres, the oxidation of ANP in mixed oxidizer atmospheres consume more gas molecules.

#### 3.2.2. Reaction modes in oxidizer mixtures

The oxidation and combustion of ANP is the process of mutual diffusion between oxidizer atoms and particle atoms [15]. After diffusing into particle, a part of oxidizer atoms will bond with Al, while some will not. Taking the system ANP-O<sub>2</sub> + CO<sub>2</sub> as an example, Fig. 5 shows the three reaction modes oxidizer atoms involved in after colliding into particle. The CO<sub>2</sub> molecule slowly approaches ANP and collides with it. After the collision, the C—O bonds in the CO<sub>2</sub> molecule break. Then, C and O diffuse into ANP. The two O atoms are involved in reactive diffusion mode, bonding with Al atoms in the particle (Fig. 5c), while C atom does not (Fig. 5b). As the reaction proceeds, a new mode is observed: re-oxidation. If O<sub>2</sub> exists in the environment, the free O (from the O—O bond breaking in the environment O<sub>2</sub>) slowly approaches ANP. At the same time, the nonbonded C detaches from the ANP and bonds with the free O, producing CO. Finally, the CO diffuses into the environment. The collision, unreactive diffusion and reactive diffusion in Fig. 5(a), (b) and (c) is the basic process of ANP combustion [24]. However, the re-oxidation in Fig. 5(d) only appears in the mixed oxidizer environments. It allows the oxidizer atoms, which do not bond with ANP atoms, to bond with the free gas atoms, and further increase the reaction heat release. The experimental results of aluminum particle combustion in different oxidizing environments [46] may be explained by this oxidation process.

Typical MD trajectory of C is captured as indicated in Fig. 6 to illustrate the unreactive diffusion and re-oxidation. The O atoms in the gas are not shown in Fig. 6. At 48 ps, C atom appears near the ANP. After

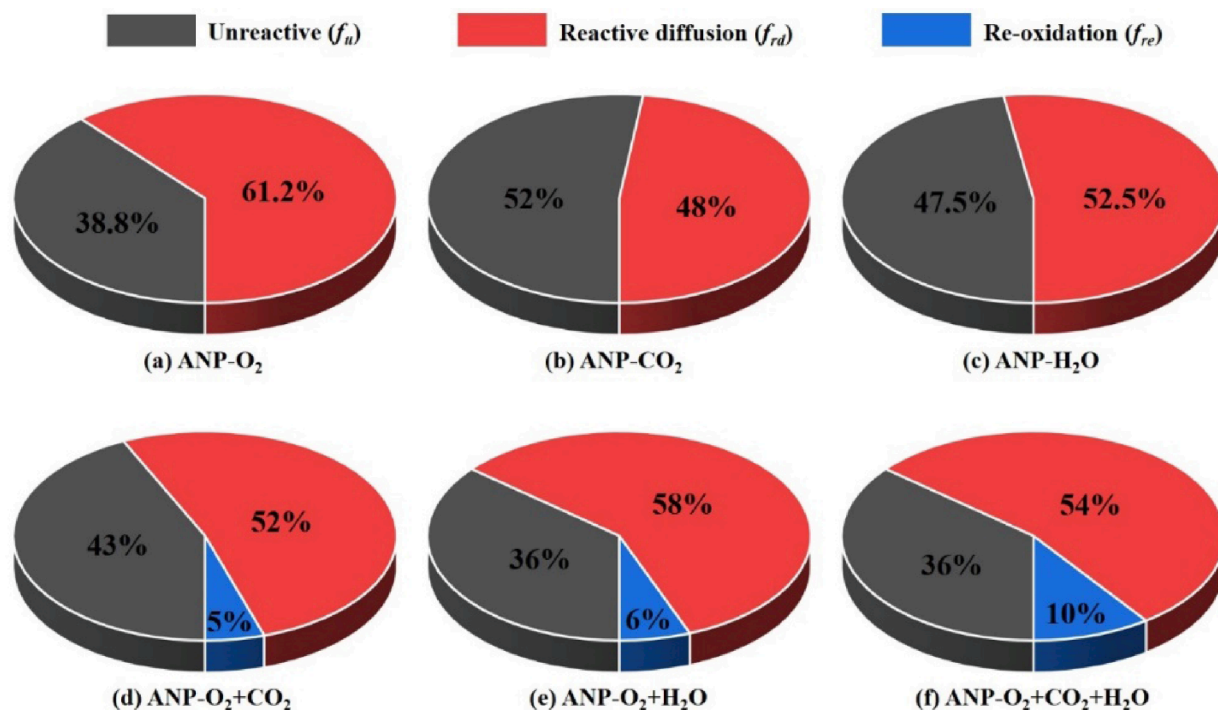


Fig. 9. Proportions of oxidizer atoms in unreactive, reactive diffusion, and re-oxidation at the end of the simulation in the six atmospheres.

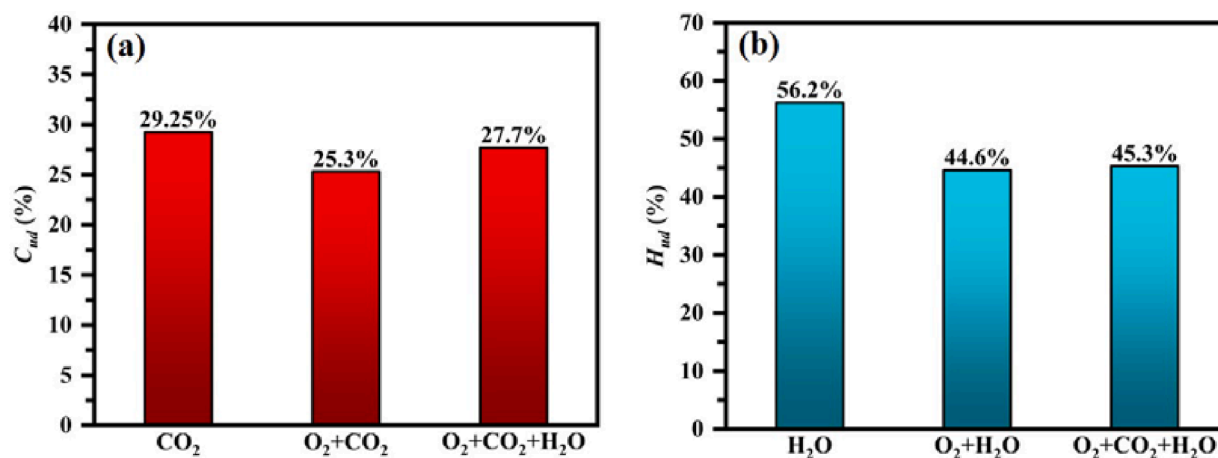


Fig. 10. Proportions of (a) C, (b) H atoms in unreactive diffusion at the end of simulation ( $t = 160$  ps).

the collision of CO<sub>2</sub> molecule and ANP, the C atom diffuses into particle. The snapshot in the lower right shows the unreactive diffusion C at 96 ps. Then, the C atom moves to the surface of ANP and detaches. Finally, at 150 ps, it appears in the distance. In fact, C atom has been bonded with O atom in oxygen at this moment. But it should be noted that from 48 ps to 150 ps, the C atom does not bond with Al or O in the ANP.

Based on the analysis above, oxidizer atoms fall into two categories which collide into the particle or move in the environment. Moreover, oxidizer atoms collide into particles contain unreactive diffusion and reactive diffusion. The unreactive diffusion oxidizer atoms do not bond with particle atoms. These atoms occupy binding sites around Al and transfer a lot of heat to ANP. When there exists another oxidizer in the environment, these atoms may be re-oxidized. Owing to the energy release of bonds, the oxidizer atoms in reactive diffusion and re-oxidation are the key sources of reaction heat release.

Furthermore, taking system ANP-O<sub>2</sub> + CO<sub>2</sub> + H<sub>2</sub>O as an example, the number of oxidizer atoms collide into particle and the fraction of

unreactive diffusion ( $f_{ud}$ ), defined as the ratio of the number of unreactive diffusion oxidizer atoms to the number of oxidizer atoms collide into particle (Eq (4)), are plotted in Fig. 7 to illustrate the behavior difference of C, H, and O atoms.

$$f_{ud} = \frac{N_{ud}}{N_{oc}} = \frac{N_{ud}}{N_{ud} + N_{rd}} \quad (4)$$

where  $N_{ud}$ ,  $N_{rd}$ , and  $N_{oc}$  are the number of oxidizer atoms in unreactive diffusion, reactive diffusion, and collide into particle.

As seen in Fig. 7(a), H atoms collide into particle are the fastest at the initial stage of the reaction. These high-temperature H atoms transfer plenty of heat to ANP. Thus, the average heat transfer rate of H<sub>2</sub>O in Fig. 3 is the largest. At the stage before ANP ignition (shadow in Fig. 7), the  $N_{oc}$  of H atoms rises rapidly and then falls, indicating that parts of H atoms break away from the particle and diffuse into the environment. Compared with H atoms, the  $N_{oc}$  of C atoms reaches a peak at about 100 ps, and it drops thereafter. This trend indicates that after 100 ps, the rate

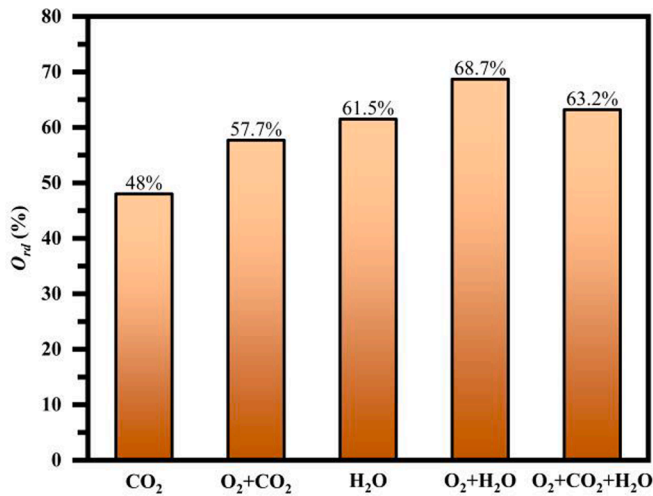


Fig. 11. Proportion of reactive diffusion for O atoms in the oxidizers at the end of the simulation ( $t = 160$  ps).

of C atoms collide into particle is less than that diffuse outward to the environment. The  $N_{oc}$  of O atoms keeps increasing during the whole reaction. At the end of the simulation, the  $N_{oc}$  of O atoms is the most, which reaches 513, more than that of H and C, 405 and 252, respectively. Observing the curves in Fig. 7(b), the  $f_{ud}$  of H atoms is almost 100 % before ignition. It means that these H atoms hardly bond with Al before ignition. The  $f_{ud}$  of C atoms decreases slightly faster than O at the initial stage. But at the stage of 15–50 ps, it is relatively stable. The reason should be that with the accumulation of C atoms on the particle surface, the reaction of subsequent C atoms is hindered [24]. At this stage, the  $f_{ud}$  of O atoms shrinks rapidly, and exceeds that of C atoms. After the ignition of ANP, the  $f_{ud}$  of C, H, and O atoms drops fleetly. After 75 ps, the  $f_{ud}$  curve of H atoms does not decrease significantly, and the  $N_{oc}$  curve is still increasing. It illustrates that the reaction rate of H atoms tends to be stable. Likewise, after 100 ps, the  $f_{ud}$  of C atoms almost does not decrease, but the  $N_{oc}$  curve shows a small drop, indicating that C atoms mainly undergo re-oxidation reaction at this stage, a large amount of C atoms diffusing outward. As for O atoms, its  $f_{ud}$  is the lowest. Almost all the O atoms colliding into ANP are involved in reactive diffusion, bonding with Al.

The variations of H<sub>2</sub>O and CO generated by re-oxidation (denoted as H<sub>2</sub>O<sup>re</sup> and CO<sup>re</sup>) and the re-oxidation process in system ANP-O<sub>2</sub> + CO<sub>2</sub> + H<sub>2</sub>O are shown in Fig. 8. After H<sub>2</sub>O molecule collides into particle, the

O atom bond with Al, while H atoms do not. At the stage of H atoms diffuse outward in Fig. 7(a), H<sub>2</sub>O<sup>re</sup> begin to appear, which means that re-oxidation occurs at this time. H atoms bond with free O in the environment and produce extra H<sub>2</sub>O. This is why the number of H<sub>2</sub>O in Fig. 4 (c) slightly increases. Similarly, the number of CO<sup>re</sup> begins to rise at about 75 ps, indicating that parts of C atoms experience re-oxidation and produce CO.

### 3.2.3. Influences of re-oxidation

In mixed atmospheres, re-oxidation will influence the behavior of oxidizer atoms. The fraction of oxidizer atoms in unreactive (including moves in the environment and unreactive diffusion), reactive diffusion, and re-oxidation (denoted as  $f_{iu}$ ,  $f_{rd}$ , and  $f_{re}$ ) in different environments are examined as shown in Fig. 9. They are calculated by

$$f_{iu} = \frac{N_e + N_{ud}}{N_{total}} \quad (5)$$

$$f_{rd} = \frac{N_{rd}}{N_{total}} \quad (6)$$

$$f_{re} = \frac{N_{re}}{N_{total}} \quad (7)$$

where  $N_{total}$  is the total number of oxidizer atoms in different atmospheres.  $N_e$ ,  $N_{ud}$ ,  $N_{rd}$ ,  $N_{re}$ , are the number of oxidizer atoms move in the environment, unreactive diffusion, reactive diffusion, and re-oxidation, respectively.

Based on the definition of reactive diffusion, it occurs between particle atoms and oxidizer atoms, which can reflect the oxidation degree of ANP. In Fig. 9, the lowest  $f_{rd}$  is the ANP-CO<sub>2</sub> system. Only 48 % of the 8,100 gas atoms participate in reactive diffusion. And the  $f_{rd}$  in system ANP-O<sub>2</sub> is the largest, indicating that the oxidation degree of ANP in O<sub>2</sub> environment is the highest. When adding O<sub>2</sub> in pure CO<sub>2</sub> or H<sub>2</sub>O, the  $f_{rd}$  will increase lightly. Moreover, in mixed gas environments, the  $f_{iu}$  significantly decreases due to the re-oxidation. In the system ANP-O<sub>2</sub> + CO<sub>2</sub>, the  $f_{iu}$  is only 43 %, which is 9 % lower than the system ANP-CO<sub>2</sub>. And 5 % gas atoms are involved in re-oxidation. Similarly, in system ANP-O<sub>2</sub> + H<sub>2</sub>O, the  $f_{iu}$  is 11.5 % lower than that in system ANP-H<sub>2</sub>O, and its  $f_{re}$  is 6 %. In the system ANP-O<sub>2</sub> + CO<sub>2</sub> + H<sub>2</sub>O, the  $f_{iu}$  is only 36 %, and the  $f_{re}$  even reaches 10 %. Notably, compared to system ANP-CO<sub>2</sub> and ANP-H<sub>2</sub>O, the  $f_{iu}$  in system ANP-O<sub>2</sub> + CO<sub>2</sub> and ANP-O<sub>2</sub> + H<sub>2</sub>O decrease significantly. It is because that plenty of nonbonded C and H atoms detach from the ANP, causing other gas atoms diffusion into ANP and bond with Al, increasing the reaction heat release.

To explore the influence of re-oxidation on C and H atoms

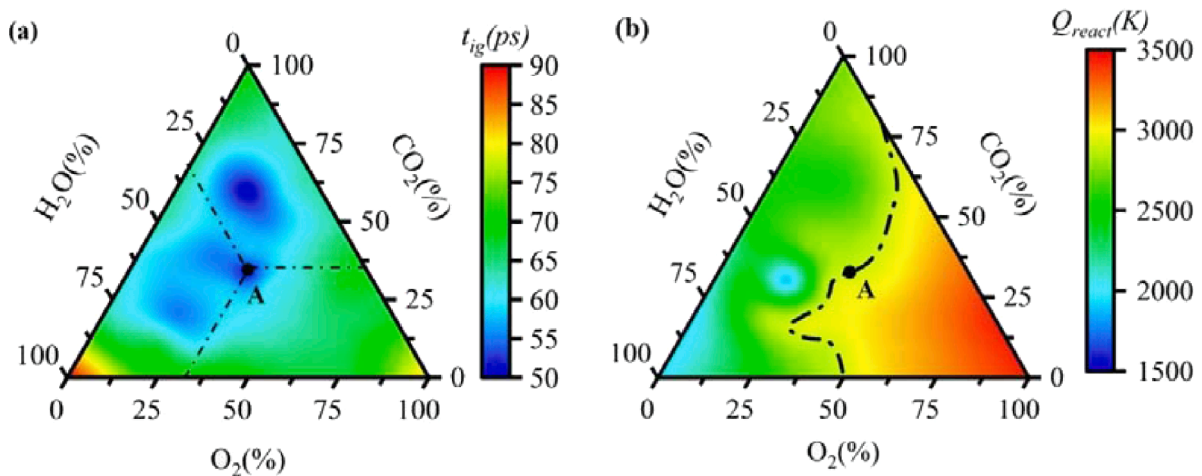


Fig. 12. (a) Ignition delay time and (b) reaction heat release in different atmospheres. Chain-dotted line in (a) is the coordinate of point A and (b) is the contour line of reaction heat release reaching 2900 K.

quantitatively, the fraction of C and H atoms involved in unreactive diffusion in different atmospheres (defined as the ratio of C or H atoms in unreactive diffusion to the total number of C or H atoms, denoted as  $C_{ud}$  and  $H_{ud}$ ) are examined, as shown in Fig. 10. According to Fig. 10(a), in the three environments containing  $\text{CO}_2$ ,  $C_{ud}$  in mixed oxidizers systems are 25.3 % and 27.7 %, slightly lower than that in system ANP- $\text{CO}_2$  (29.25 %). Fig. 10(b) shows that in the three environments containing  $\text{H}_2\text{O}$ ,  $H_{ud}$  values in mixed oxidizer systems are notably lower than that in system ANP- $\text{H}_2\text{O}$ . It indicates that re-oxidation reduces C and H atoms in unreactive diffusion inside the particle, releasing the binding site around Al atoms. And the reduction of H atoms is more significant than C atoms.

In addition, Fig. 11 shows the fraction of O atoms involved in reactive diffusion in different environments (defined as the ratio of O atoms in reactive diffusion to the total number of O atoms, denoted as  $O_{rd}$ ). It can be seen that  $O_{rd}$  in system ANP- $\text{O}_2 + \text{CO}_2$  is larger than that in system ANP- $\text{CO}_2$ . Similarly,  $O_{rd}$  in oxidizer mixtures of  $\text{O}_2$  and  $\text{H}_2\text{O}$  is more significant than that in a pure  $\text{H}_2\text{O}$  environment. And the  $O_{rd}$  in oxidizer mixtures of  $\text{O}_2$ ,  $\text{CO}_2$ , and  $\text{H}_2\text{O}$  is also more prominent than in a pure  $\text{CO}_2$  or  $\text{H}_2\text{O}$  environment. The increase of  $O_{rd}$  means that O atoms reoccupy the binding sites around the Al and bonding with Al atoms.

### 3.3. Optimize the ignition delay time and reaction heat release

The above analyses of heat transfer and reaction between oxidizer atoms and ANP are at the micro level. The specific effects of these phenomena on the macro mainly reflect the ignition delay time and reaction heat release of ANP. Therefore, the ignition delay time and reaction heat release of ANP in different environments are calculated. As shown in Fig. 12(a), ANP will experience a relatively long ignition delay time in an environment with more than 90 %  $\text{O}_2$  or  $\text{H}_2\text{O}$  (lower left and lower right regions in Fig. 12(a)). In environments with more  $\text{O}_2$ , the heat transfer from gas to ANP is poor at the initial oxidation stage, resulting in a slow temperature rise of ANP. And in environments with more  $\text{H}_2\text{O}$ , the heat transfer rate is fast in the early stage, but H atoms diffusing into ANP do not bond with Al, leading to less reaction heat. The ignition delay time of ANP will be effectively reduced if the contents of  $\text{CO}_2$  and  $\text{H}_2\text{O}$  in the range of 20 %–75 % and the content of  $\text{O}_2$  in the range of 10 %–50 % (blue region in Fig. 12(a)). As for reaction heat release, the environment with more  $\text{O}_2$  will relatively increase the reaction heat release, as shown in Fig. 12(b). When the concentration of  $\text{CO}_2$  and  $\text{H}_2\text{O}$  in the atmosphere is high, the reaction heat release will be low. Briefly, by tailoring the contents of three oxidizers ( $\text{O}_2$ ,  $\text{CO}_2$ , and  $\text{H}_2\text{O}$ ) in the environment, the ignition delay time and reaction heat release can be adjusted to achieve the optimal performance of ANP combustion. For instance, the chain-dotted line in Fig. 12(b) represents the contour line of reaction heat release ( $Q_{react}$ ) reaching 2900 K. Point A in Fig. 12(a) is the contents of oxidizers ( $n_{\text{O}_2} = 35\%$ ,  $n_{\text{CO}_2} = 32\%$ ,  $n_{\text{H}_2\text{O}} = 33\%$ ) with the shortest ignition delay time (50 ps) under the  $Q_{react}$  of 2900 K.

## 4. Conclusion

In this study, ReaxFF molecular dynamics simulations were performed to study the heat transfer and reaction heat release in the ignition and combustion process of ANP under  $\text{O}_2$ ,  $\text{CO}_2$ ,  $\text{H}_2\text{O}$ , and their mixture atmospheres. The ignition of ANP is triggered by heat transfer and reaction heat release, where the reaction heat release contributes more significantly. ANP experiences a shorter ignition delay time in mixed oxidizer atmospheres. The core-shell reaction of ANP is closely related to the average heat transfer rate of oxidizers. The number of Al-O bonds at ignition will increase in the atmosphere with a higher average heat transfer rate, resulting from the atoms in the particle move more violently. In the early stage of combustion,  $\text{H}_2\text{O}$  molecules transfer heat to ANP at the fastest rate due to the rapid diffusion of H atoms. Before ignition, H atoms almost do not bond with Al. C and O atoms

diffuse slowly in the early stage, but they bond with Al easily after collision with ANP. Collision, unreactive diffusion, and reactive diffusion are the basic processes during ANP oxidation. While in the environment of mixed oxidizers, oxidizer atoms will be involved in a new reaction mode: re-oxidation. Re-oxidation of H atoms occurs around ANP ignition. Nonbonded H atoms inside the particle diffuse to the environment and bond with free O atoms in the environment to produce  $\text{H}_2\text{O}$  molecules, resulting in a temporary increase in the quantity of  $\text{H}_2\text{O}$ . Re-oxidation of C atoms occurs after 75 ps and produces additional CO. The re-oxidation reduces the number of C and H atoms in unreactive diffusion and increases the fraction of O atoms in reactive diffusion. In addition, re-oxidation also increases the fraction of oxidizer atoms bonding with Al. In conclusion, this work reveals that the ANP combustion characteristics (ignition delay time and reaction heat release) are largely determined by the contents of  $\text{O}_2$ ,  $\text{CO}_2$ , and  $\text{H}_2\text{O}$  in the environment, which are expected to provide a theoretical guide for applying aluminum nanoparticles in various oxidizers.

### CRedit authorship contribution statement

**Yintao Zhou:** Investigation, Writing – original draft. **Baolu Shi:** Methodology, Writing – review & editing. **Qingzhao Chu:** Visualization, Writing – review & editing. **Lijuan Liao:** Supervision, Writing – review & editing.

### Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

### Data availability

Data will be made available on request.

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### References

- [1] D. Sundaram, V. Yang, R.A. Yetter, Metal-based nanoenergetic materials: synthesis, properties, and applications, *Prog. Energy Combust. Sci.* 61 (2017) 293–365, <https://doi.org/10.1016/j.pecs.2017.02.002>.
- [2] S. Gumus, H. Ozcan, M. Ozbey, B. Topaloglu, Aluminum oxide and copper oxide nanodiesel fuel properties and usage in a compression ignition engine, *Fuel* 163 (2016) 80–87, <https://doi.org/10.1016/j.fuel.2015.09.048>.
- [3] T.R. Sippel, T.L. Pourpoint, S.F. Son, Combustion of nanoaluminum and water propellants: effect of equivalence ratio and safety/aging characterization, *Propellants Explos. Pyrotech.* 38 (2013) 56–66, <https://doi.org/10.1002/prep.201200143>.
- [4] H.T. Huang, M.S. Zou, X.Y. Guo, R.J. Yang, Y.K. Li, Analysis of the aluminum reaction efficiency in a hydro-reactive fuel propellant used for a water ramjet, *Combust. Explos. Shock Waves* 49 (2013) 541–547, <https://doi.org/10.1134/S0010508213050055>.
- [5] J.M. Bergthorson, Recyclable metal fuels for clean and compact zero-carbon power, *Prog. Energy Combust. Sci.* 68 (2018) 169–196, <https://doi.org/10.1016/j.pecs.2018.05.001>.
- [6] C. Mandilas, G. Karagiannakis, A.G. Konstandopoulos, C. Beatrice, M. Lazzaro, G. Di Blasio, et al., Study of basic oxidation and combustion characteristics of aluminum nanoparticles under engine-like conditions, *Energy Fuel* 28 (2014) 3430–3441, <https://doi.org/10.1021/ef5001369>.
- [7] P. Bucher, R.A. Yetter, F.L. Dryer, E.P. Vicenzi, T.P. Parr, D.M. Hanson-Parr, Condensed-phase species distributions about Al particles reacting in various oxidizers, *Combust. Flame* 117 (1999) 351–361, [https://doi.org/10.1016/S0010-2180\(98\)00074-1](https://doi.org/10.1016/S0010-2180(98)00074-1).



- [8] Y.S. Kwon, A.A. Gromov, A.P. Ilyin, E.M. Popenko, G.H. Rim, The mechanism of combustion of superfine aluminum powders, *Combust. Flame* 133 (2003) 385–391, [https://doi.org/10.1016/S0010-2180\(03\)00024-5](https://doi.org/10.1016/S0010-2180(03)00024-5).
- [9] W. Wang, R. Clark, A. Nakano, R.K. Kalia, P. Vashishta, Effects of oxide-shell structures on the dynamics of oxidation of Al nanoparticles, *Appl. Phys. Lett.* 96 (2010) 1–4, <https://doi.org/10.1063/1.3425888>.
- [10] B. Wu, F.C. Wu, Y.B. Zhu, A.M. He, P. Wang, H.A. Wu, Fast reaction of aluminum nanoparticles promoted by oxide shell, *J. Appl. Phys.* (2019) 126, <https://doi.org/10.1063/1.5115545>.
- [11] Y. Li, R.K. Kalia, A. Nakano, P. Vashishta, Size effect on the oxidation of aluminum nanoparticle: multimillion-atom reactive molecular dynamics simulations, *J. Appl. Phys.* (2013) 114, <https://doi.org/10.1063/1.4823984>.
- [12] A. Rai, D. Lee, K. Park, M.R. Zachariah, Importance of phase change of aluminum in oxidation of aluminum nanoparticles, *J. Phys. Chem. B* 108 (2004) 14793–14795, <https://doi.org/10.1021/jp0373402>.
- [13] Q. Chu, B. Shi, L. Liao, Y. Zhou, K.H. Luo, N. Wang, Size-derived reaction mechanism of core-shell aluminum nanoparticle, *Appl. Phys. Lett.* (2020) 117, <https://doi.org/10.1063/5.0015367>.
- [14] T. Bazyn, H. Krier, N. Glumac, Combustion of nanoaluminum at elevated pressure and temperature behind reflected shock waves, *Combust. Flame* 145 (2006) 703–713, <https://doi.org/10.1016/j.combustflame.2005.12.017>.
- [15] Q. Chu, B. Shi, L. Liao, K.H. Luo, N. Wang, C. Huang, Ignition and oxidation of core-shell Al/Al<sub>2</sub>O<sub>3</sub> nanoparticles in an oxygen atmosphere: insights from molecular dynamics simulation, *J. Phys. Chem. C* 122 (2018) 29620–29627, <https://doi.org/10.1021/acs.jpcc.8b09858>.
- [16] A. Rai, K. Park, L. Zhou, M.R. Zachariah, Understanding the mechanism of aluminium nanoparticle oxidation, *Combust. Theory Model.* 10 (2006) 843–859, <https://doi.org/10.1080/13647830600800686>.
- [17] X. Zou, N. Wang, L. Liao, Q. Chu, B. Shi, Prediction of nano/micro aluminum particles ignition in oxygen atmosphere, *Fuel* 266 (2020), 116952, <https://doi.org/10.1016/j.fuel.2019.116952>.
- [18] X. Zhang, C. Fu, Y. Xia, Y. Duan, Y. Li, Z. Wang, et al., Atomistic origin of the complex morphological evolution of aluminum nanoparticles during oxidation: a chain-like oxide nucleation and growth mechanism, *ACS Nano* 13 (2019) 3005–3014, <https://doi.org/10.1021/acs.nano.8b07633>.
- [19] G. Li, L. Niu, W. Hao, Y. Liu, C. Zhang, Atomistic insight into the microexplosion-accelerated oxidation process of molten aluminum nanoparticles, *Combust. Flame* 214 (2020) 238–250, <https://doi.org/10.1016/j.combustflame.2019.12.027>.
- [20] Y. Tang, C. Kong, Y. Zong, S. Li, J. Zhuo, Q. Yao, Combustion of aluminum nanoparticle agglomerates: from mild oxidation to microexplosion, *Proc. Combust. Inst.* 36 (2017) 2325–2332, <https://doi.org/10.1016/j.proci.2016.06.144>.
- [21] K. Brandstadt, D.L. Frost, J.A. Kozinski, Preignition characteristics of nano- and micrometer-scale aluminum particles in Al-CO<sub>2</sub> oxidation systems, *Proc. Combust. Inst.* (2009) 32, <https://doi.org/10.1016/j.proci.2008.08.014>.
- [22] W. Yang, W. Shi, C. Chen, T. Zhang, J. Liu, Z. Wang, et al., Efficiency analysis of a novel electricity and heat co-generation system in the basis of aluminum–water reaction, *Int. J. Hydrogen Energy* 42 (2017) 3598–3604, <https://doi.org/10.1016/j.ijhydene.2016.08.207>.
- [23] S. Mercati, M. Milani, L. Montorsi, F. Paltrinieri, Design of the steam generator in an energy conversion system based on the aluminum combustion with water, *Appl. Energy* 97 (2012) 686–694, <https://doi.org/10.1016/j.apenergy.2012.01.028>.
- [24] Q. Chu, B. Shi, L. Liao, X. Zou, K.H. Luo, N. Wang, Reaction mechanism of the aluminum nanoparticle: physicochemical reaction and heat/mass transfer, *J. Phys. Chem. C* 124 (2020) 3886–3894, <https://doi.org/10.1021/acs.jpcc.9b11410>.
- [25] M. Saba, T. Kato, T. Oguchi, Chemical kinetics modeling for combustion of Al in CO<sub>2</sub>, *Combust. Flame* 233 (2021), 111613, <https://doi.org/10.1016/j.combustflame.2021.111613>.
- [26] B. Zhu, T. Du, Y. Sun, Oxidation kinetics of nano-aluminum in a carbon dioxide environment, *Prog. React. Kinet. Mech.* 41 (2016) 14–22, <https://doi.org/10.3184/146867816X14525972784045>.
- [27] F. Saceleanu, T.V. Vuong, E.R. Master, J.Z. Wen, Tunable kinetics of nanoaluminum and microaluminum powders reacting with water to produce hydrogen, *Int. J. Energy Res.* 43 (2019) 7384–7396, <https://doi.org/10.1002/er.4769>.
- [28] M.F. Russo, R. Li, M. Mench, A.C.T. Van Duin, Molecular dynamic simulation of aluminum-water reactions using the ReaxFF reactive force field, *Int. J. Hydrogen Energy* 36 (2011) 5828–5835, <https://doi.org/10.1016/j.ijhydene.2011.02.035>.
- [29] M. Zheng, X. Li, J. Liu, L. Guo, Initial chemical reaction simulation of coal pyrolysis via ReaxFF molecular dynamics, *Energy Fuel* 27 (2013) 2942–2951, <https://doi.org/10.1021/ef400143z>.
- [30] K. Chenoweth, A.C.T. van Duin, A. William, I. Goddard, ReaxFF reactive force field for molecular dynamics simulations of hydrocarbon oxidation, *Chem. A Eur. J.* 112 (2008) 1040–1053.
- [31] S. Huygh, A. Bogaerts, A.C.T. Van Duin, E.C. Neyts, Development of a ReaxFF reactive force field for titanium dioxide/water systems, *Comput. Mater. Sci.* 95 (2014) 579–591, <https://doi.org/10.1016/j.commatsci.2014.07.056>.
- [32] S. Hong, A. Krishnamoorthy, P. Rajak, S. Tiwari, M. Misawa, F. Shimojo, et al., Computational synthesis of MoS<sub>2</sub> layers by reactive molecular dynamics simulations: initial sulfidation of MoO<sub>3</sub> surfaces, *Nano Lett.* 17 (2017) 4866–4872, <https://doi.org/10.1021/acs.nanolett.7b01727>.
- [33] A.C.T. Van Duin, A. Strachan, S. Stewman, Q. Zhang, X. Xu, W.A. Goddard, ReaxFFSiO reactive force field for silicon and silicon oxide systems, *Chem. A Eur. J.* 107 (2003) 3803–3811, <https://doi.org/10.1021/jp0276303>.
- [34] A.C.T. Van Duin, S. Dasgupta, F. Lorant, W.A. Goddard, ReaxFF: a reactive force field for hydrocarbons, *Chem. A Eur. J.* 105 (2001) 9396–9409, <https://doi.org/10.1021/jp004368u>.
- [35] S. Hong, A.C.T. Van Duin, Molecular dynamics simulations of the oxidation of aluminum nanoparticles using the ReaxFF reactive force field, *J. Phys. Chem. C* 119 (2015) 17876–17886, <https://doi.org/10.1021/acs.jpcc.5b04650>.
- [36] T.P. Senftle, S. Hong, M.M. Islam, S.B. Kylasa, Y. Zheng, Y.K. Shin, et al., The ReaxFF reactive force-field: development, applications and future directions, *npj Comput. Mater.* 2 (2016), <https://doi.org/10.1038/npjcompumats.2015.11>.
- [37] S. Hong, A.C.T. Van Duin, Atomistic-scale analysis of carbon coating and its effect on the oxidation of aluminum nanoparticles by ReaxFF-molecular dynamics simulations, *J. Phys. Chem. C* 120 (2016) 9464–9474, <https://doi.org/10.1021/acs.jpcc.6b00786>.
- [38] P. Liu, J. Liu, M. Wang, Ignition and combustion of nano-sized aluminum particles: A reactive molecular dynamics study, *Combust. Flame* 201 (2019) 276–289, <https://doi.org/10.1016/j.combustflame.2018.12.033>.
- [39] Y. Cheng, Y. Zhao, F. Zhao, S. Xu, X. Ju, C. Ye, ReaxFF simulations on the combustion of Al and n-butanol nanofluid, *Fuel* 330 (2022), <https://doi.org/10.1016/j.fuel.2022.125465>.
- [40] Y.R. Zhang, A.C.T. van Duin, K.H. Luo, Investigation of ethanol oxidation over aluminum nanoparticle using ReaxFF molecular dynamics simulation, *Fuel* 234 (2018) 94–100, <https://doi.org/10.1016/j.fuel.2018.06.119>.
- [41] A. Rajabpour, R. Seif, S. Arabha, M.M. Heyhat, S. Merabia, A. Hassanali, Thermal transport at a nanoparticle-water interface: A molecular dynamics and continuum modeling study, *J. Chem. Phys.* 150 (2019), <https://doi.org/10.1063/1.5084234>.
- [42] A.P. Thompson, H.M. Aktulga, R. Berger, D.S. Bolintineanu, W.M. Brown, P. S. Crozier, et al., LAMMPS - a flexible simulation tool for particle-based materials modeling at the atomic, meso, and continuum scales, *Comput. Phys. Commun.* 271 (2022), 108171, <https://doi.org/10.1016/j.cpc.2021.108171>.
- [43] H.M. Aktulga, J.C. Fogarty, S.A. Pandit, A.Y. Grama, Parallel reactive molecular dynamics: Numerical methods and algorithmic techniques, *Parallel Comput.* 38 (2012) 245–259, <https://doi.org/10.1016/j.parco.2011.08.005>.
- [44] A. Stukowski, Visualization and analysis of atomistic simulation data with OVITO—the Open Visualization Tool, *Model. Simul. Mater. Sci. Eng.* 18 (2010), <https://doi.org/10.1088/0965-0393/18/1/015012>.
- [45] Q. Chu, X. Chang, D. Chen, A physicochemical model for the combustion of aluminum nano-agglomerates in high-speed flows, *Combust. Flame* 237 (2022), 111739, <https://doi.org/10.1016/j.combustflame.2021.111739>.
- [46] F. Halter, V. Glasziou, M. Di Lorenzo, S. Gallier, C. Chauveau, Peculiarities of aluminum particle combustion in steam, *Proc. Combust. Inst.* (2022) 1–10, <https://doi.org/10.1016/j.proci.2022.07.120>.